

# Top Quark Precision Physics at Linear Colliders

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1 Linear  $e^+e^-$  colliders provide a rich set of opportunities for precision top physics, crucial for  
2 the understanding of electroweak symmetry breaking and for the search for physics beyond  
3 the Standard Model. A  $t\bar{t}$  threshold scan in  $e^+e^-$  annihilation enables a precise measure-  
4 ment in theoretically well-defined mass schemes with small experimental and theoretical  
5 systematic uncertainties. Above the production threshold, the efficient identification to  
6 top pair events combined with polarized beams provides the potential to extract the form  
7 factors for the top quark couplings with high precision and in a model-independent way,  
8 resulting in excellent sensitivity to physics beyond the standard model. This contribution  
9 provides an overview of top physics at linear colliders based on results from full-simulation  
10 studies of top quark pair production in the detectors proposed for ILC and CLIC.

## 11 1 Introduction

12 As the heaviest particle in the Standard Model, the top quark has a special role. Due to its  
13 high mass, it has the strongest coupling to the Higgs field of all known particles. It also takes a  
14 central role in many models of New Physics, and thus provides a high sensitivity for phenomena  
15 beyond the Standard Model.

16 To date, the top quark is the only quark that has only been studied at hadron colliders.  
17 The clean experimental environment in  $e^+e^-$  collisions enables the study of all decay modes  
18 of the top quark with high resolution and very low background levels. The measurements at  
19 lepton colliders also profit from the high precision of theoretical calculations, which result in  
20 small overall systematic uncertainties.

21 At  $e^+e^-$  colliders, there are two different main top physics programs. The first is the study  
22 of the threshold for top quark pair production, which provides access to the detailed properties  
23 of the top quark. The second is the use of the top quark as a tool for the search for physics  
24 beyond the Standard Model, for example by precisely measuring its coupling to the electroweak  
25 interactions. In the first case, collision energies at several different values around 350 GeV are  
26 necessary, while the second program requires energies substantially in excess of the threshold  
27 for top pair production, in the order of 500 GeV or higher. In particular the energies above  
28 threshold are uniquely available at linear  $e^+e^-$  colliders.

29 Two such high-energy  $e^+e^-$  colliders are currently being developed in international collab-  
30 oration, the International Linear Collider (ILC) [1] and the Compact Linear Collider (CLIC)  
31 [2]. They are based on different acceleration technologies, resulting in a different energy reach  
32 for the full projects. ILC is based on superconducting RF structures, and is planned as a 500  
33 GeV collider with operation at different energies from 250 GeV to 500 GeV, including the re-  
34 gion around the  $t\bar{t}$  threshold, and the possibility for upgrades to the TeV region. CLIC uses a

35 normal-conducting two-beam acceleration scheme, and is foreseen to be constructed in several  
 36 stages. It has an ultimate energy of 3 TeV and two lower energy stages to maximise the physics  
 37 potential, with the first stage covering the  $t\bar{t}$  threshold. For ILC, the technical design report  
 38 has been completed, while for CLIC a conceptual design report was delivered, with a technical  
 39 design phase still ongoing until 2018.

40 In the following, the top physics program at these future colliders is illustrated based on  
 41 two examples that have been studied with detailed simulations with realistic detector models  
 42 including physics and machine-related backgrounds. For the  $t\bar{t}$  threshold scan, studies have  
 43 been performed both in the context of ILC and CLIC, while the investigation of the physics  
 44 potential for measurements of the electroweak couplings of the top quark have been performed  
 45 for ILC at 500 GeV.

## 46 2 A top threshold scan at ILC and CLIC

47 The cross section of  $t\bar{t}$  production close to the threshold strongly depends on the top quark  
 48 mass. In addition, it receives contributions from the top quark width, from the strong coupling  
 49 and from the top Yukawa coupling. The top width influences the shape of the would-be bound  
 50 state of the  $t\bar{t}$  pair. The strong coupling and the top Yukawa coupling, which both influence the  
 51 interaction of the two top quarks, primarily affect the overall magnitude of the cross section.  
 52 Beyond those effects connected to the  $t\bar{t}$  system, the cross section also receives corrections due  
 53 to initial state radiation (ISR) and due to the luminosity spectrum of the collider. The pure  
 54  $e^+e^- \rightarrow t\bar{t}$  cross section can be calculated with high precision, resulting in clean theoretical  
 55 predictions for the observables based on theoretically well-defined parameters, such as the 1S  
 56 mass of the top quark.

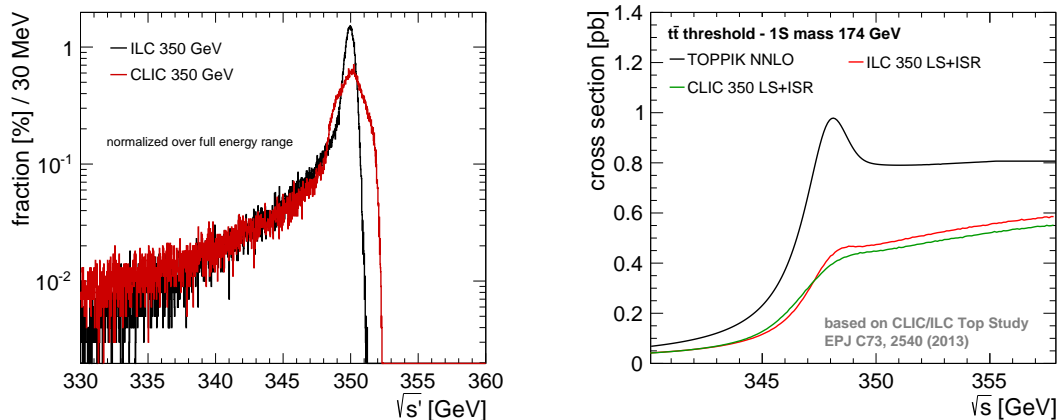


Figure 1: The luminosity spectrum for ILC and CLIC at 350 GeV (*left*) and the resulting total  $t\bar{t}$  cross section in the threshold region based on TOPPIK NNLO calculations [3, 4] including ISR and luminosity spectrum effects.

57 Figure 1 shows the luminosity spectrum of both ILC and CLIC at an energy of 350 GeV,  
 58 and illustrates the effect of these spectra together with initial state radiation on the pure  $t\bar{t}$

59 production cross section calculated with NNLO QCD [3, 4]. The luminosity spectrum and ISR  
60 result in an overall reduction of the effective cross section since they shift a fraction of the  
61 luminosity below the threshold energy, and lead to a broadening of the threshold turn-on due  
62 to the low-energy tail and due to the width of the main luminosity peak. Since the beam energy  
63 spread is larger at CLIC than at ILC, the smearing is slightly more pronounced at CLIC.

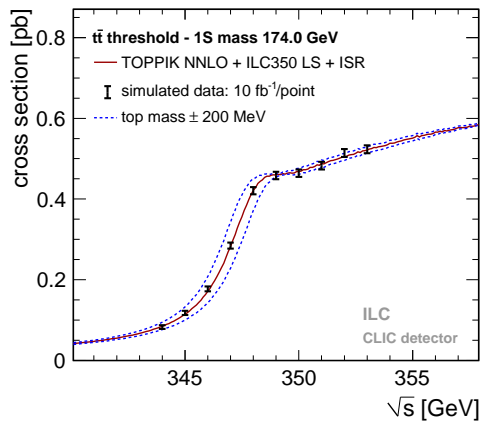


Figure 2: A simulated  $t\bar{t}$  threshold scan at ILC with 10 points spaced by 1 GeV each, assuming an integrated luminosity of  $10 \text{ fb}^{-1}$  per point with unpolarised beams. For illustration purposes, the effect of a shift in the 1S top quark mass by  $\pm 200 \text{ MeV}$  is shown in addition to the simulated data points. Figure taken from [6].

64 With full detector simulations of the CLIC\_ILD concept [5] the reconstruction efficiencies  
65 for  $t\bar{t}$  events and the rejection efficiency for Standard Model background was determined in  
66 the threshold region. These efficiencies are used to simulate threshold scans at ILC and CLIC,  
67 as illustrated in Figure 2. From these scans, the top mass is determined via a template fit  
68 of the measured cross section. With a 10-point scan with a total integrated luminosity of  
69  $100 \text{ fb}^{-1}$  assuming unpolarised beams, the top quark mass can be determined with a statistical  
70 uncertainty of 18 MeV in the case of ILC and 21 MeV in the case of CLIC [6]. The current  
71 precision of  $\alpha_s$  of 0.0007 leads to a systematic uncertainty of equal magnitude (18 MeV for ILC,  
72 20 MeV for CLIC), which is expected to improve in the future with a more precise determination  
73 of the strong coupling constant.

74 In addition there are experimental systematic uncertainties from several sources, such as  
75 the beam energy and the reconstruction efficiency and background contamination, which are  
76 expected to have total size below 50 MeV. On top of that, there are theoretical systematics due  
77 to the precision of the calculation of the total  $t\bar{t}$  cross section. These depend on the details of  
78 the calculations, and are still being evaluated. With the simplified assumption of a 3% overall  
79 normalisation uncertainty, the resulting systematic uncertainty of the mass is around 50 MeV,  
80 making theoretical uncertainties potentially the leading source of systematics.

81 A potentially important source of experimental systematics is the knowledge of the luminos-  
82 ity spectrum. The impact of this has been studied for CLIC by reconstructing the luminosity  
83 spectrum from simulated measurements of large-angle Bhabha scattering [7]. In a preliminary  
84 study, the uncertainty resulting from the precision of the reconstructed luminosity spectrum

85 has been found to be on the order of 6 MeV, demonstrating that this is not a limiting factor  
 86 for the overall precision of the top quark mass measurement. Since the luminosity spectrum at  
 87 ILC is less complicated than the one at CLIC, even smaller uncertainties are expected for the  
 88 ILC case.

89 Overall, a  $t\bar{t}$  threshold scan at linear colliders is expected to provide the top quark mass  
 90 in a theoretically well-defined mass scheme with sub-100 MeV total uncertainty, which would  
 91 provide a knowledge of the  $\overline{MS}$  mass of the top quark on the 100 MeV level or better. Given the  
 92 dominance of systematics and the uncertainties involved in the conversion from the 1S to the  
 93  $\overline{MS}$  mass, the small differences in statistical uncertainties between the different linear collider  
 94 options are insignificant.

### 95 3 Electroweak couplings

96 The capability for polarised beams at linear colliders provides excellent conditions to probe  
 97 the electroweak couplings of the top quark in  $t\bar{t}$  production above threshold. These couplings  
 98 are precisely determined in the Standard Model, but may receive substantial modifications in  
 99 scenarios with physics beyond the SM, such as extra dimensions and Higgs compositeness. The  
 100 measurement of the total production cross section, the forward-backward asymmetry and the  
 101 helicity angle, each for two different polarisation configurations, provides sufficient information  
 102 to fully constrain the top quark couplings with high precision. Since the asymmetry and  
 103 angle measurements require the identification of the top quark charge and rely on the correct  
 104 association of  $W$  bosons and  $b$  jets to top candidates, these measurements profit from higher  
 105 energy which provides a clean separation of the two top quarks in the  $t\bar{t}$  system.

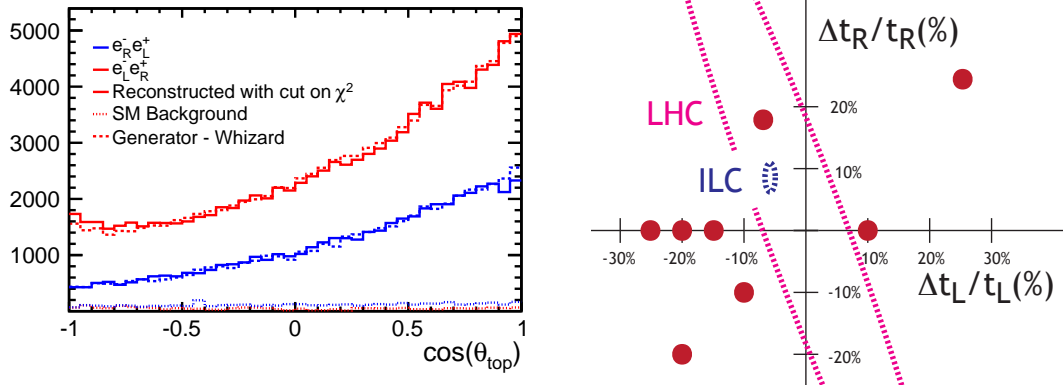


Figure 3: The forward-backward asymmetry of  $t\bar{t}$  production at 500 GeV in a full simulation study for two different polarisation configurations of the beams ( $\pm 80\% e^-$ ,  $\mp 30\% e^+$  polarisation) (*left*). Figure taken from [8]. The precision achievable at ILC at 500 GeV with an integrated luminosity of  $500 \text{ fb}^{-1}$  for the left- and right-handed couplings of the top quark, compared to the expected precision achievable at LHC [9].

106 Figure 3 *left* shows the forward-backward asymmetry in a full simulation study with the ILD  
 107 detector [10] for an integrated luminosity of  $500 \text{ fb}^{-1}$  at an energy of 500 GeV at ILC. The total

108 integrated luminosity is equally split between two polarisation configurations of  $\pm 80\%$ ,  $\mp 30\%$   
109 for electrons and positrons, respectively [8]. From this measurement, the forward-backward  
110 asymmetry is extracted with a  $\sim 2\%$  uncertainty including statistical and systematic contribu-  
111 tions. Similarly, the helicity angle distribution can be extracted with a precision of 4%, and  
112 the total cross section with a 0.5% uncertainty. From these results, the left- and right-handed  
113 couplings can be extracted with a 0.7% and 1.8% precision, respectively [8, 9]. This precision  
114 is illustrated in Figure 3 *right* together with the predicted deviations from the Standard Model  
115 for several scenarios of New Physics and with the precision expected from the LHC [9]. This  
116 clearly illustrates the immense power of a polarised high-energy electron-positron collider not  
117 only to discover possible new phenomena in the top sector, but also to precisely pin down the  
118 underlying mechanism if deviations from the Standard Model are observed.

## 119 4 Summary

120 The future linear electron-positron colliders ILC and CLIC provide excellent opportunities for a  
121 precise study of the top quark sector. With polarised beams, the possibility for a scan of the  $t\bar{t}$   
122 production threshold and with measurements of the electroweak couplings of the top quark at  
123 energies substantially above the threshold they will provide high precision measurements of top  
124 quark properties and significant sensitivity for various physics scenarios beyond the Standard  
125 Model. A linear collider will determine the top-quark mass in the theoretically well-defined  
126  $\overline{MS}$  scheme with a total precision of 100 MeV or better, and is capable of a percent-level  
127 measurement of the top electroweak couplings, which provides sensitivity to new physics scales  
128 extending substantially beyond the direct reach of present colliders.

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