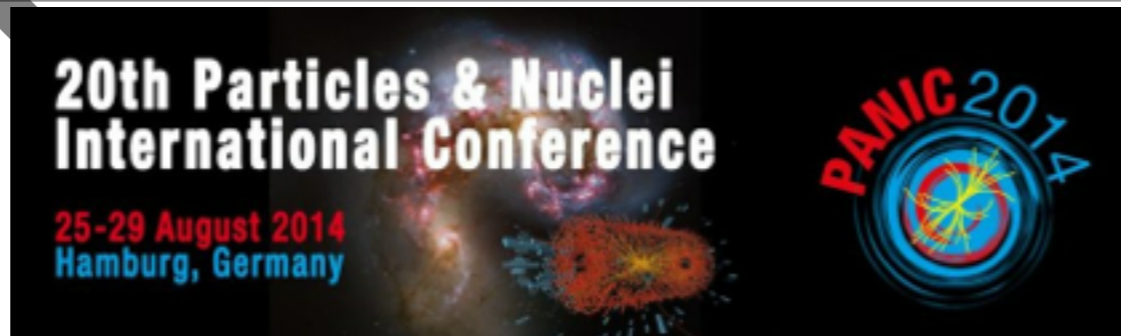


Top Quark Precision Physics at Linear Colliders

Frank Simon,
Max-Planck-Institut für Physik
Munich, Germany

on behalf of the ILC Physics & Detector Study and CLICdp

PANIC, Hamburg, August 2014

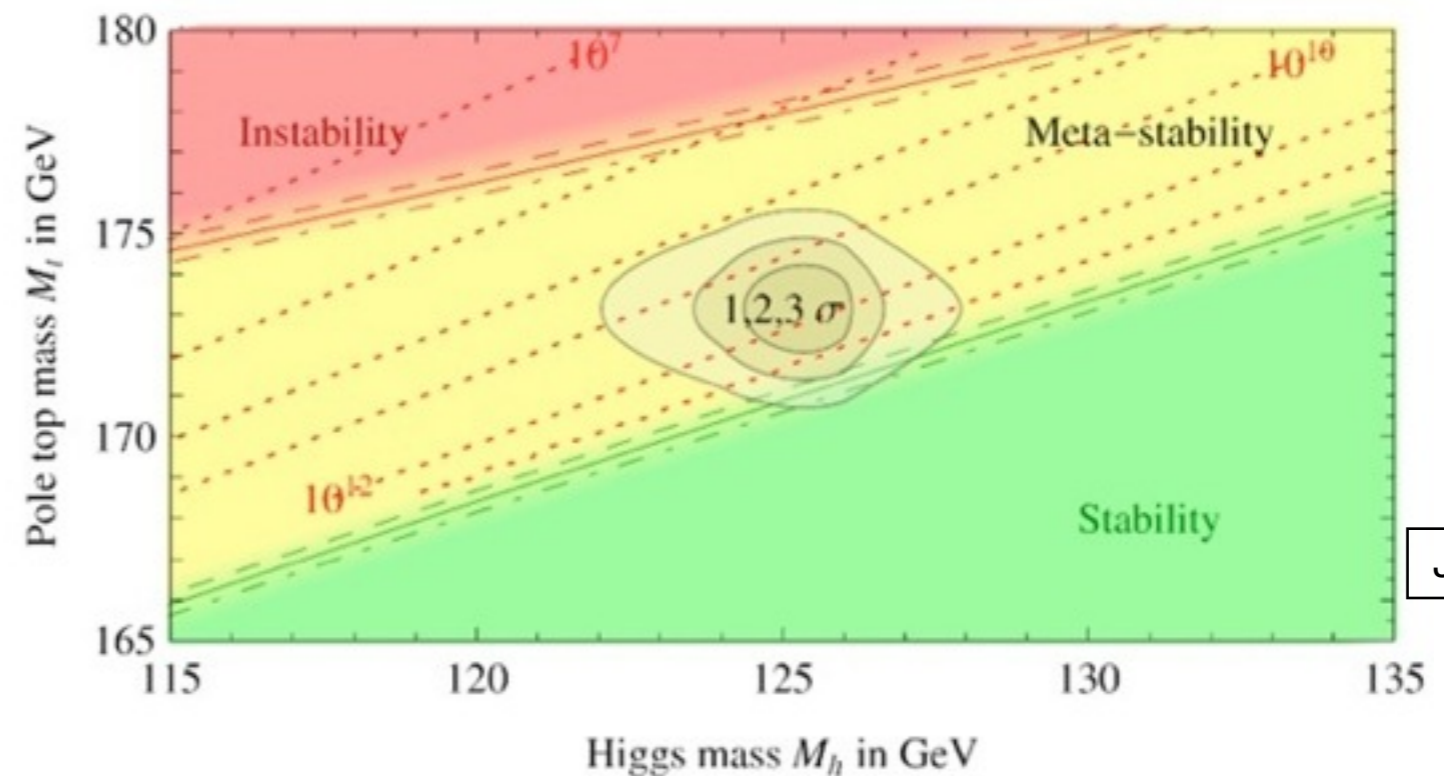
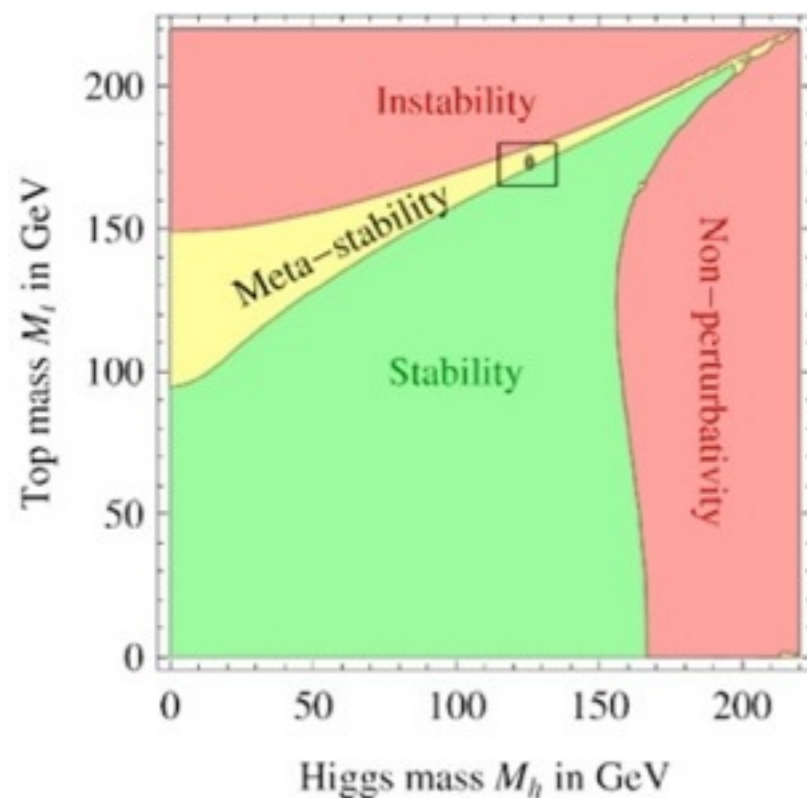


Outline

- Introduction: motivation for precision
- Linear Colliders in brief
- Top quarks in e^+e^- collisions
- Top properties: Mass
- Top as a BSM probe: Electroweak couplings
- Summary

Top Physics - Motivation for Precision

- Key motivation for future energy frontier colliders after the Higgs discovery:
 - Full understanding of EWSB
 - Discovering / constraining New Physics to provide answers to open questions
- ▶ As the heaviest SM particle, the Top plays an important role in this: Strongest coupling to the Higgs field, potential sensitivity to New Physics
 - The top mass is the leading uncertainty in the study of the vacuum stability of the SM



JHEP 08, 98 (2012)

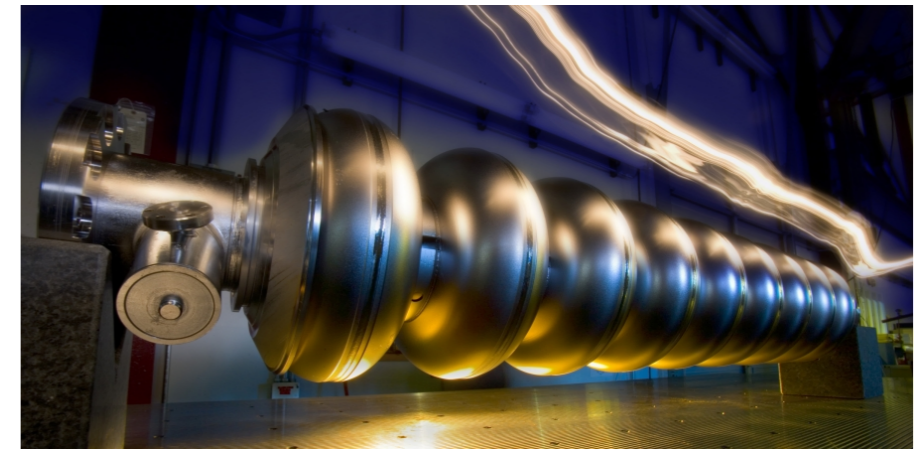
- Deviations from the SM expectations in electroweak couplings could point to BSM physics at higher scales

Linear Colliders - In Brief

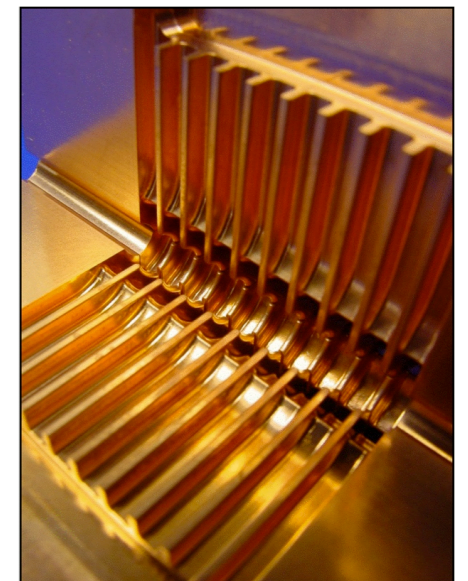
- Two accelerator concepts for an energy-frontier e^+e^- collider with an energy reach up to the top pair threshold and beyond:



- ILC - 500 GeV with 250 GeV initial stage, extendable to 1 TeV, based on SCRF with gradients of ~ 35 MV/m
TDR completed - almost shovel-ready

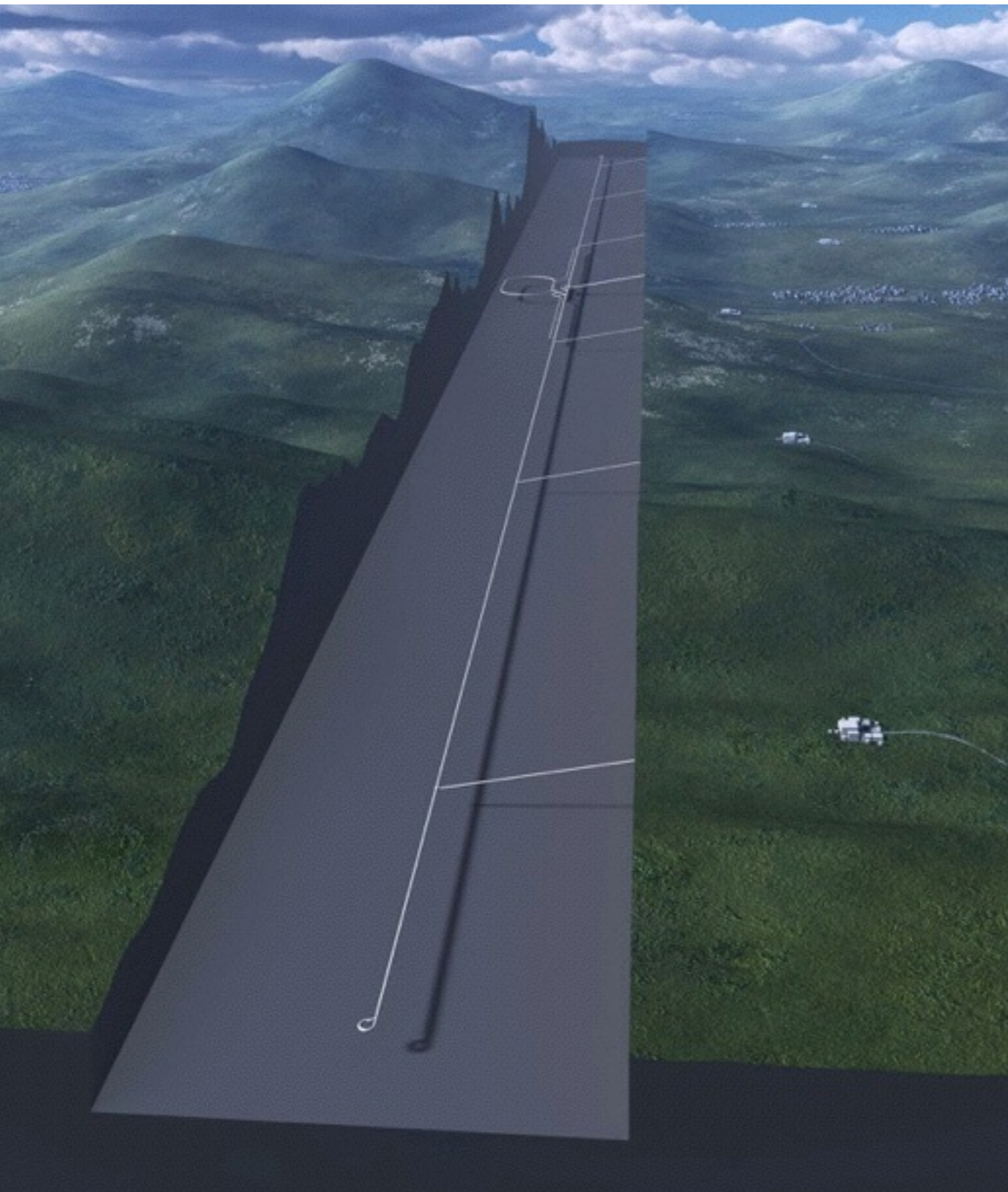


- CLIC - 3 TeV with two lower-energy stages, based on two-beam acceleration with warm RF, gradients of 100 MV/m
CDR completed - Development phase until ~ 2018 to reach maturity for construction



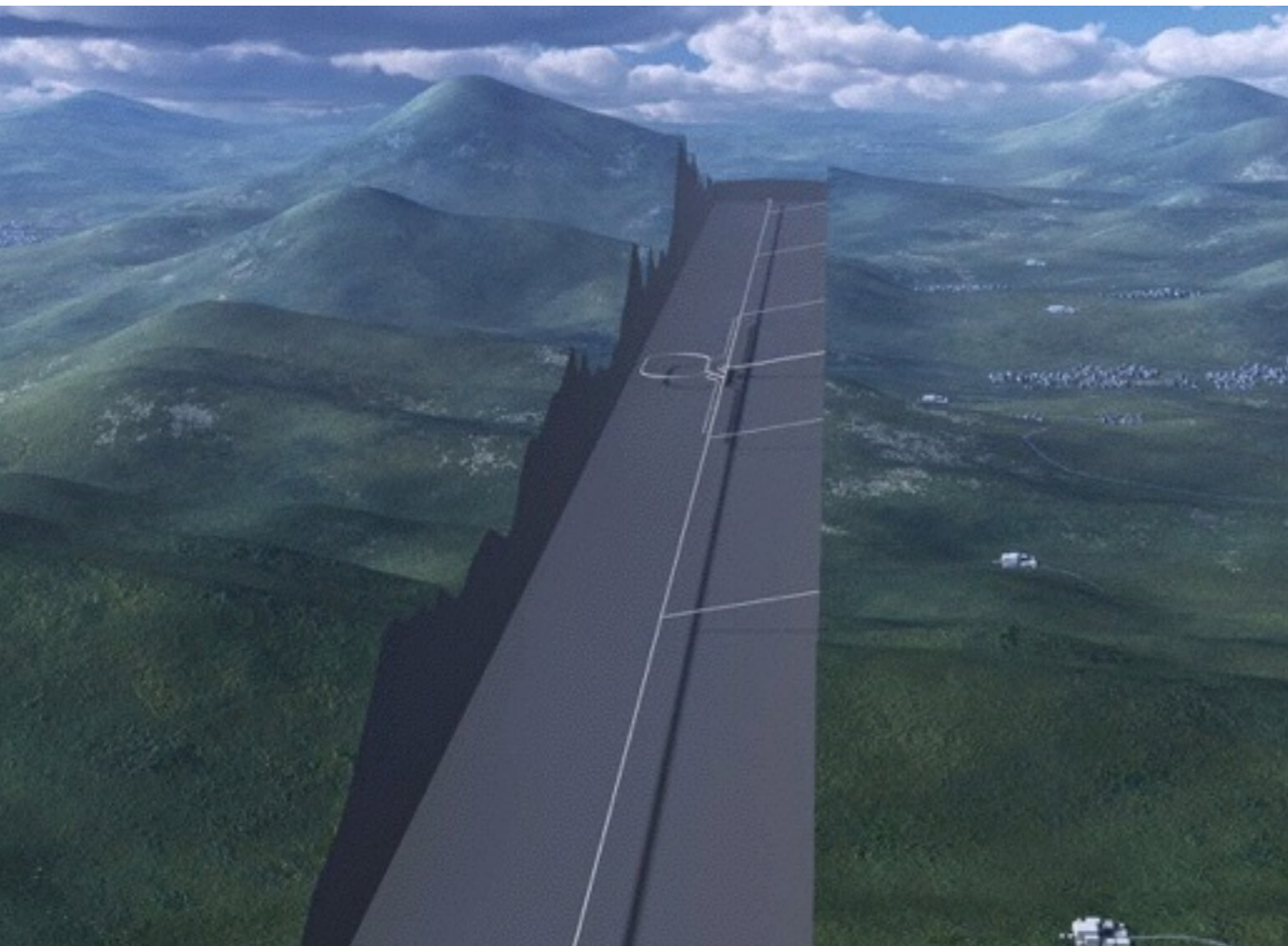
- ▶ Both provide luminosities on the $1 - 2 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$ level at the top threshold, possibilities for threshold scans and polarized beams

Linear Colliders - In Brief



- ILC: Site selected in Japan: Kitakami, north of Sendai
 - 30 km for 500 GeV, 50 km for 1 TeV
- Now: Discussions on political levels...

Linear Colliders - In Brief

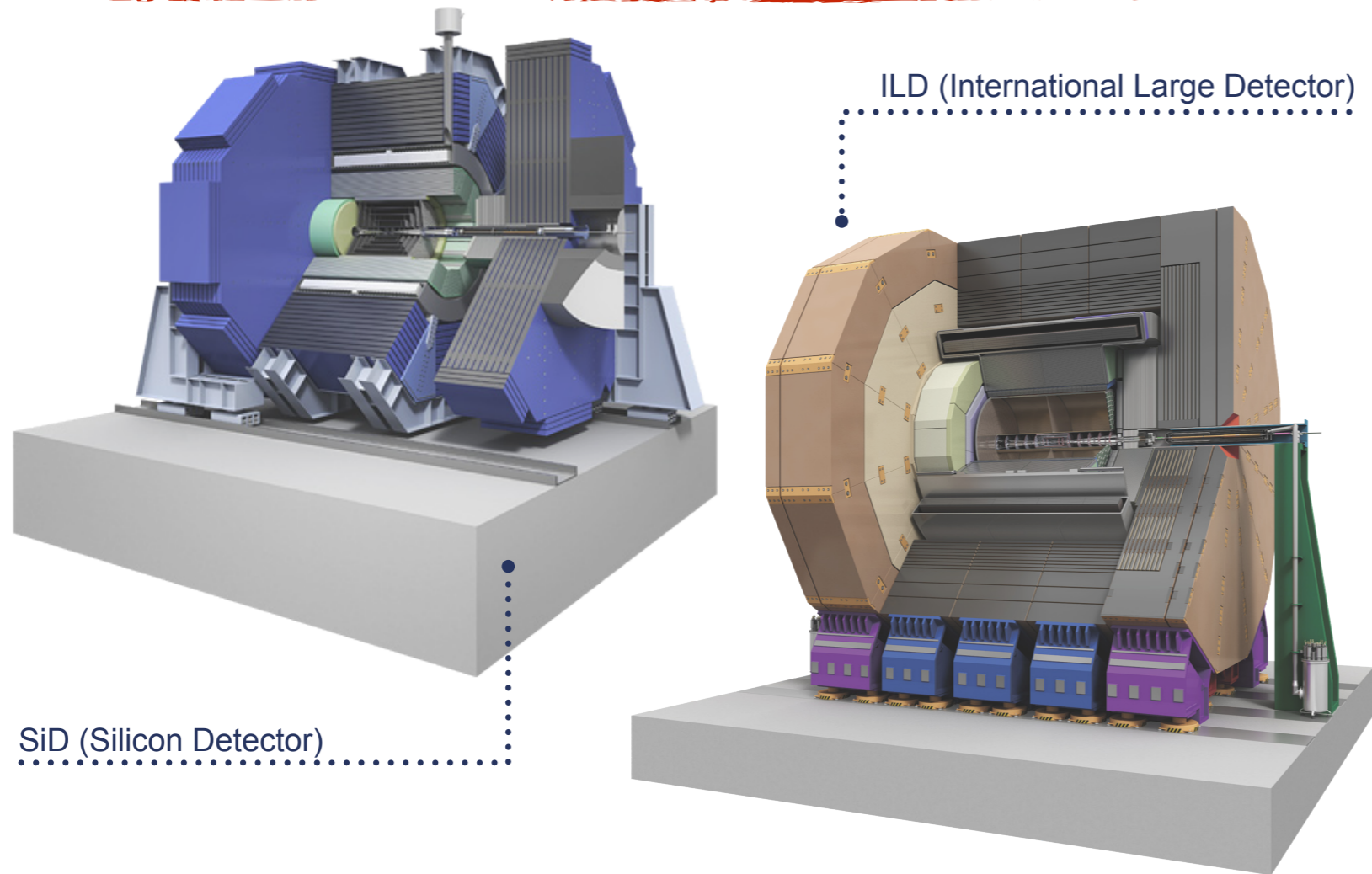


- ILC: Site selected in Japan: Kitakami, north of Sendai
 - 30 km for 500 GeV, 50 km for 1 TeV
- Now: Discussions on political levels...

- CLIC: A possible future high energy frontier project at CERN
 - 50 km for 3 TeV
- R&D for accelerator & detectors



Detector Systems at Linear Colliders



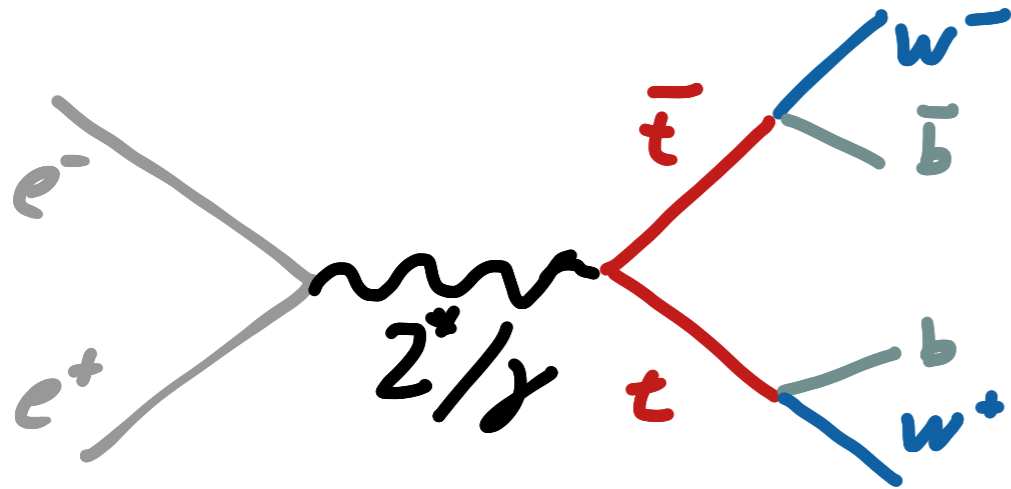
- Low-mass, high precision vertexing & tracking
- Highly granular calorimeters
- Particle flow event reconstruction

- CLIC detectors based on ILC concepts, with modifications in the calorimeters, vertex and forward regions to account for higher energy and higher backgrounds
- Detailed simulation models implemented in GEANT4
- Realistic event reconstruction including pattern recognition, tracking, PFA
- ▶ Full simulation studies used for all results presented here

Top Quark Physics at Linear Colliders

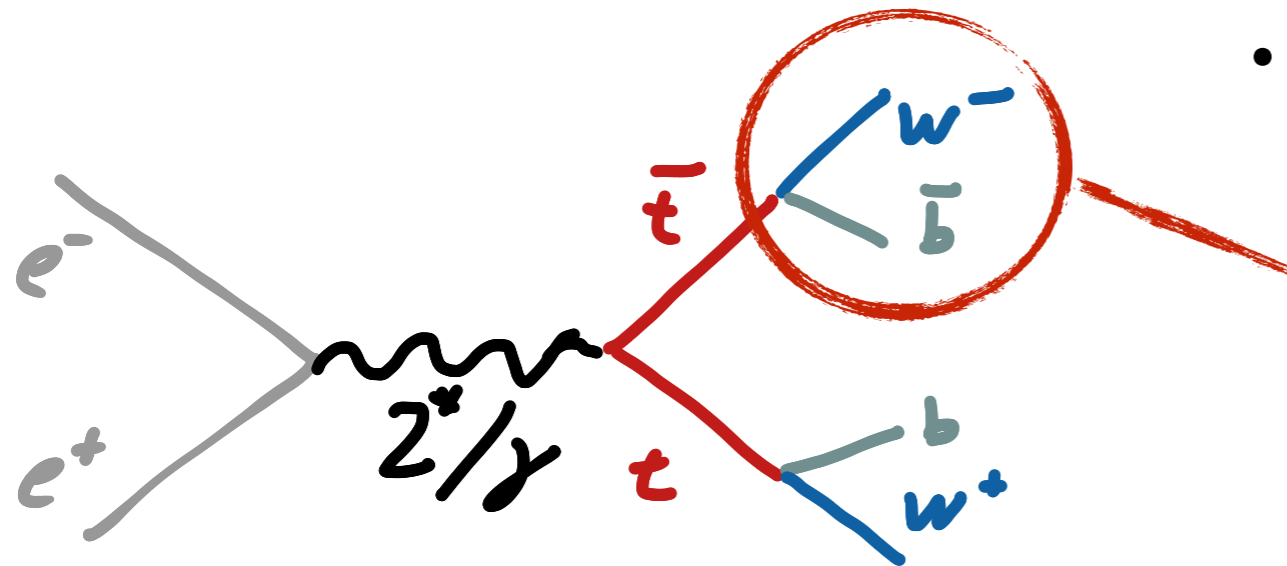
- The dominant production mechanism: Top pair production

- Rich physics opportunities:



Top Quark Physics at Linear Colliders

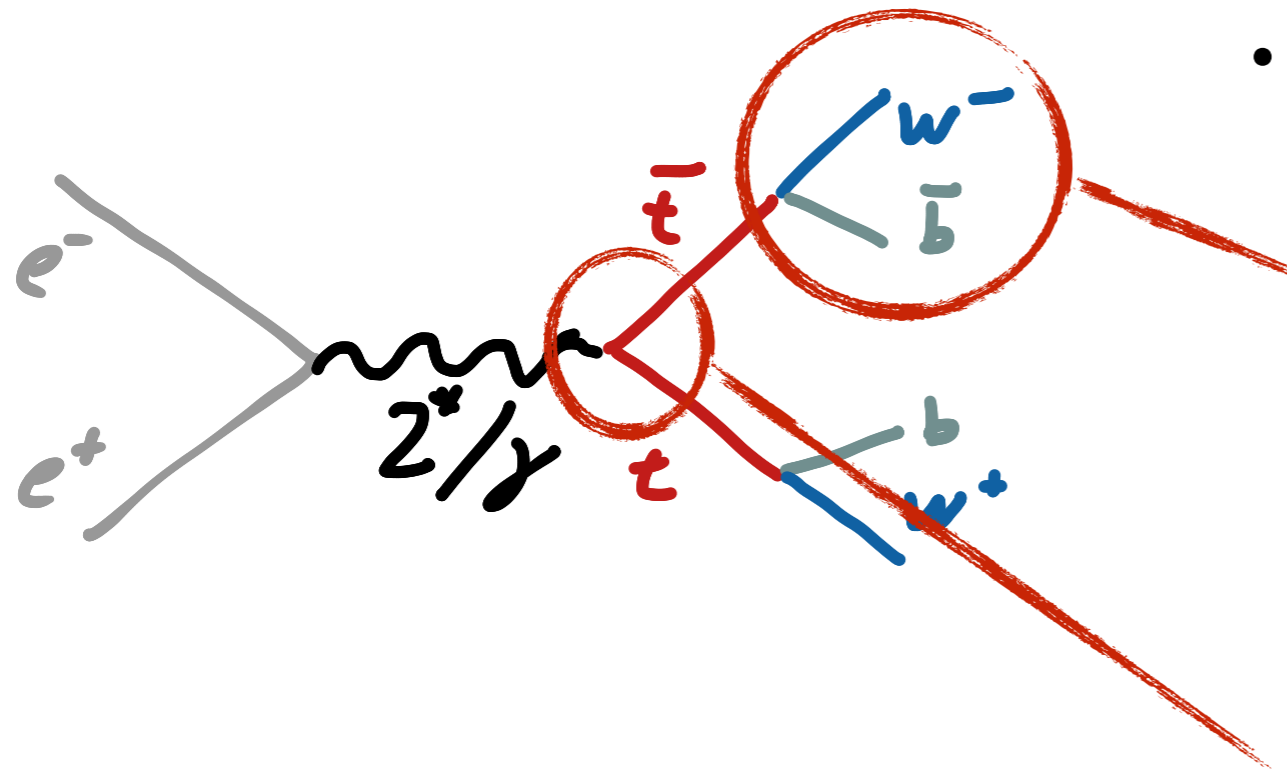
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- Rich physics opportunities:
 - Top properties: **mass**, width, decay modes
 - BSM sensitivity: CP violation, flavor-changing decays,...

Top Quark Physics at Linear Colliders

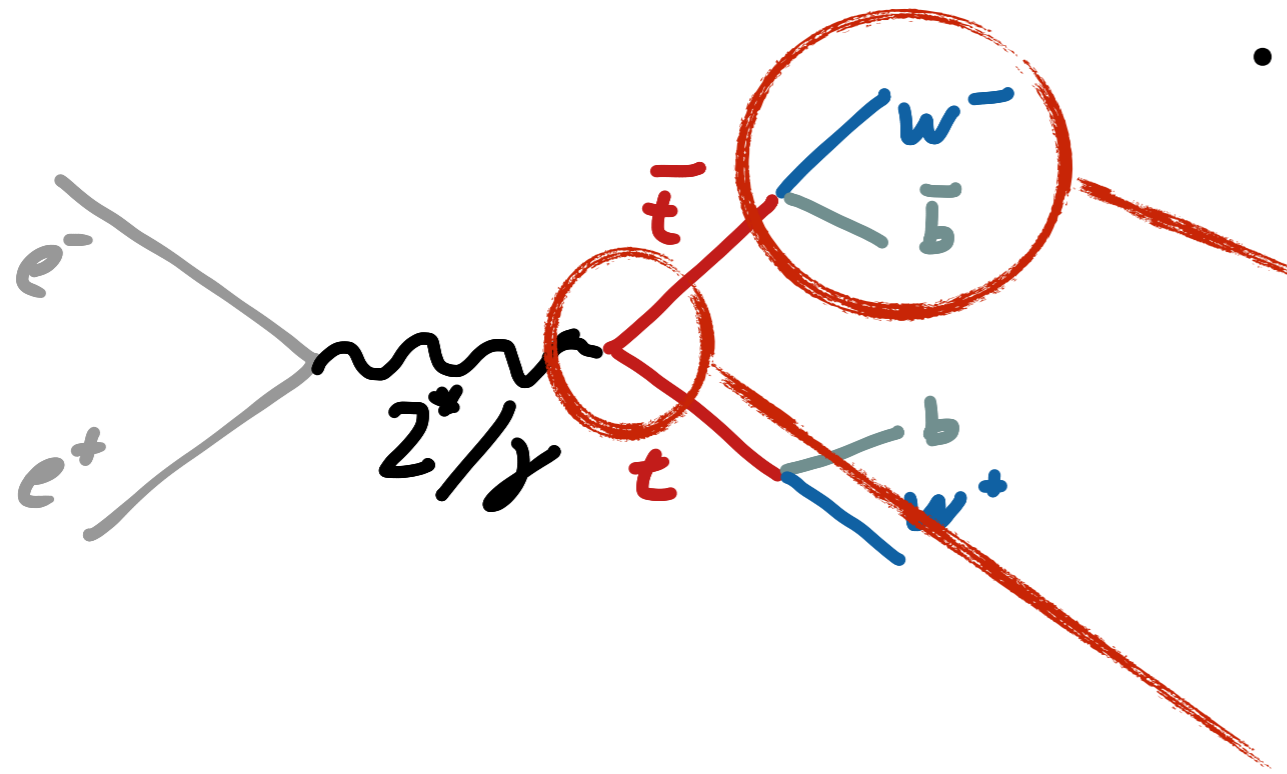
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- Rich physics opportunities:
 - Top properties: **mass**, width, decay modes
 - BSM sensitivity: CP violation, flavor-changing decays,...
 - Top properties: **mass**, width,
 - Yukawa coupling, strong coupling constant
 - **Electroweak couplings** - sensitivity to BSM physics

Top Quark Physics at Linear Colliders

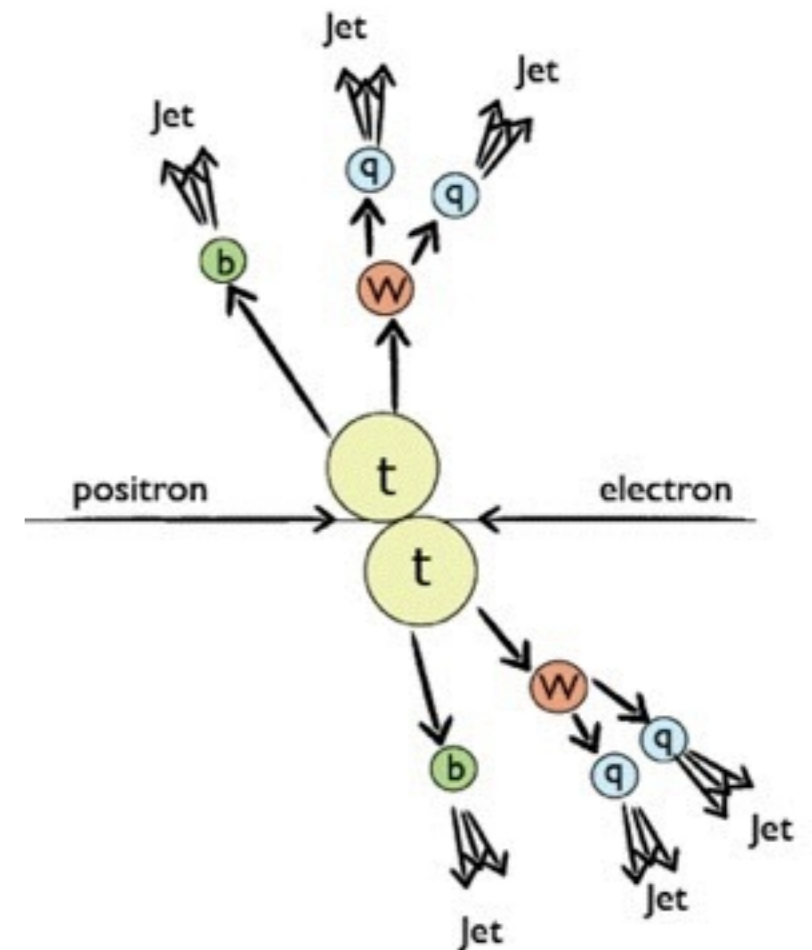
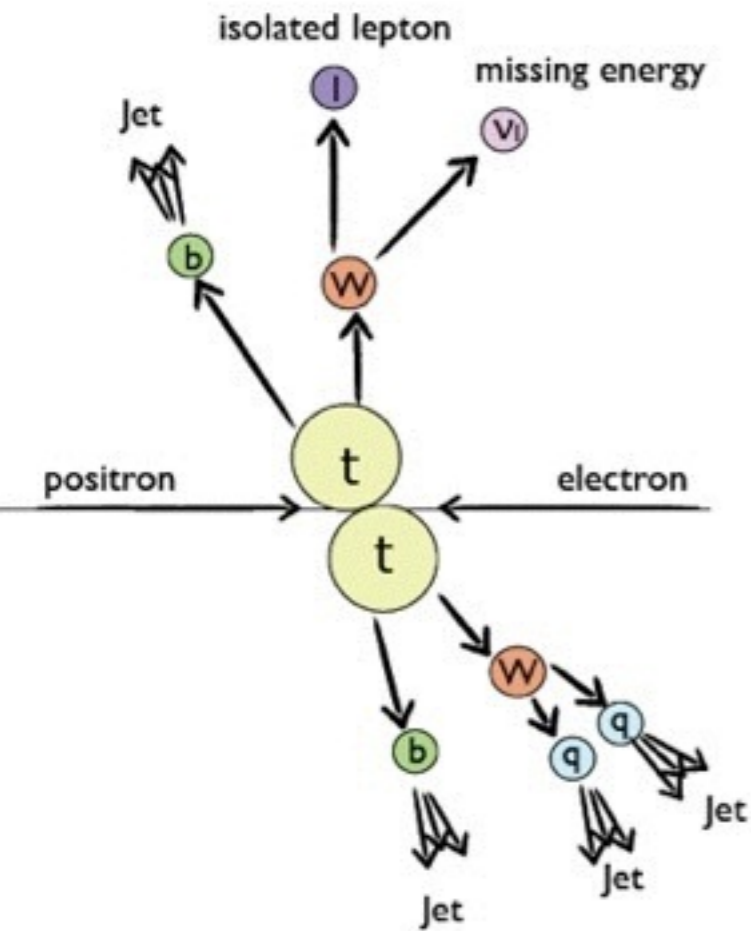
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- Rich physics opportunities:
 - Top properties: **mass**, width, decay modes
 - BSM sensitivity: CP violation, flavor-changing decays,...
 - Top properties: **mass**, width,
 - Yukawa coupling, strong coupling constant
 - **Electroweak couplings** - sensitivity to BSM physics
- Measurements enabled by
 - known initial state & clean final state
 - Possibility for polarized beams - crucial for coupling measurements

Identifying & Reconstructing Top Quarks

- Strategy depends on targeted $t\bar{t}$ final state

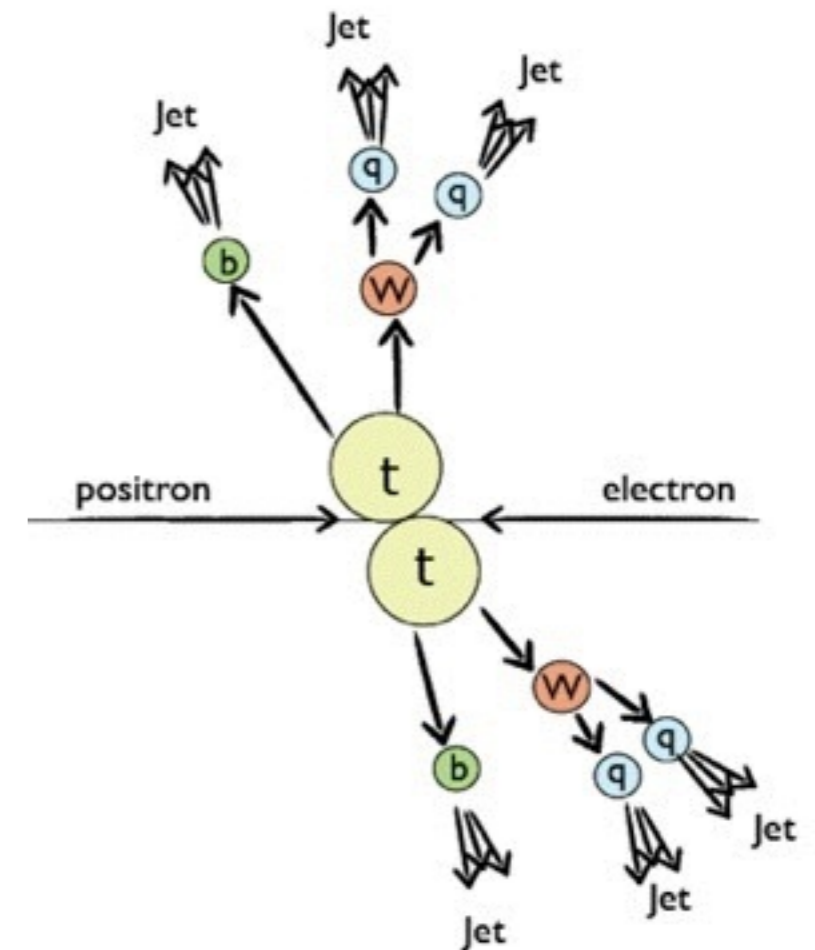
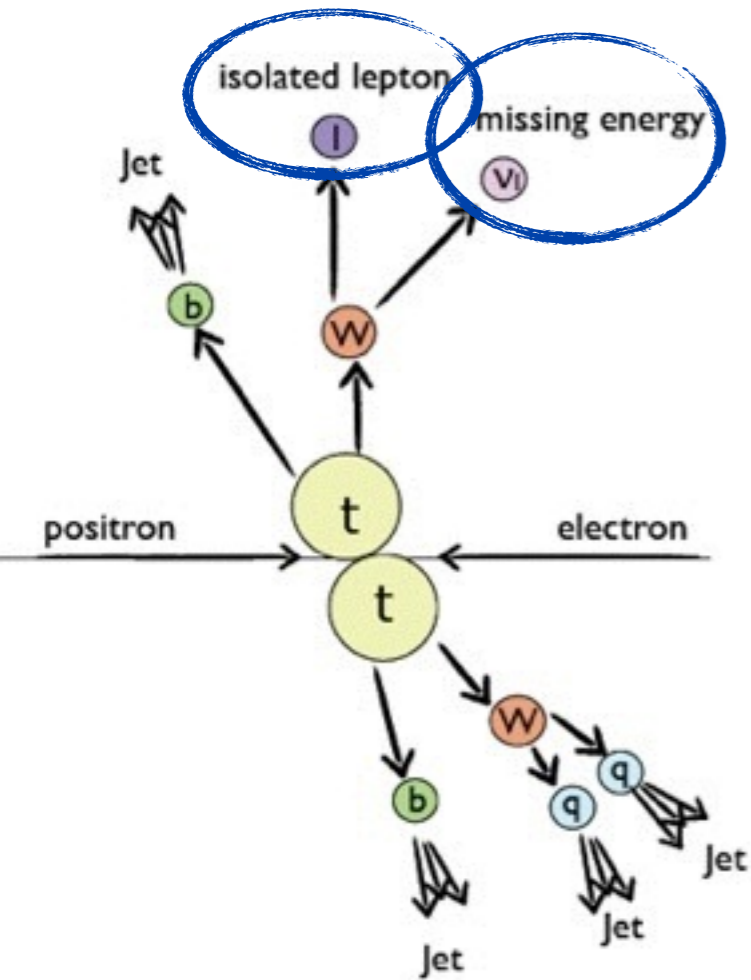


Identifying & Reconstructing Top Quarks

- Strategy depends on targeted $t\bar{t}$ final state

Semi-leptonic:

- isolated lepton ID, momentum measurement
- provides t / \bar{t} identification
- missing energy measurement



Identifying & Reconstructing Top Quarks

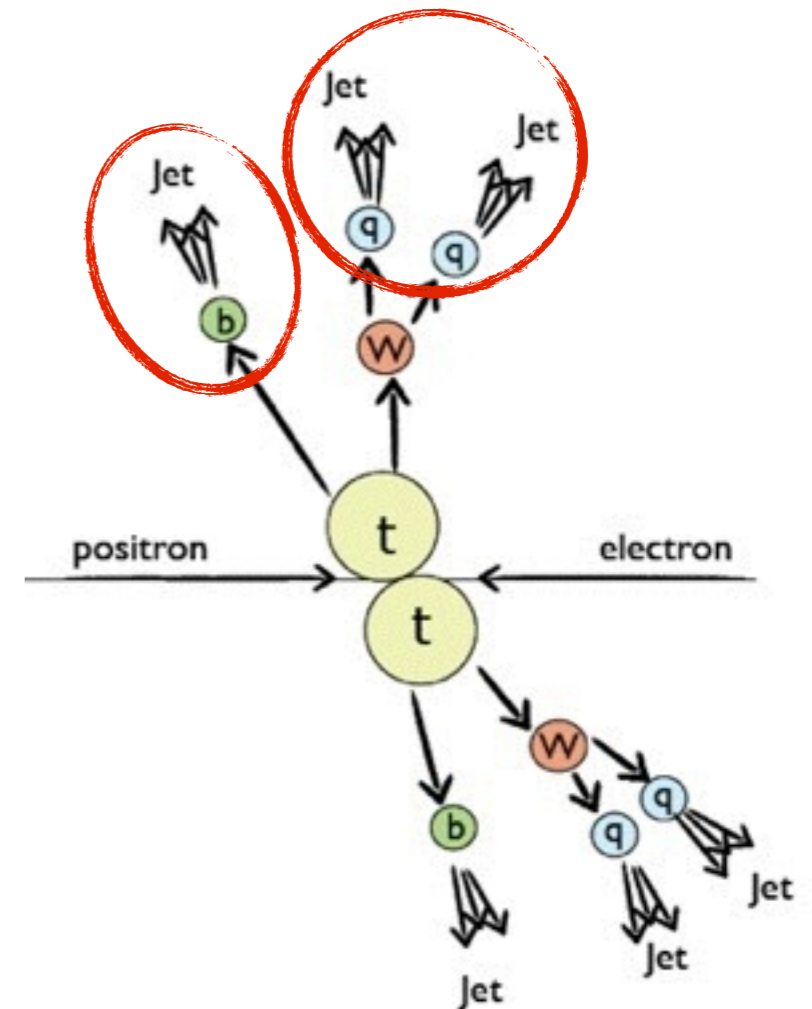
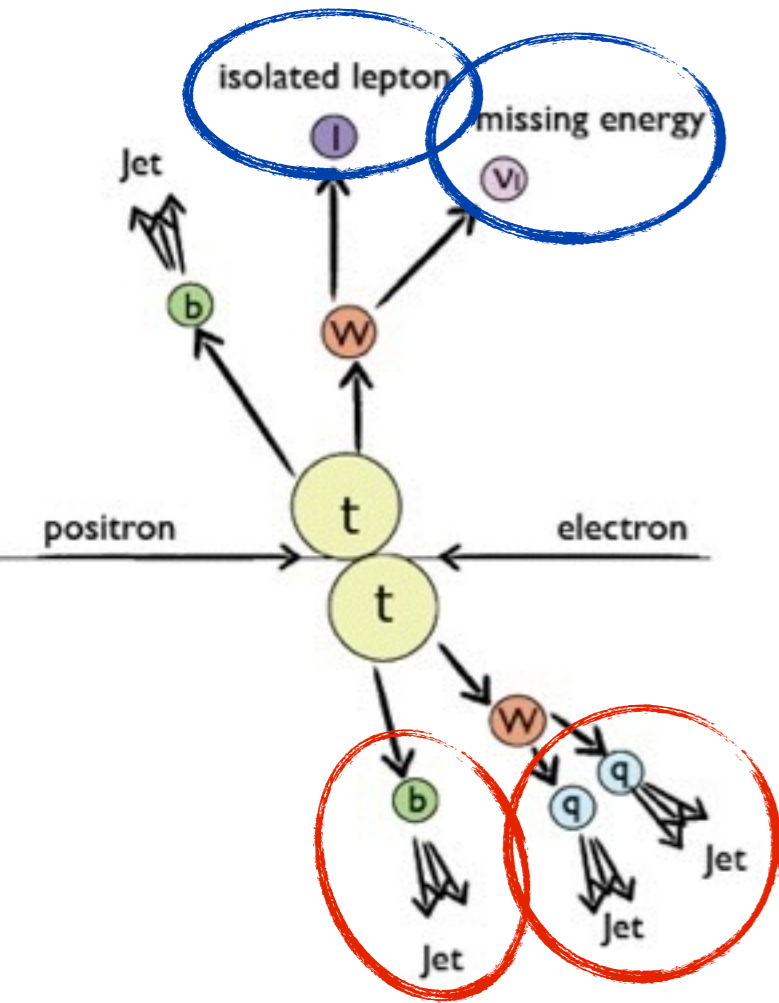
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Universal

- Flavor tagging:
 - b - identification
 - b/c separation
 - b-Jet energy measurement
 - light Jet reconstruction & energy measurement



Identifying & Reconstructing Top Quarks

- Strategy depends on targeted $t\bar{t}$ final state

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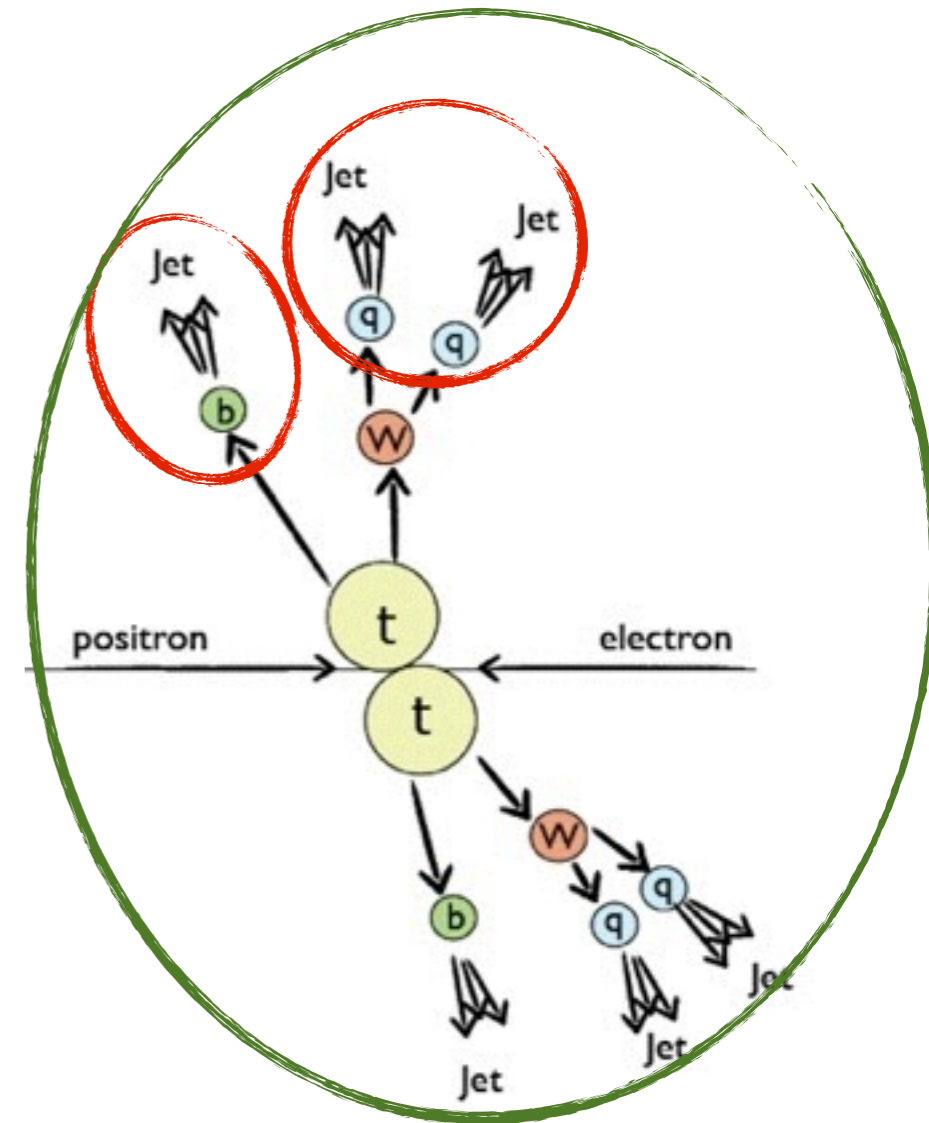
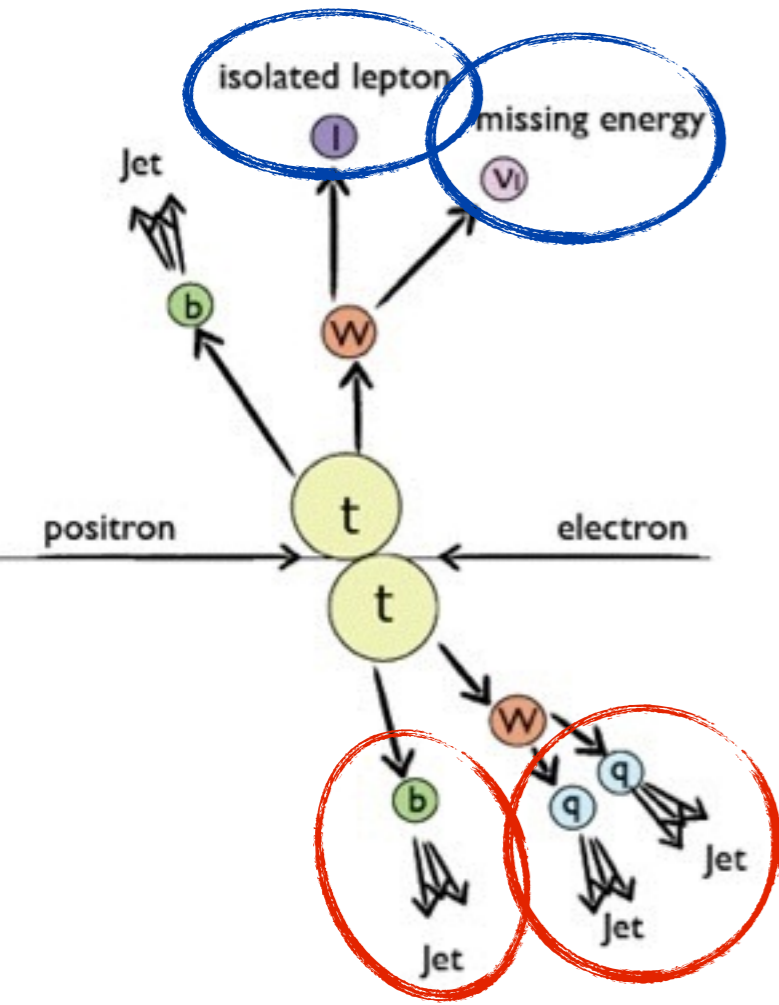
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Universal

- Flavor tagging:
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 - b/c separation
 - b -Jet energy measurement
 - light Jet reconstruction & energy measurement

All-hadronic

- global hadronic energy reconstruction



Top Mass at e^+e^- Colliders

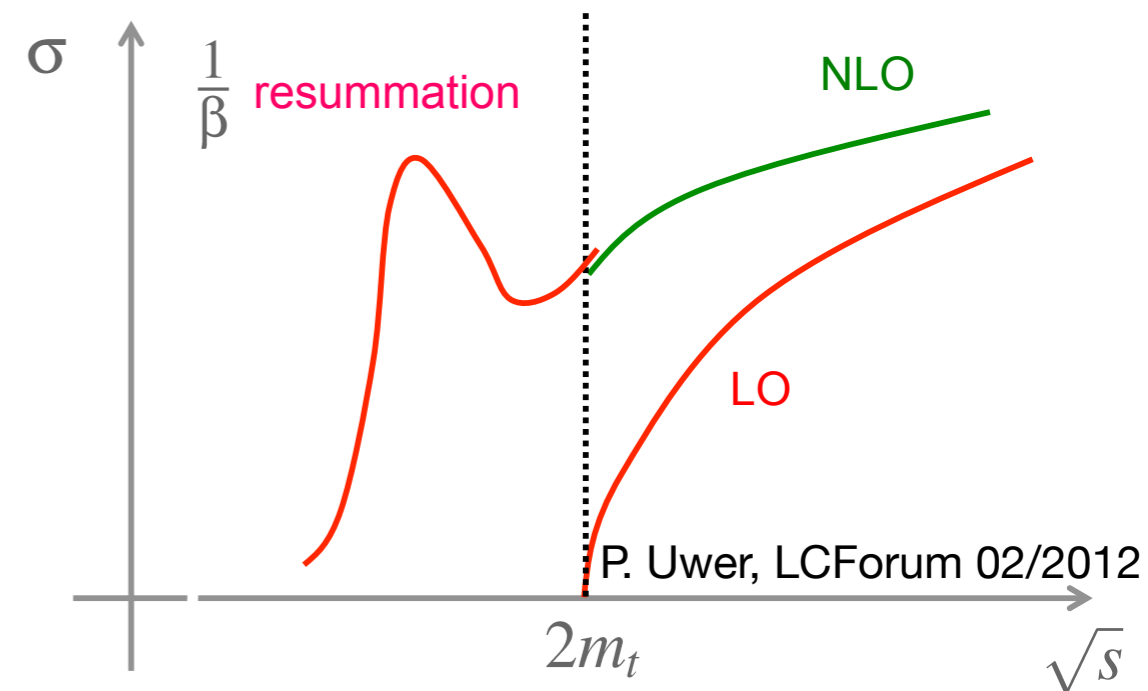
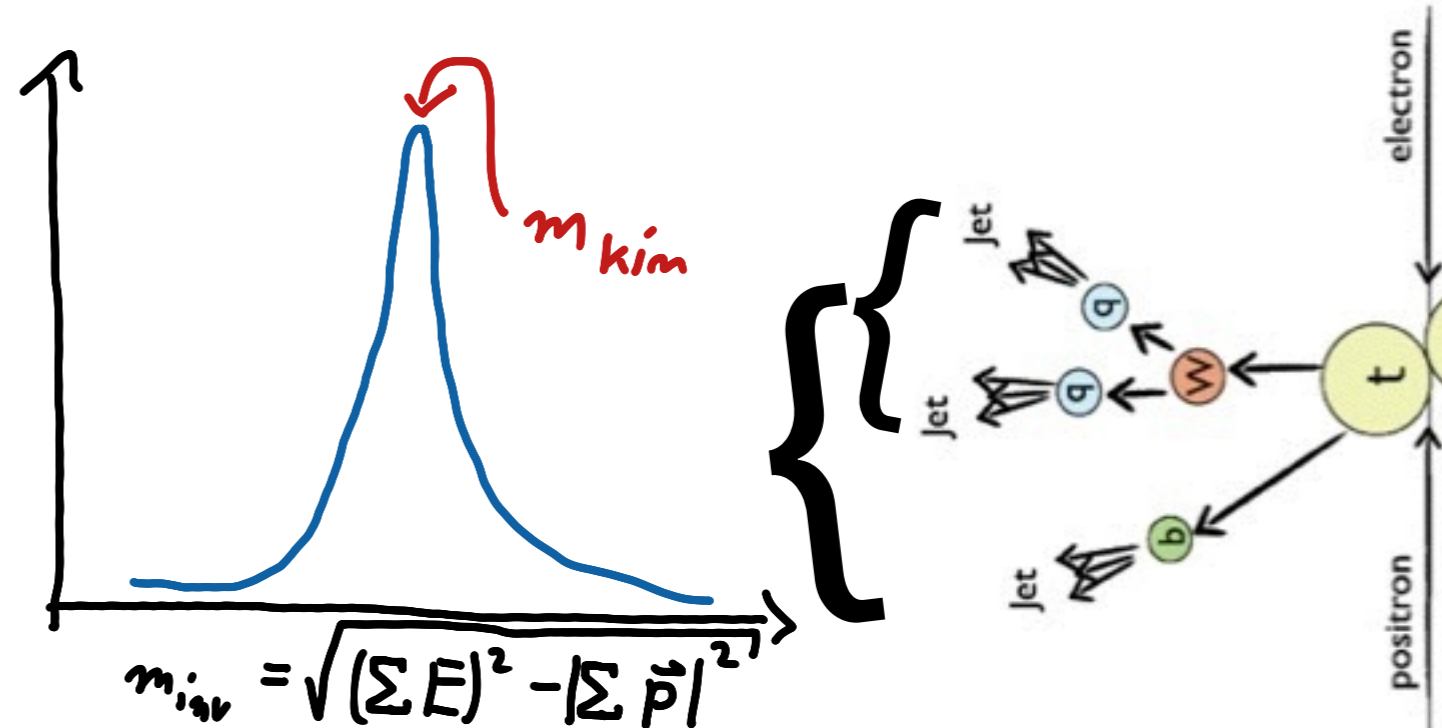
- Measurement in top pair production, two possibilities, each with advantages and disadvantages:

- Invariant mass

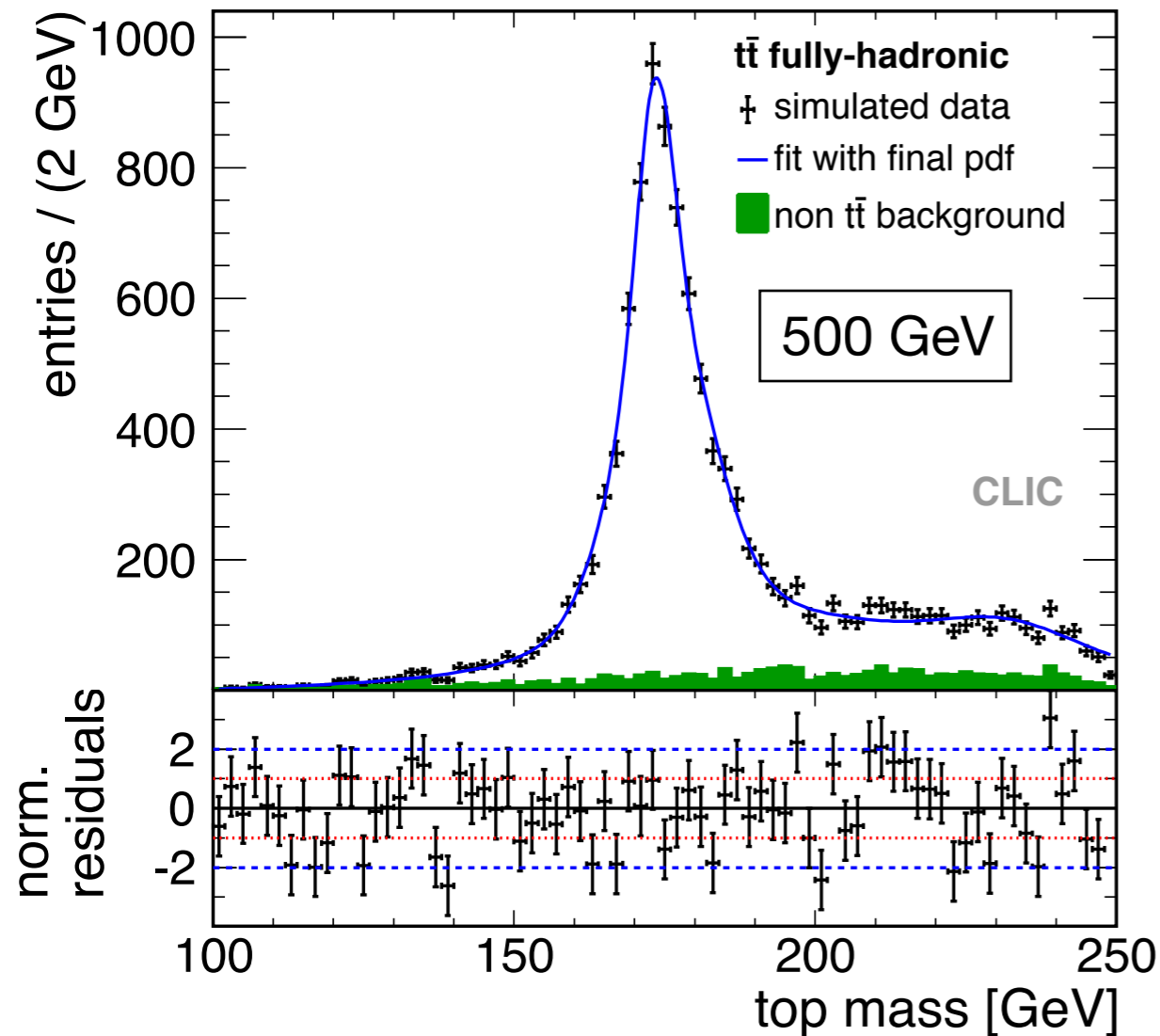
- experimentally well defined (but not theoretically: “PYTHIA mass”)
- can be performed at arbitrary energy above threshold: high integrated luminosity

- Threshold scan

- theoretically well understood, can be calculated to higher orders
- needs dedicated running of the accelerator (but is also in a sweet spot for Higgs physics)
- ▶ The “ultimate” mass measurement at a LC!



Reconstruction and kinematic Mass - Performance



- Very low non- $t\bar{t}$ background
 - S/B ~ 8.5 (12) for FH (SL) at 500 GeV
 - S/B ~ 4.5 directly above threshold
- High reconstruction efficiency
 - 34% (44%) for FH (SL) at 500 GeV
 - 92% for selected decay modes at threshold

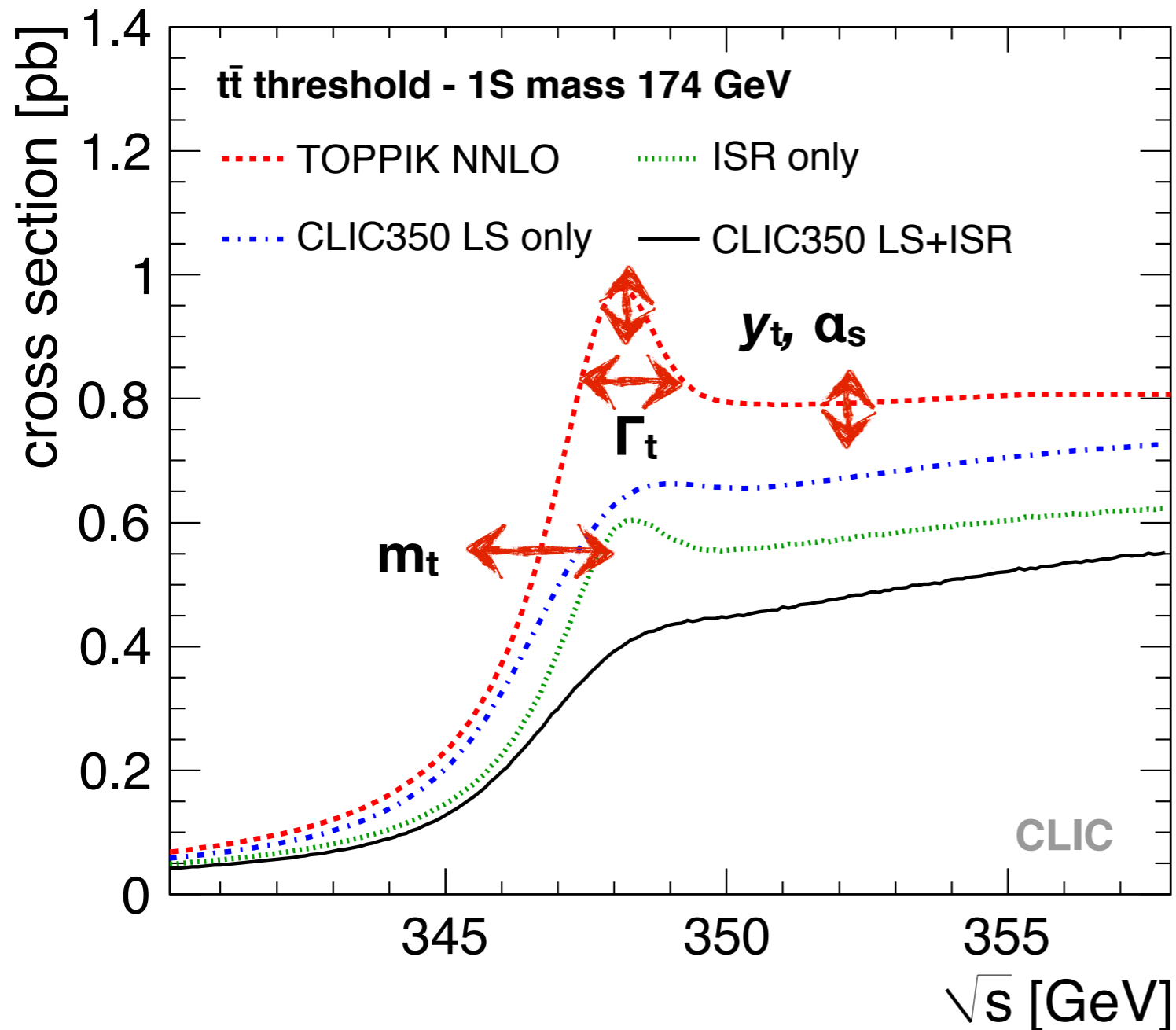
Analysis at threshold optimized for significance, not highest reconstruction quality

Full simulations with a detailed detector model, signal, physics & machine backgrounds

Mass fit - Result:

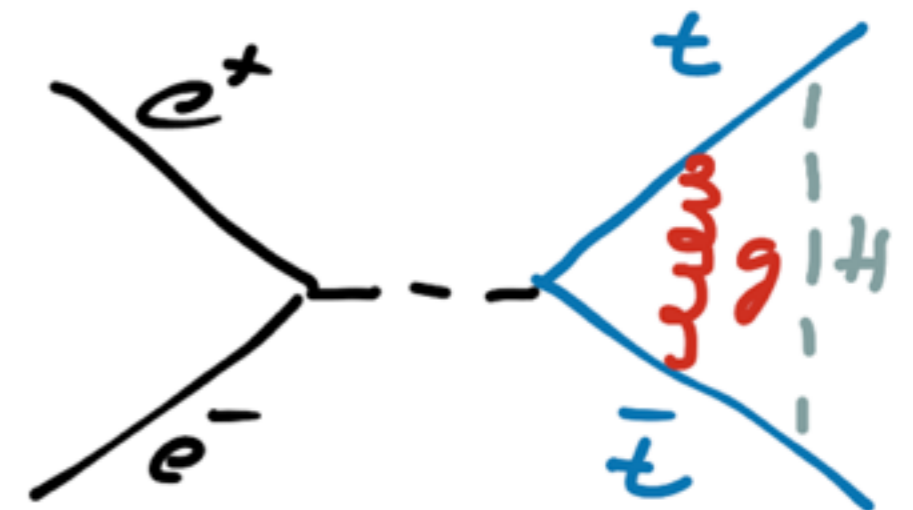
stat. uncertainty on m_t : 80 MeV (FH + SL)
stat. uncertainty on Γ_t : 220 MeV (FH + SL)
exp. systematics of similar order

The Top Threshold - Ultimate Sensitivity



The cross-section around the threshold is affected by several properties of the top quark and by QCD

- Top mass, width, Yukawa coupling
- Strong coupling constant

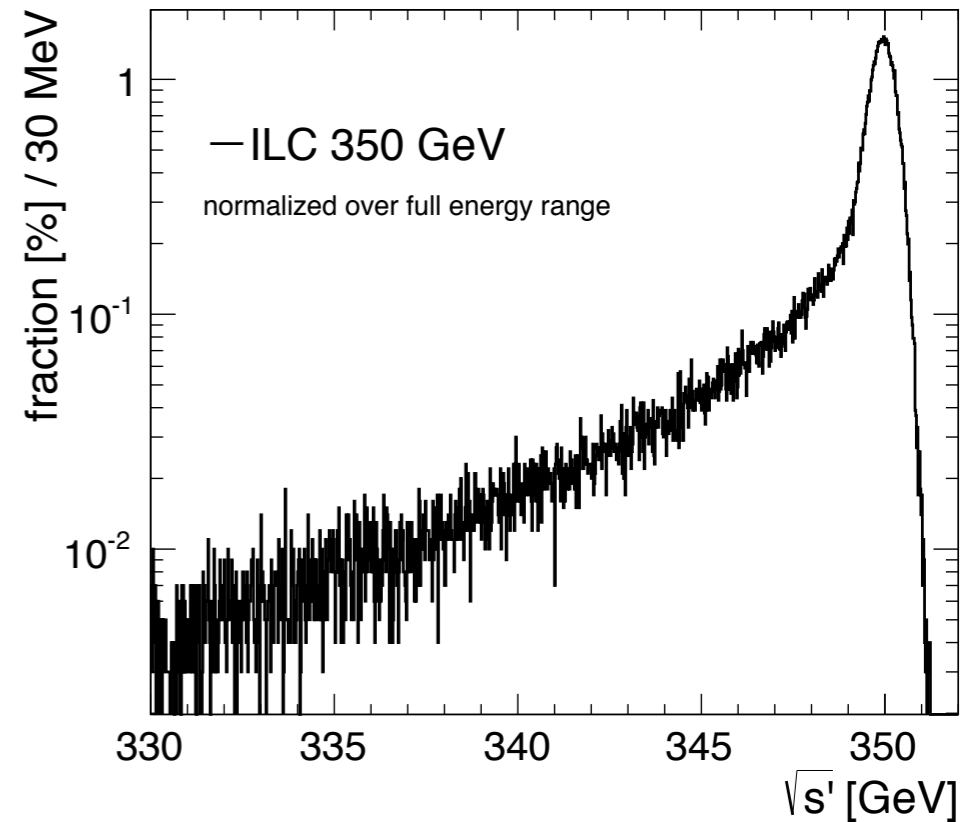
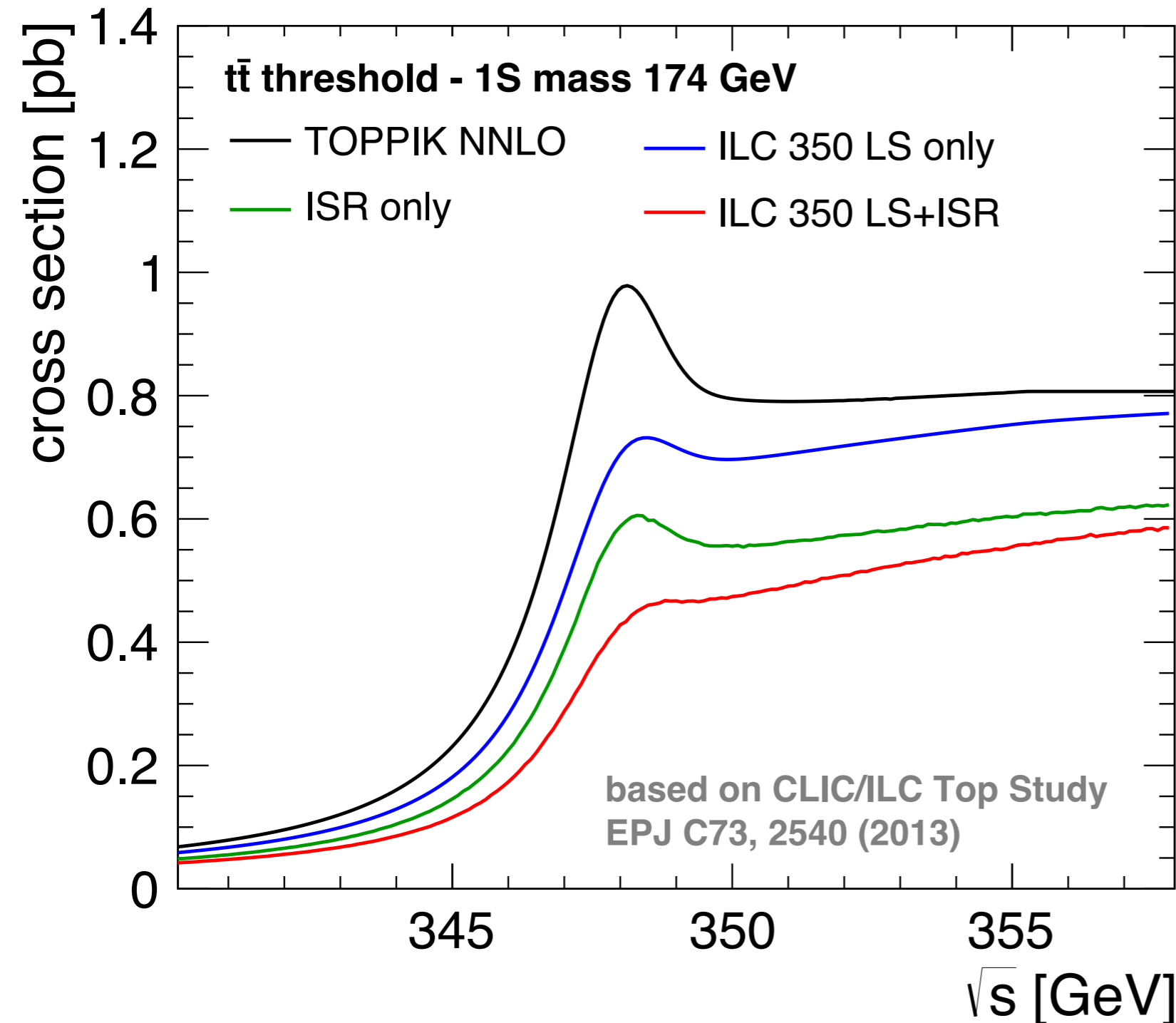


Here: Extract mass and α_s

- Effects of some parameters are correlated; dependence on Yukawa coupling rather weak - precise external α_s helps

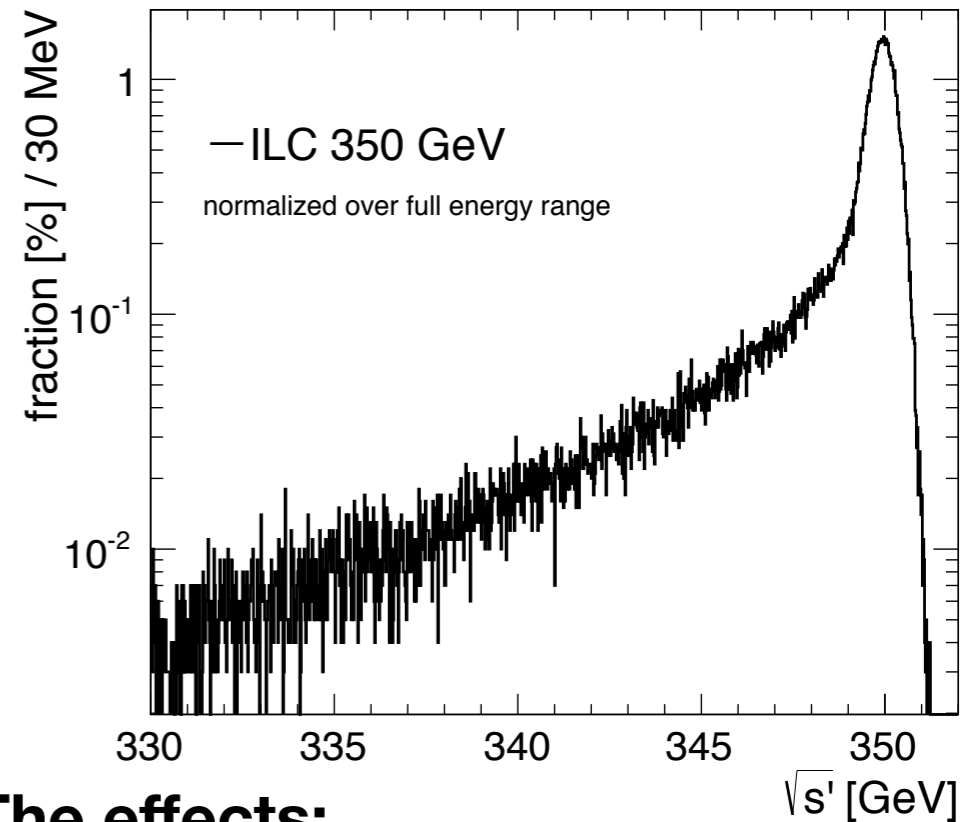
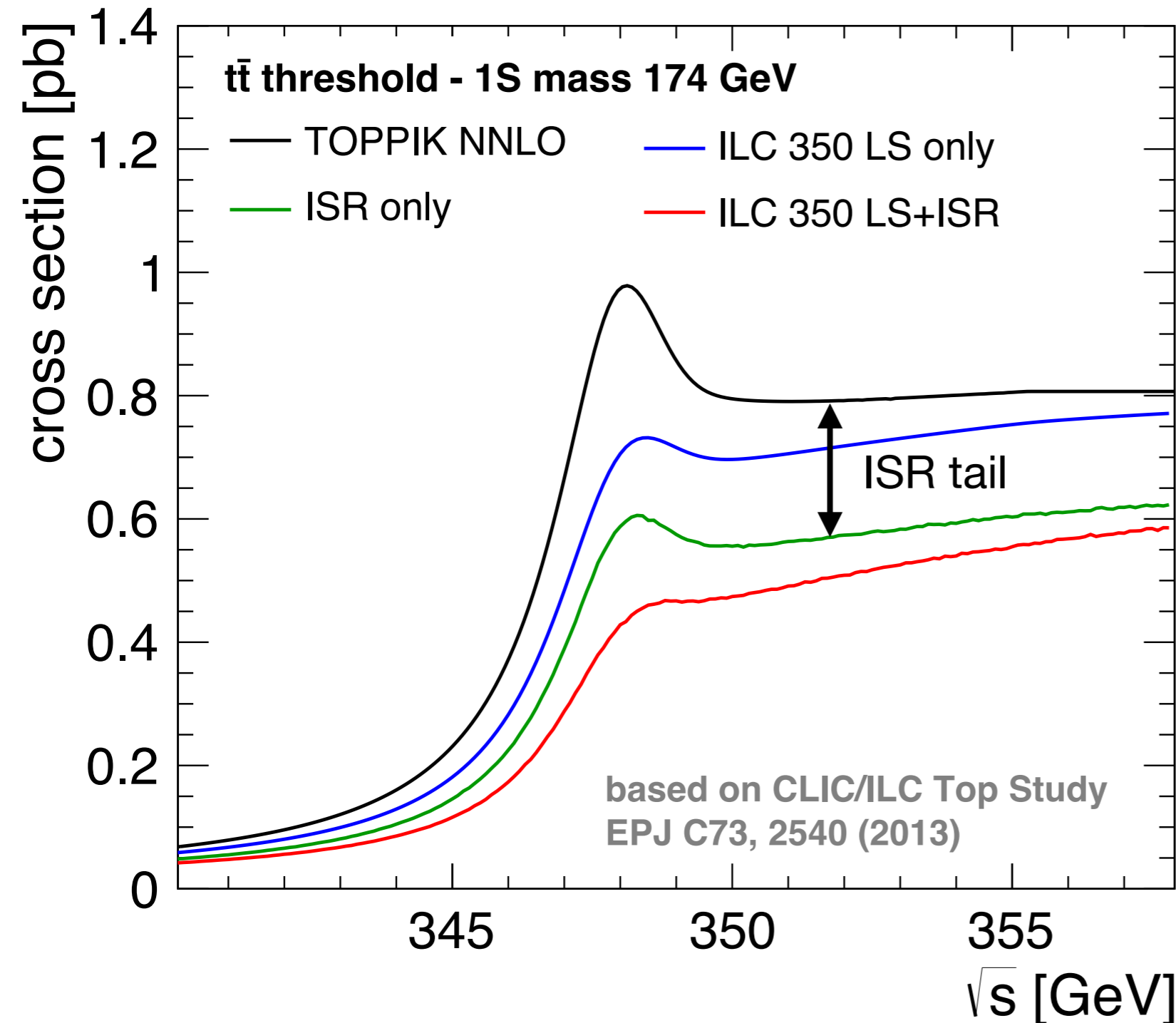
From Theory to Experiment: Collider Effects

- The luminosity spectrum of the collider and ISR affect the shape of the threshold



From Theory to Experiment: Collider Effects

- The luminosity spectrum of the collider and ISR affect the shape of the threshold

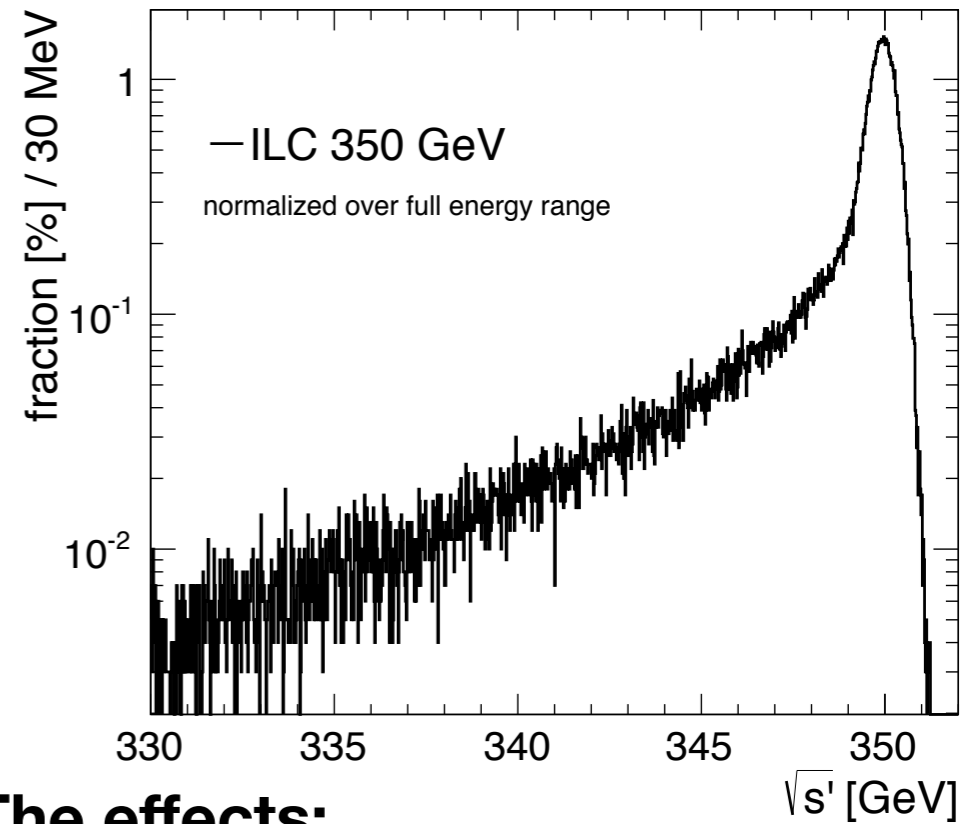
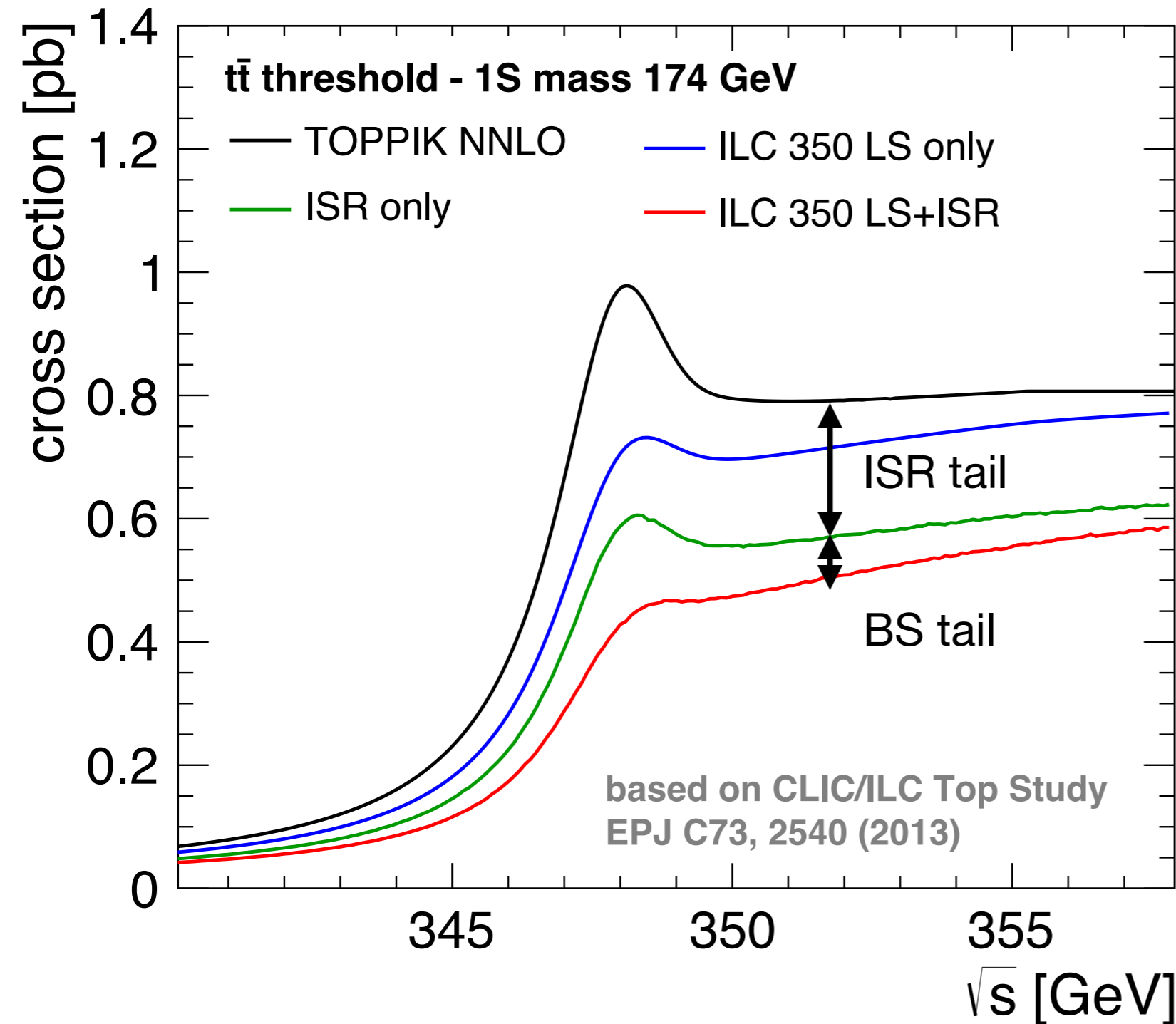


The effects:

- ISR tail: lowering of effective L at top energy

From Theory to Experiment: Collider Effects

- The luminosity spectrum of the collider and ISR affect the shape of the threshold

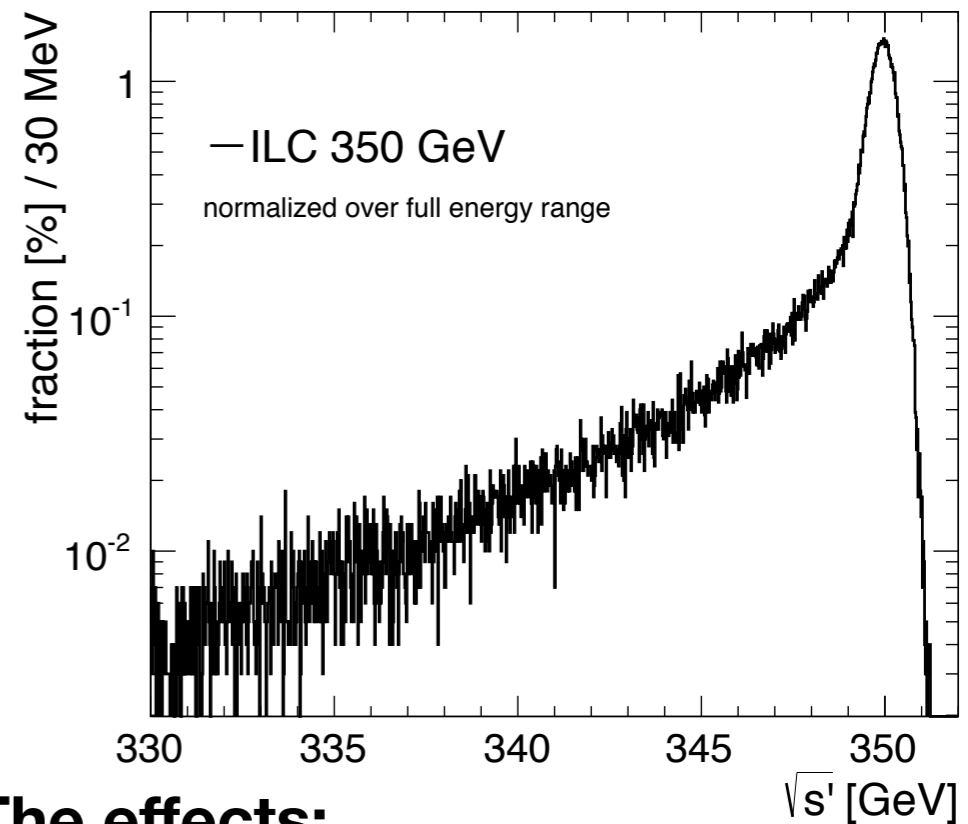
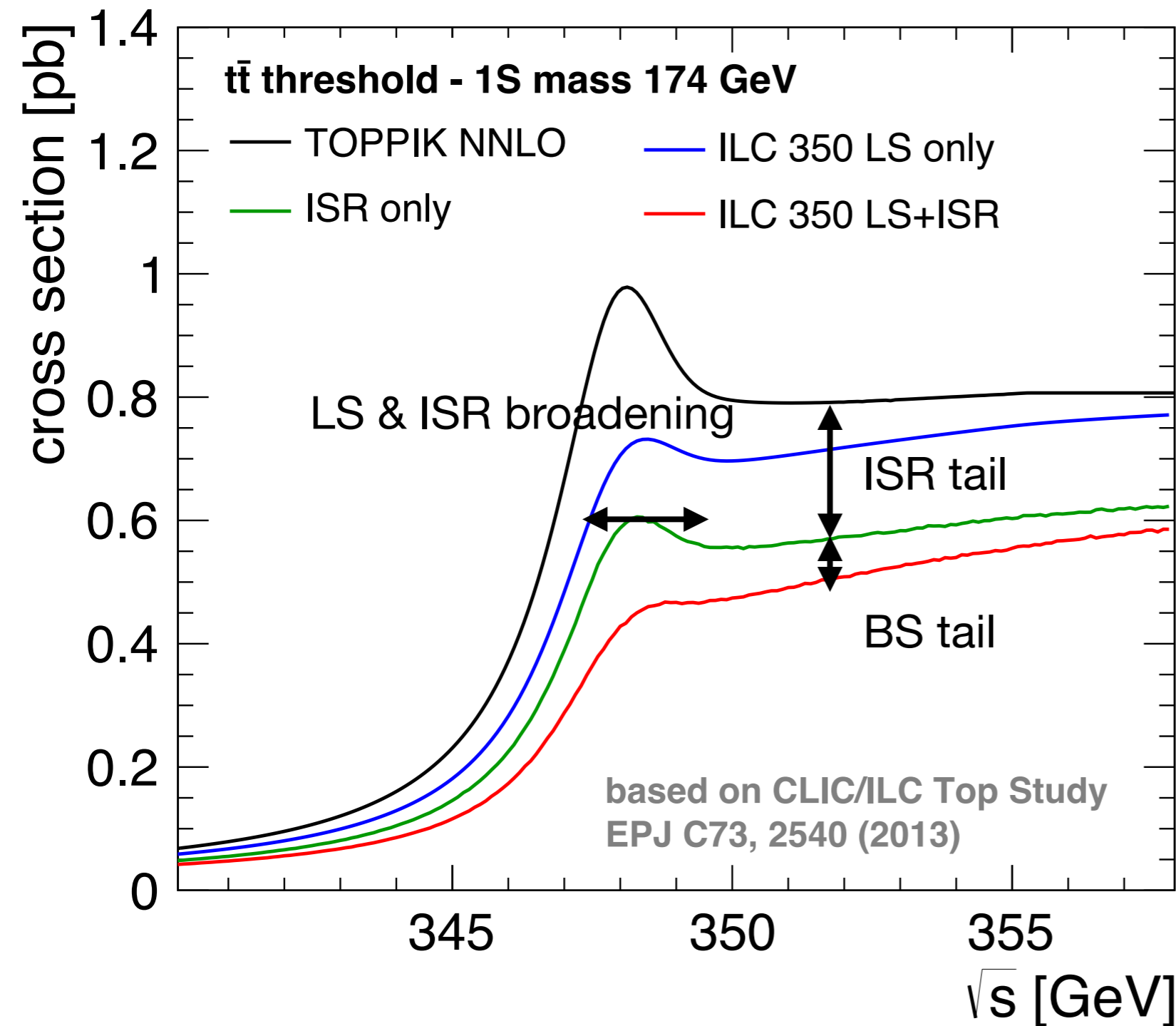


The effects:

- ISR tail: lowering of effective L at top energy
- BS tail: lowering of effective L at top energy

From Theory to Experiment: Collider Effects

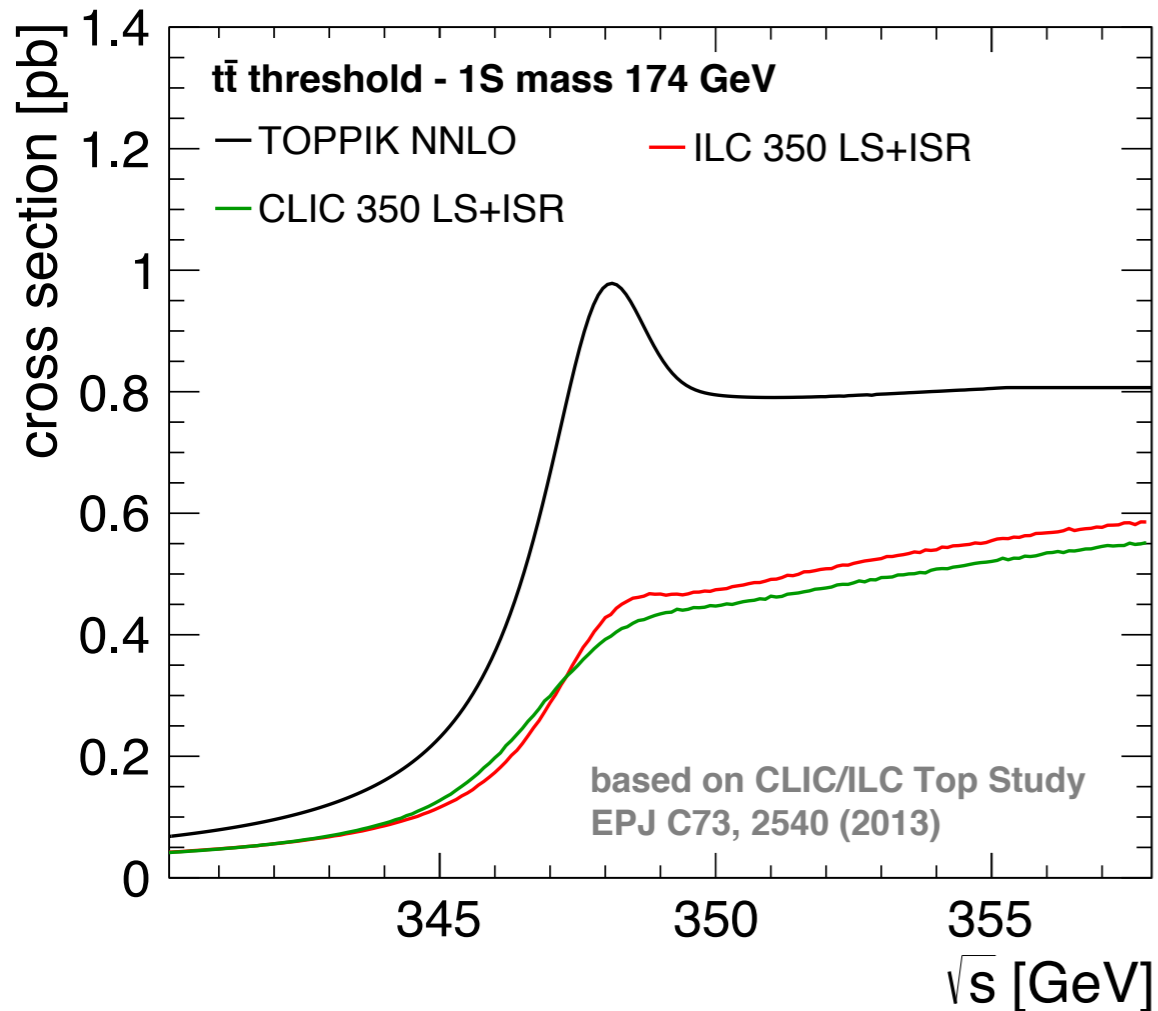
- The luminosity spectrum of the collider and ISR affect the shape of the threshold



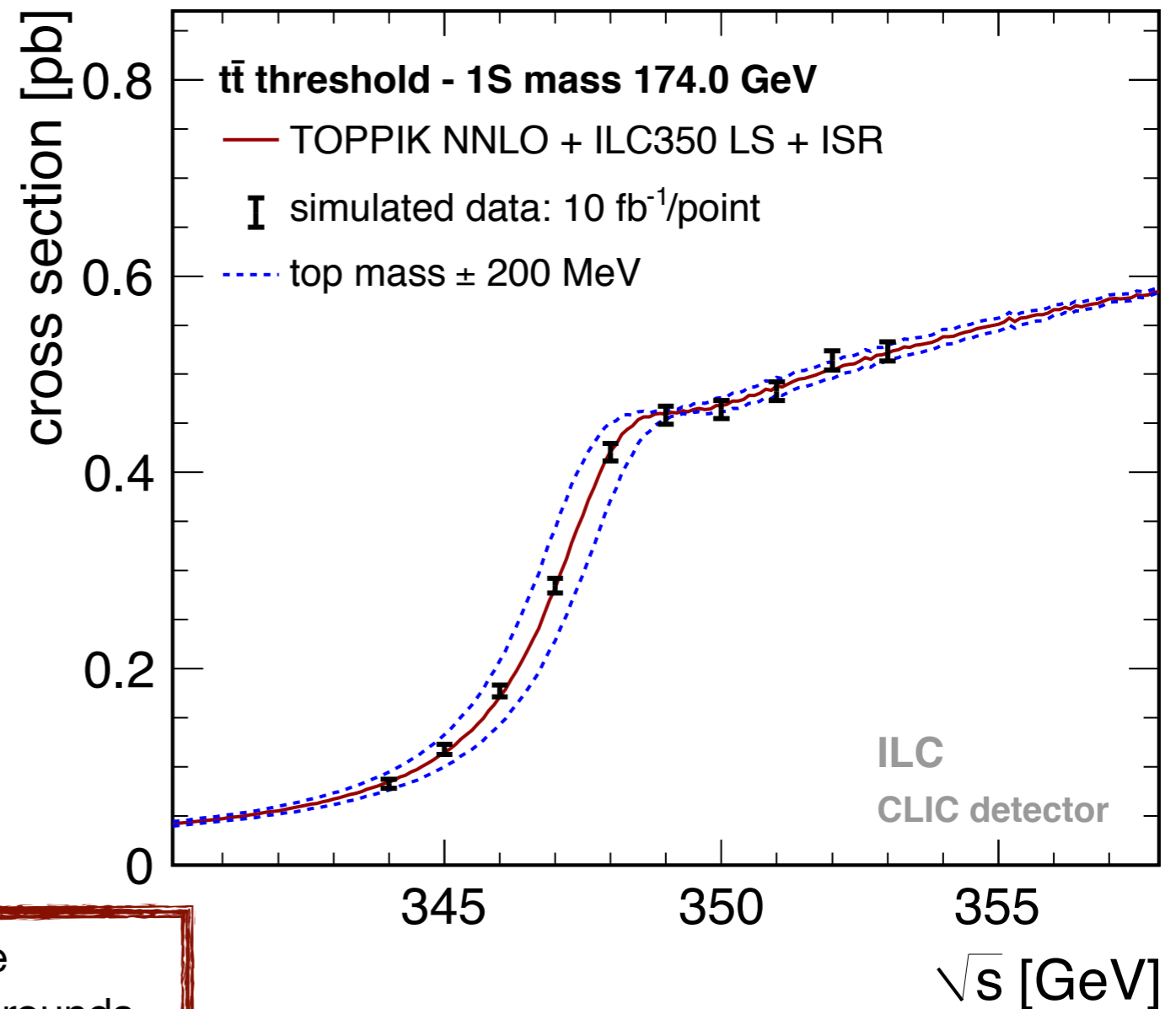
The effects:

- ISR tail: lowering of effective L at top energy
- BS tail: lowering of effective L at top energy
- LS & ISR broadening: smearing of Xsection due to beam energy spread, BS tail and ISR

Threshold Scans at Linear Colliders



- The precise threshold shape depends on the collider
- rather small differences between ILC and CLIC

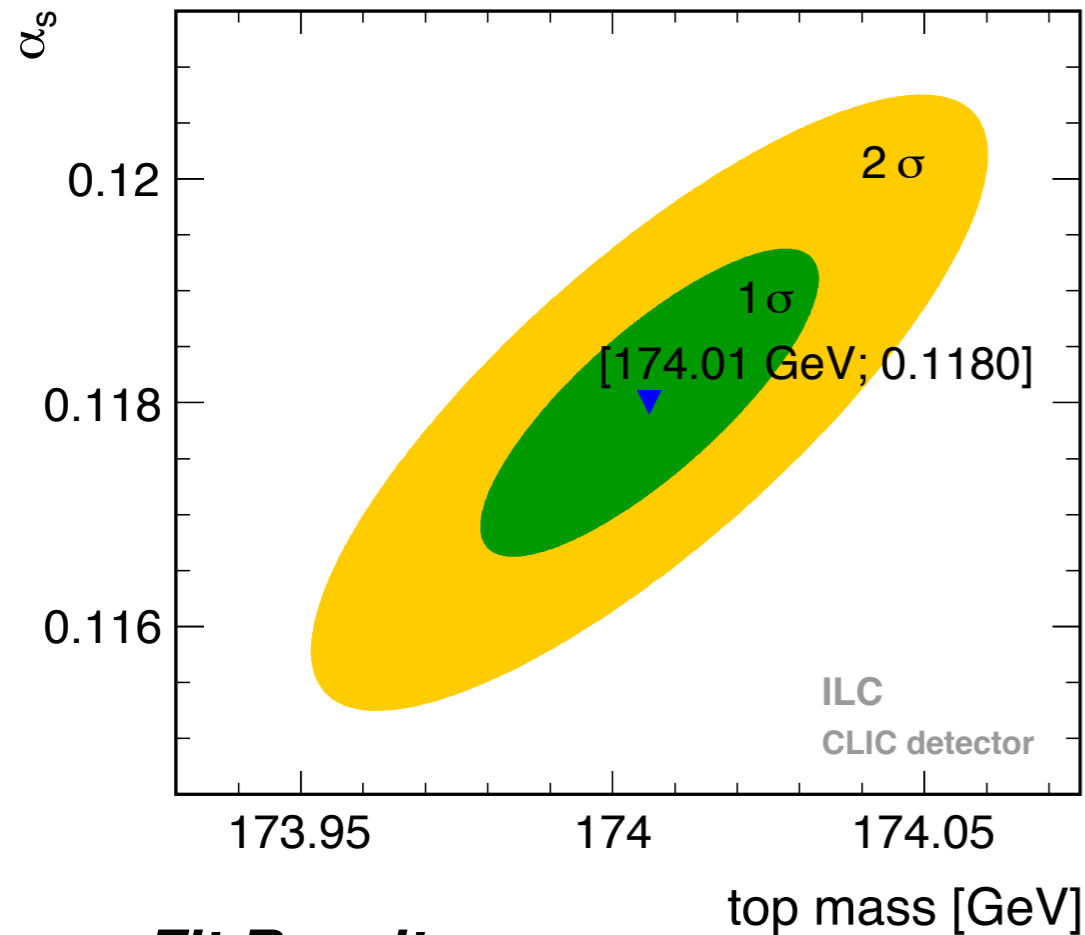


- Assume an integrated luminosity of 100 fb^{-1} , equally spread over 10 points

NB: Assuming unpolarized beams - LC beams can be polarized, increasing cross-sections / reducing backgrounds



Statistical Precision from Threshold Scan



- Additional possibilities:
 - With high precision external α_s the Top Yukawa coupling can be measured with $\sim 7\%$ (stat) precision
 - The top width can also be included in the fit - uncertainties (stat) ~ 30 MeV arXiv:1310.0563

Fit Results

[MeV]	Δm	theory 1%/3%	$\Delta \alpha$	theory 1%/3%
ILC - 2D Fit	27	5/9	0.0008	0.0009/0.0022
CLIC - 2D Fit	34	5/8	0.0009	0.0008/0.0022

[MeV]	Δm	theory 1%/3%	α_s
ILC - 1D Fit	21	18/55	21
CLIC - 1D Fit	22	18/56	20

EPJ C73, 2540 (2013)

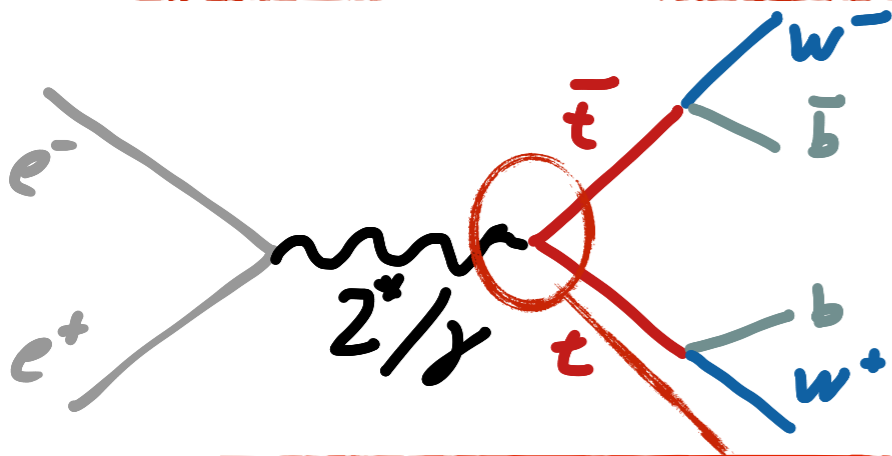
Systematics: First Studies

- Measurements at the top threshold are will likely be systematics limited
 - first studies have been done, still incomplete

Mass:

- *Statistical* uncertainty for 100 fb^{-1} (reasonably modest program)
~ **30 MeV (stat)**
- *Experimental* Systematics
 - Beam Energy: ~ **30 MeV**
 - Non-ttbar background, selection efficiencies: ~ **10 MeV**
 - Luminosity Spectrum (studied for CLIC LS with reconstruction of spectrum via Bhabha scattering): ~ **6 MeV**
- *Theory* Systematics
 - Expected to be significant, naive estimates provide numbers of up to $O(100 \text{ MeV})$ -
Requires a dedicated study - in progress

Electroweak Couplings of the Top Quark



- The production of top pairs provides direct access to electroweak couplings - axial and vector form factors

$$\Gamma_{\mu}^{ttX}(k^2, q, \bar{q}) = ie \left\{ \gamma_{\mu} \left(\tilde{F}_{1V}^X(k^2) + \gamma_5 \tilde{F}_{1A}^X(k^2) \right) + \frac{(q - \bar{q})_{\mu}}{2m_t} \left(\tilde{F}_{2V}^X(k^2) + \gamma_5 \tilde{F}_{2A}^X(k^2) \right) \right\}$$

X: Z, γ

A: axial coupling

V: vector coupling

- In total: 5 non-trivial CP-conserving form factors:

$$\begin{matrix} F_{1V}^{\gamma} & \boxed{F_{1A}^{\gamma}} & F_{2V}^{\gamma} & = 0 \text{ due to} \\ & & & \text{gauge invariance} \\ F_{1V}^Z & F_{1A}^Z & F_{2V}^Z & \end{matrix}$$

- Accessible through measurements of:

- **Total cross-section**

- **Forward-backward Asymmetry A_{FB}**

- **Helicity Angle λ** distribution (related to fraction of left- and right-handed tops)

- For each: Two polarizations $e^-_L - e^+_R$, $e^-_R - e^+_L$

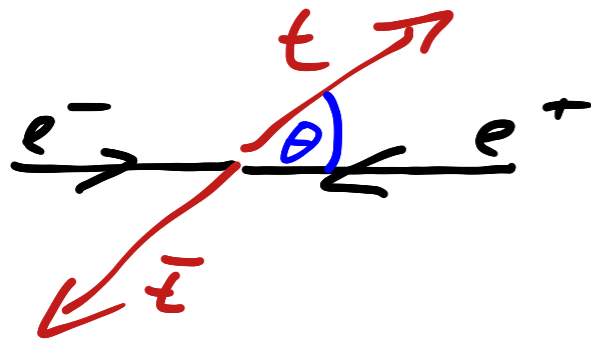
⇒ LC polarised beams crucial!



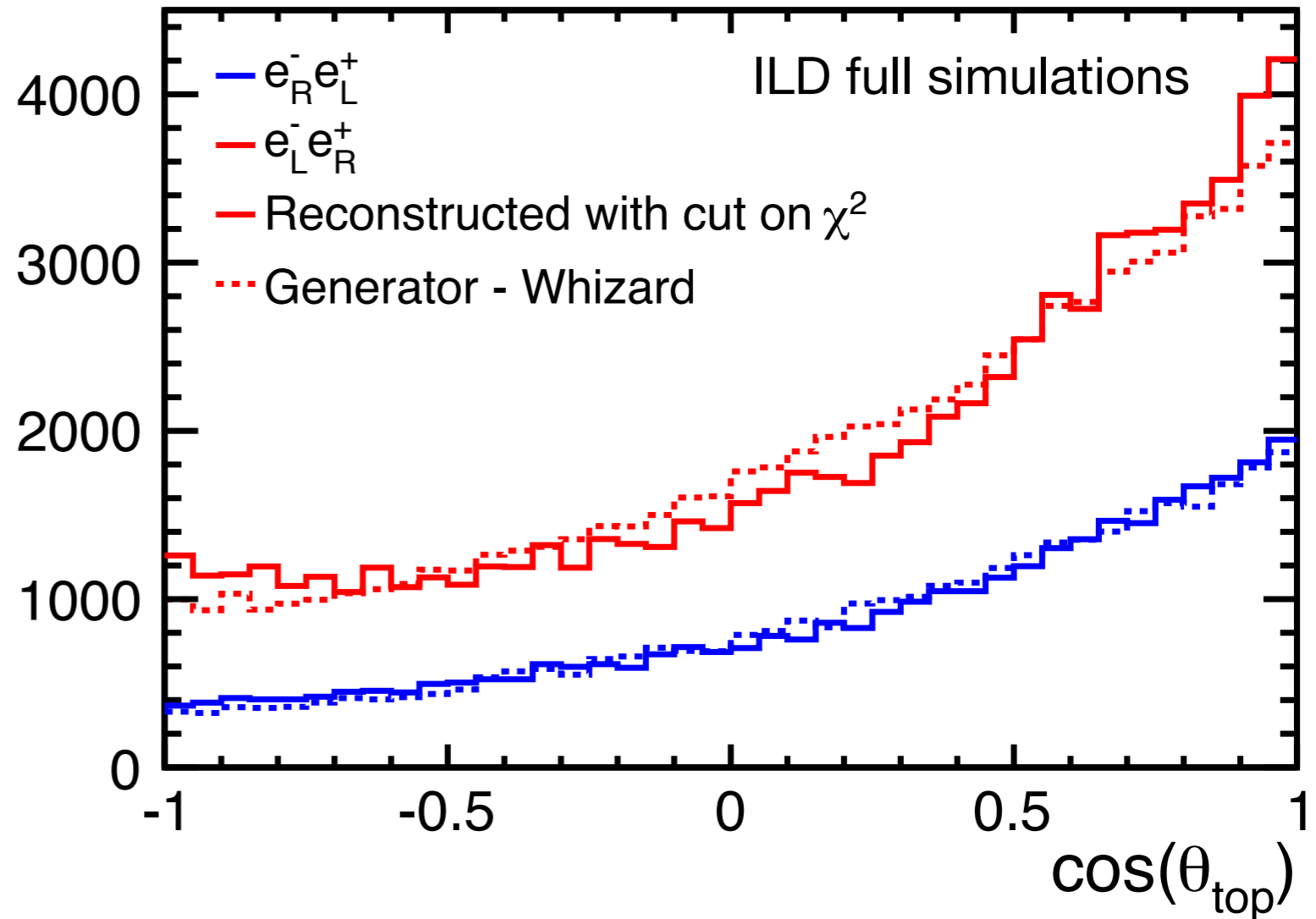
Accessing EW Couplings: Asymmetries & Angles

- Forward-backward asymmetry:

$$A_{FB}^t = \frac{N(\cos\theta > 0) - N(\cos\theta < 0)}{N(\cos\theta > 0) + N(\cos\theta < 0)}$$



- ILC, 500 GeV, 500 fb⁻¹
- Two polarisation configurations:
 - e⁻_Re⁺_L: P(e⁻) -80%, P(e⁺) +30%
 - e⁻_Le⁺_R: P(e⁻) +80%, P(e⁺) -30%

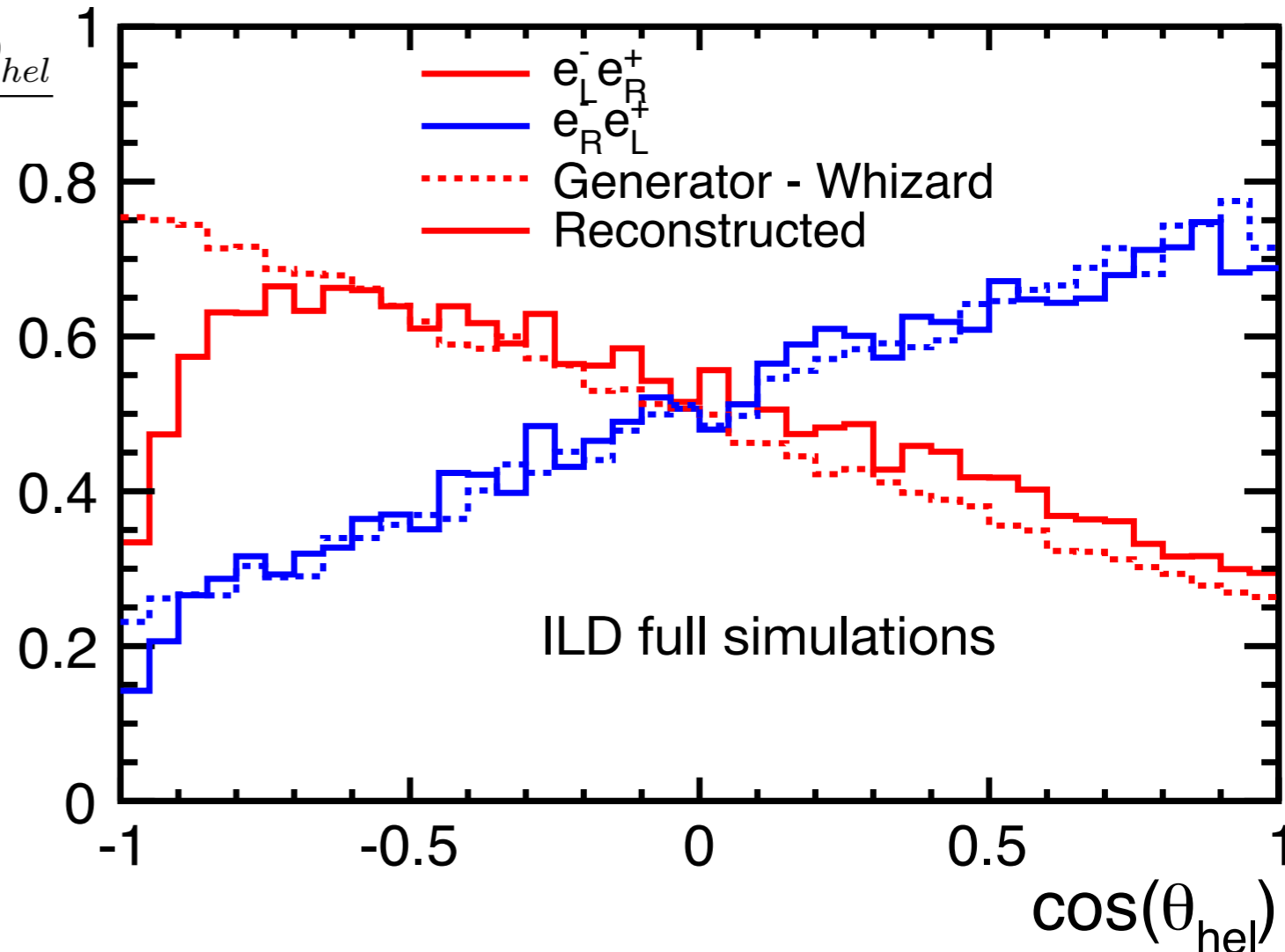
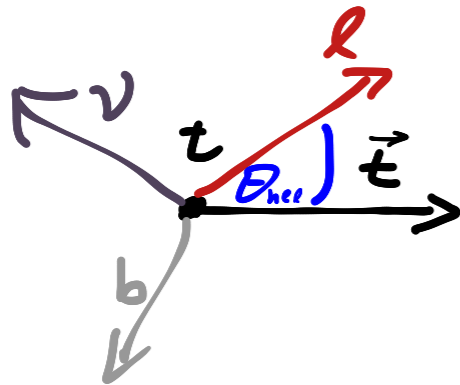


precision on asymmetry:
~2% (stat+ syst)

Accessing EW Couplings: Asymmetries & Angles

- Helicity Angle

$$\frac{1}{\Gamma} \frac{d\Gamma}{d\cos\theta_{hel}} = \frac{1 + \lambda_t \cos\theta_{hel}}{2} = \frac{1}{2} + (2F_R - 1) \frac{\cos\theta_{hel}}{2}$$



- ILC, 500 GeV, 500 fb⁻¹
- Two polarisation configurations:
 - e⁻_Re⁺_L: P(e⁻) -80%, P(e⁺) +30%
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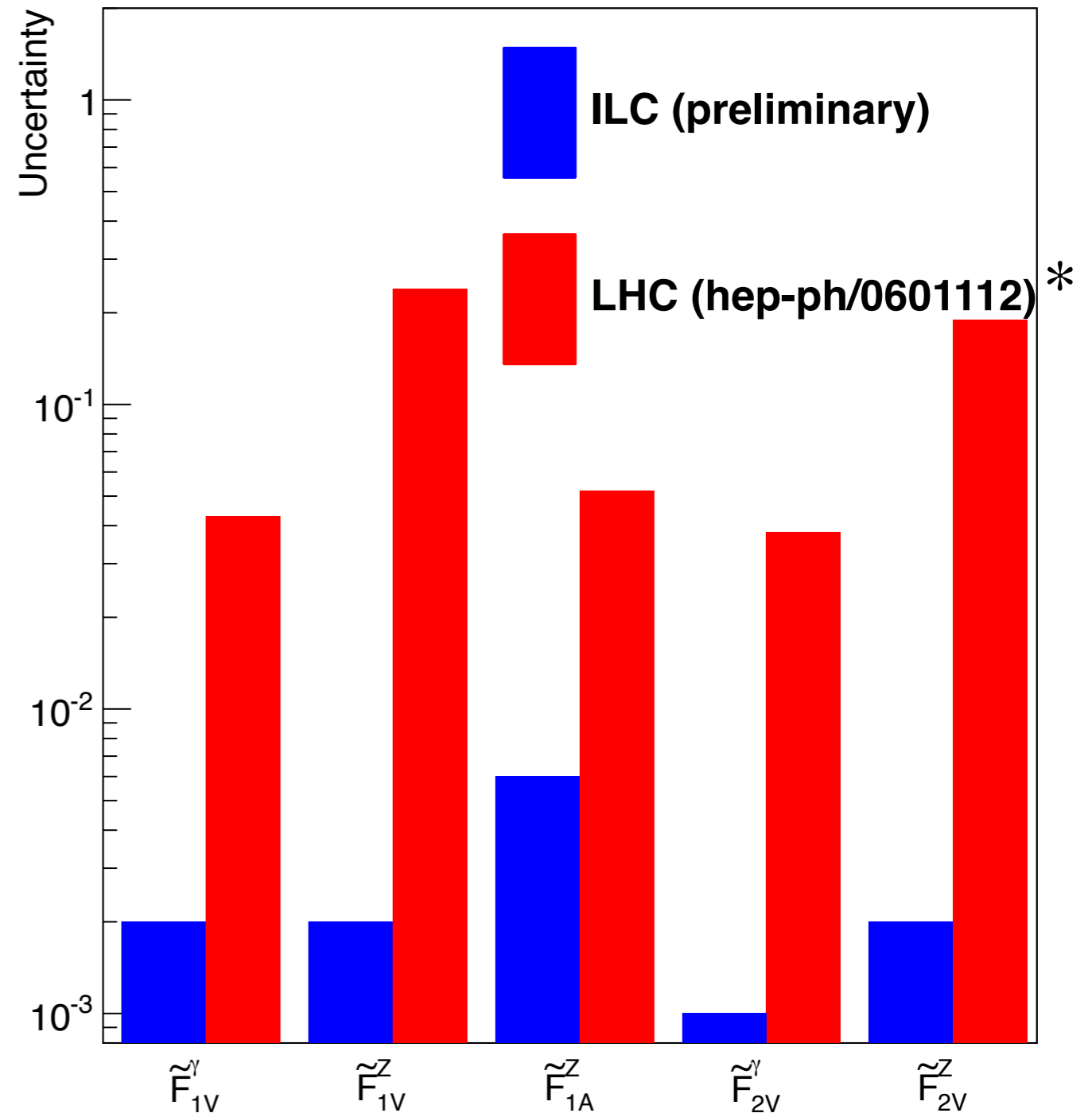
precision on helicity angle:
~4% (stat+ syst)

Electroweak Couplings: Expected Precision

precision on total cross-section:
~0.5% (stat+ lumi)

- The combination of polarised cross-section, asymmetry and helicity angle measurements gives access to all relevant couplings - with percent to permille - level precision

Additional potential may exist with additional measurements and higher energy - potentially further improved BSM sensitivities
Not studied yet...



* Snowmass 2005 projection
LHC 14 TeV, 300 fb⁻¹

Summary

- Linear colliders will be capable of producing top quarks in a very clean environment: Excellent conditions for precision measurements of top quark properties and couplings
- The invariant mass can be reconstructed with an experimental precision of $O(100)$ MeV (stat+ syst), but suffers from substantial theoretical uncertainties
- A threshold scan provides the ultimate mass precision in a theoretically well-understood setting: Statistical uncertainties on the 30 MeV level, with comparable experimental systematics, studies of theoretical uncertainties ongoing
 - ▶ Total uncertainty of ~ 100 MeV or better in reach
- Polarised beams at linear colliders allow detailed measurements of top electroweak couplings with the separation of axial and vector and Z and γ contributions
 - accuracies on the percent to permille level expected

Backup

Systematics on Mass - Details

- Incomplete - but looked at several key aspects:
 - Theory uncertainties currently based on simple scaling of cross section (1%, 3%) (10 MeV up to ~50 MeV, depending on fit strategy -> uncertainty mostly absorbed in α_s uncertainty for combined fits) - More sophisticated studies planned, based on results by Beneke *et al.*, see next talk
 - Non-ttbar background: 5% uncertainty results in 18 MeV uncertainty on mass (After selection, the non-ttbar background cross section is ~ 70 fb, so 5% uncertainty can be reached with ~ 6 fb⁻¹ below threshold)
 - Beam energy: Expect 10⁻⁴ precision on CMS energy: ~30 MeV uncertainty on mass - potential for further improvement?
 - Luminosity spectrum - first study based on CLIC 3 TeV model (substantially more complicated than ILC): ~ 6 MeV uncertainty from fit of LS parameters

Systematics on Mass - Details

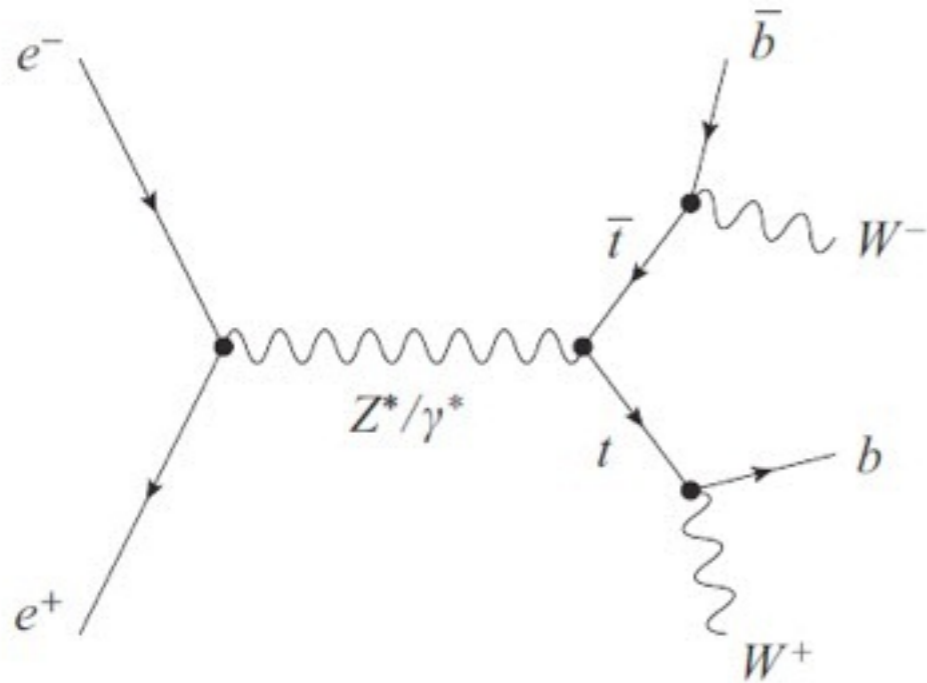
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“Interpretation” uncertainty:

Theory uncertainties are incurred when transforming the 1S mass used to describe the threshold to the \overline{MS} mass - currently $O \sim 100$ MeV, depending on α_s precision and number of orders - significant reduction possible when needed

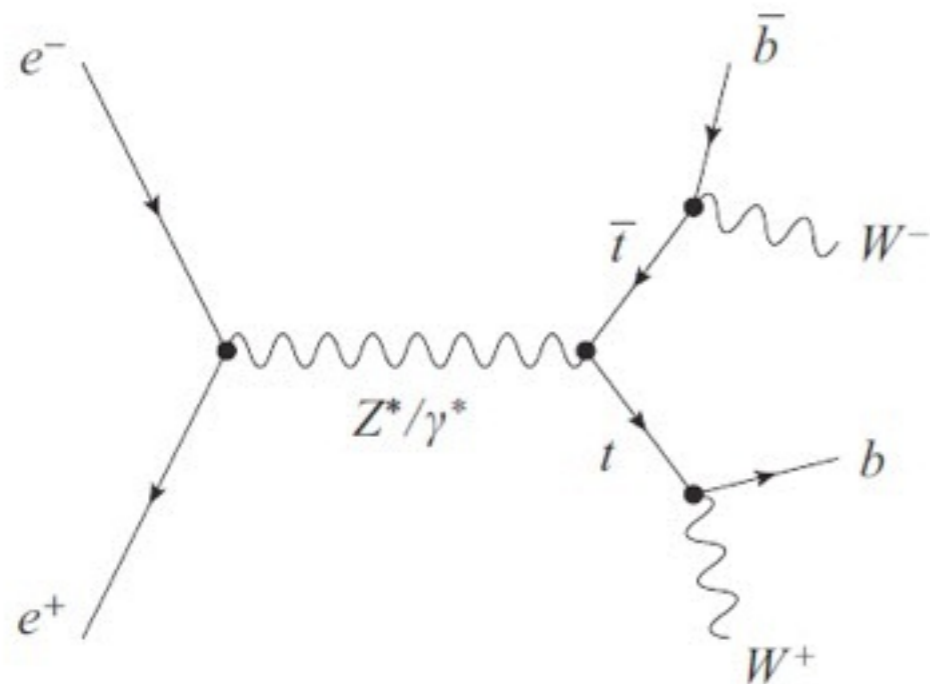
Reconstructing Top Quarks at Lepton Colliders

- Driven by production and decay:
 - Production in pairs, decay to W and b

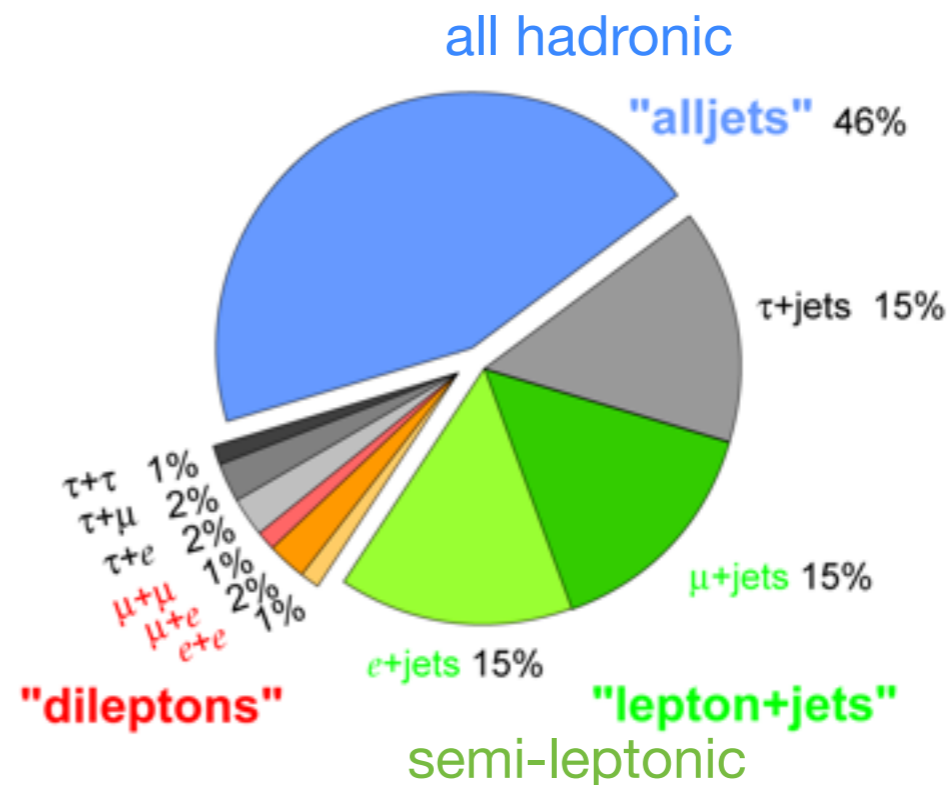


Reconstructing Top Quarks at Lepton Colliders

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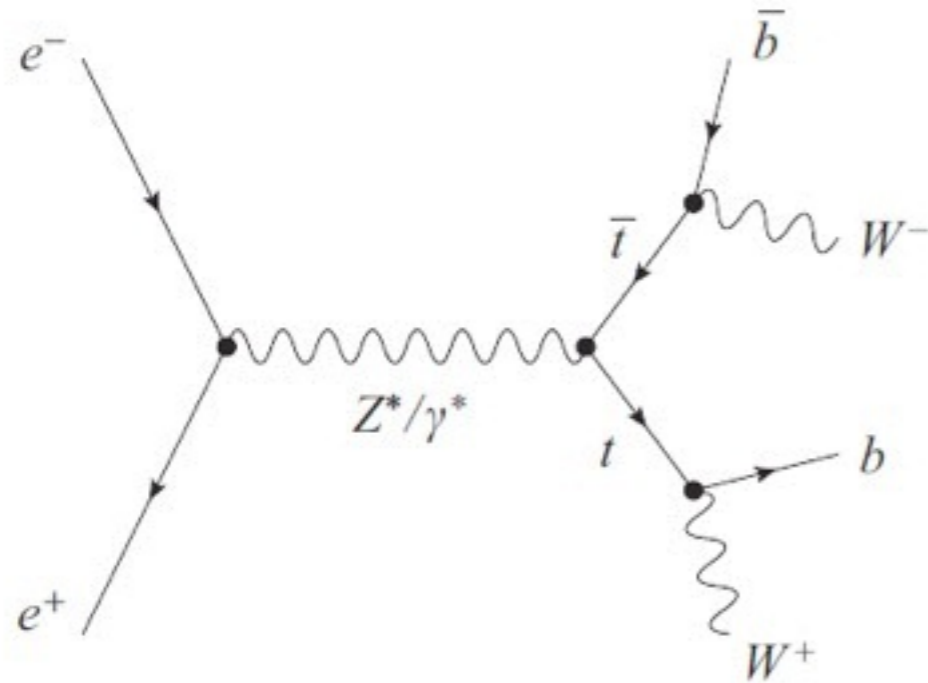


Event signature entirely given by the decay of the W bosons:

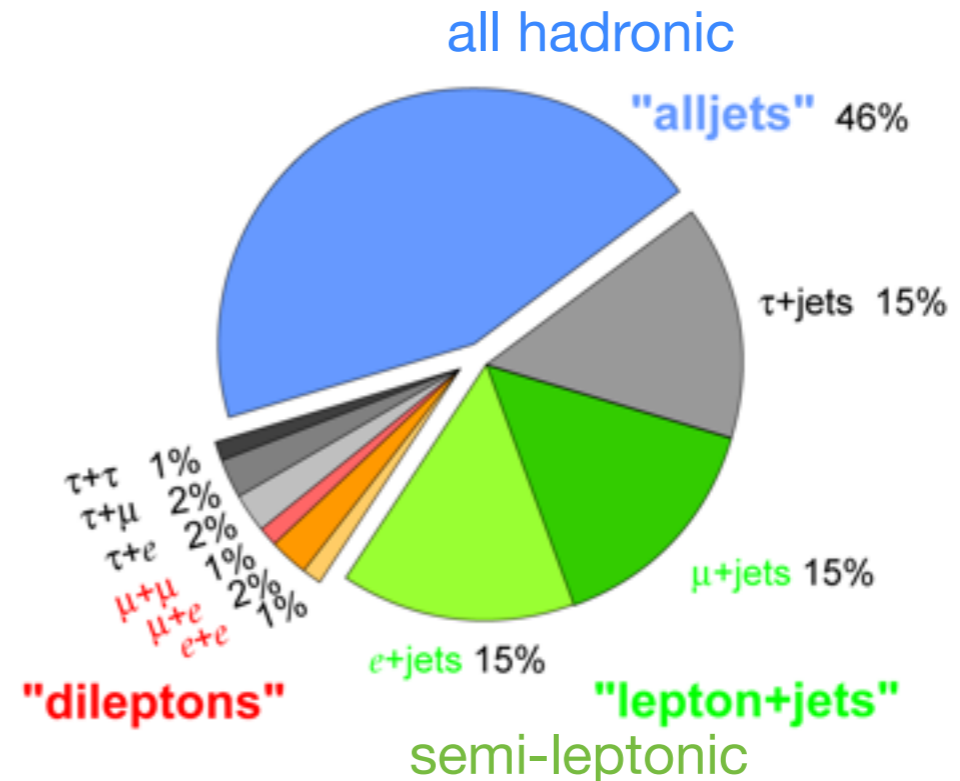


Reconstructing Top Quarks at Lepton Colliders

- Driven by production and decay:
 - Production in pairs, decay to W and b



Event signature entirely given by the decay of the W bosons:



- At hadron colliders: Hard to pick out top pairs from QCD background - Use one and two-lepton final states
- At lepton colliders: Top pairs easy to identify, concentrate on large branching fractions and controllable missing energy (not more than one neutrino!)

Analysis Strategy

- Identify the type of top decay according to number of isolated leptons
 - all-hadronic (0 leptons), semi-leptonic (1 lepton), leptonic (>1 lepton) -> rejected
- Jet clustering (exclusive k_t algorithm) according to classification: 6 or 4 jets
- Flavor-tagging: Identify the two most likely b-jet candidates
- W pairing: Jets / leptons into W bosons
 - Unique in the semi-leptonic case: 1 W from two light jets, 1 W from lepton & missing Energy
 - 3 possibilities (4 light jets) in all-hadronic case - Pick combination with minimal deviation from nominal W mass
- Kinematic fit - Use Energy/momentum conservation to constrain event
 - Performs the matching of W bosons and b-Jets to t candidates
 - Enforces equal t and anti-t mass: Only one mass measurement per event
 - Provides already good rejection on non-tt background
- Additional background rejection with likelihood method based on event variables (sphericity, b-tags, multiplicity, W masses, d_{cut} , top mass w/o kin fit)

Analysis Challenges & Event Simulation - CLIC

- Key reconstruction challenge at CLIC: pile-up of $\gamma\gamma \rightarrow$ hadrons background, rejected with timing & p_t cuts and with jet finding based on k_t algorithm
 - Also relevant for ILC: No pile-up, but several $\gamma\gamma \rightarrow$ hadrons events / BX - Jet finding now follows CLIC experience
- Event generation with PYTHIA (for $t\bar{t}$, LO) and WHIZARD, depending on final state
- Full GEANT4 detector simulation
- Reconstruction with PandoraPFA

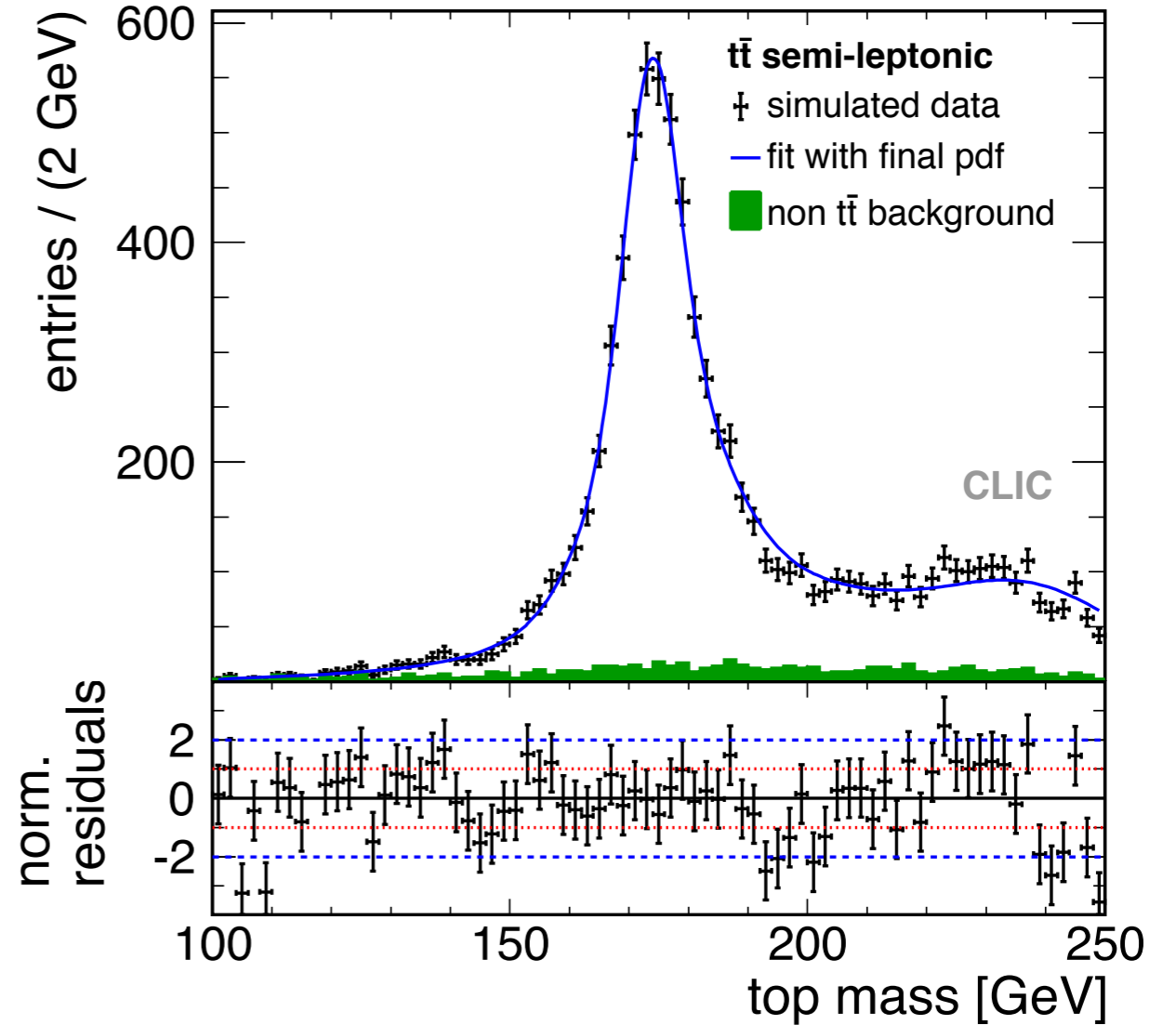
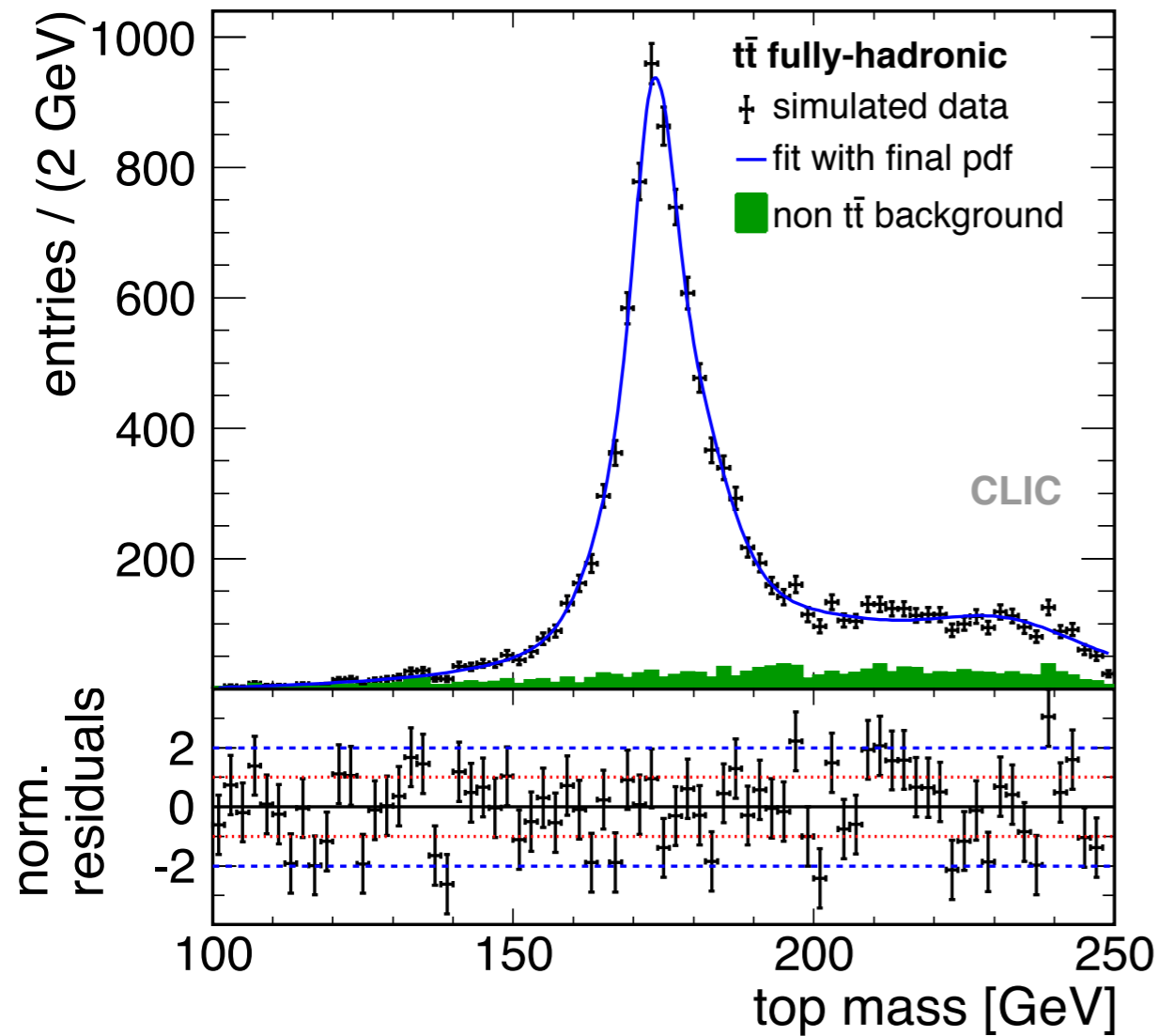
no direct simulation of threshold - currently using NNLO cross sections - *TOPPIK, Hoang & Teubner* -

both at and above threshold 100 fb^{-1} assumed

type	final state	σ 500 GeV	σ 352 GeV
Signal ($m_{\text{top}} = 174 \text{ GeV}$)	$t\bar{t}$	530 fb	450 fb
Background	WW	7.1 pb	11.5 pb
Background	ZZ	410 fb	865 fb
Background	$q\bar{q}$	2.6 pb	25.2 pb
Background	WWZ	40 fb	10 fb

... in addition: single top may be worth considering

Mass Reconstruction Above Threshold



- Width less constrained than mass: substantial detector effects (peak width ~ 5 GeV compared to 1.4 GeV top width)

channel	m_{top}	Δm_{top}	Γ_{top}	$\Delta\Gamma_{\text{top}}$
fully-hadronic	174.049	0.099	1.47	0.27
semi-leptonic	174.293	0.137	1.70	0.40
combined	174.133	0.080	1.55	0.22

Systematics - Invariant Mass above Threshold

- Still incomplete, but some key issues were investigated:
 - Possible bias from top mass and width assumptions in detector resolution: Below statistical error, no indication for bias found
 - Jet Energy Scale: Reconstruction of W bosons can be used to fix this to better than 1% for light jets, assume similar precision for b jets from Z and ZZ events: Systematics below statistical uncertainties of the measurement
 - Color Reconnection: Not studied yet - depends on space-time overlap of final-state partons from t and anti- t decay - Expected to be less than in WW at LEP2: Comparable or smaller systematics on mass - less than 100 MeV

The key issue - and open question:

Above threshold the “PYTHIA mass” is measured - not well defined theoretically

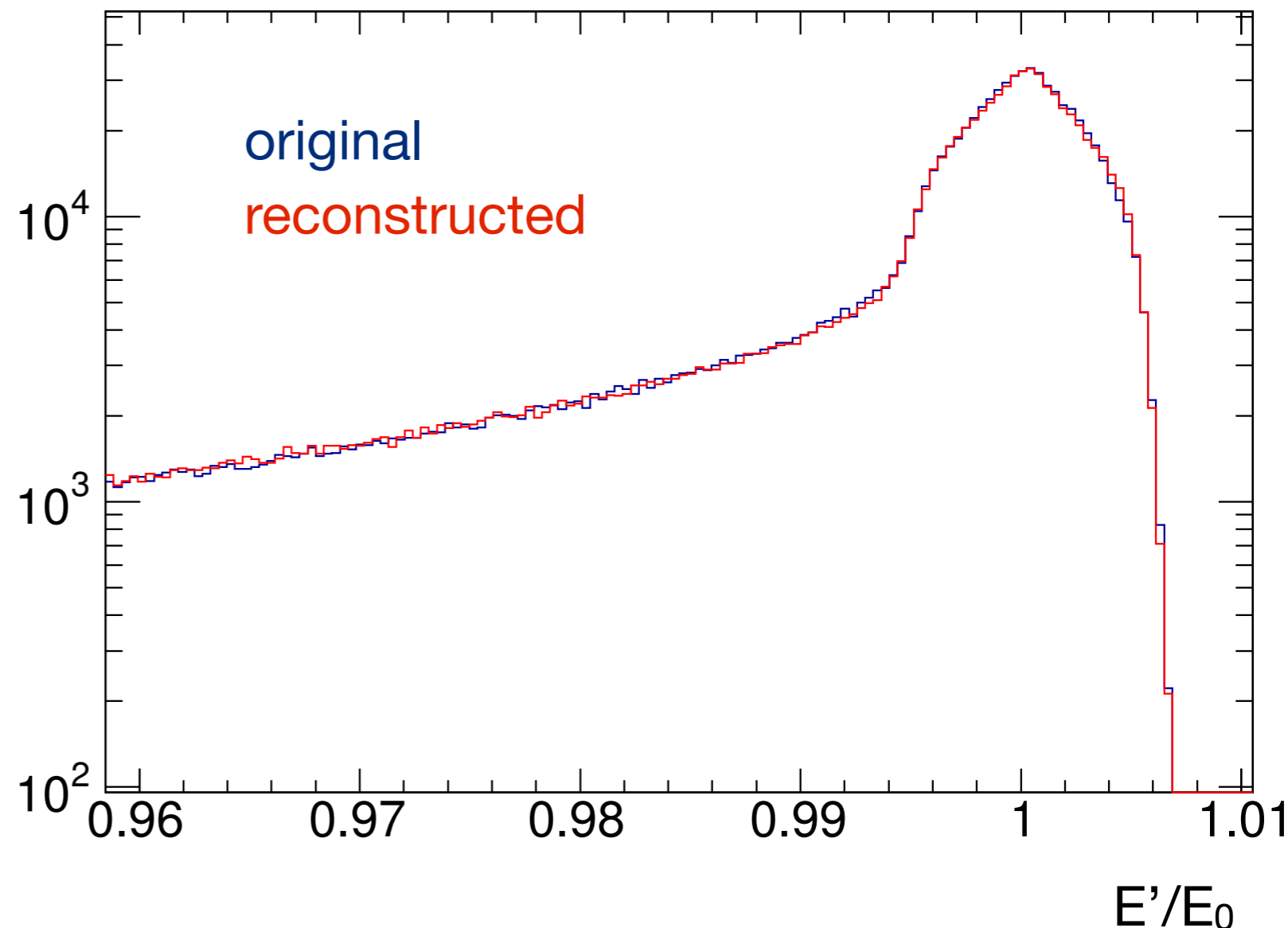
- ⇒ Substantial uncertainties in the interpretation of the measurements, far outweighs statistical uncertainties
- ⇒ Some theory work in this direction already exists, but more is needed (also in terms of connecting theory and experimental observables)



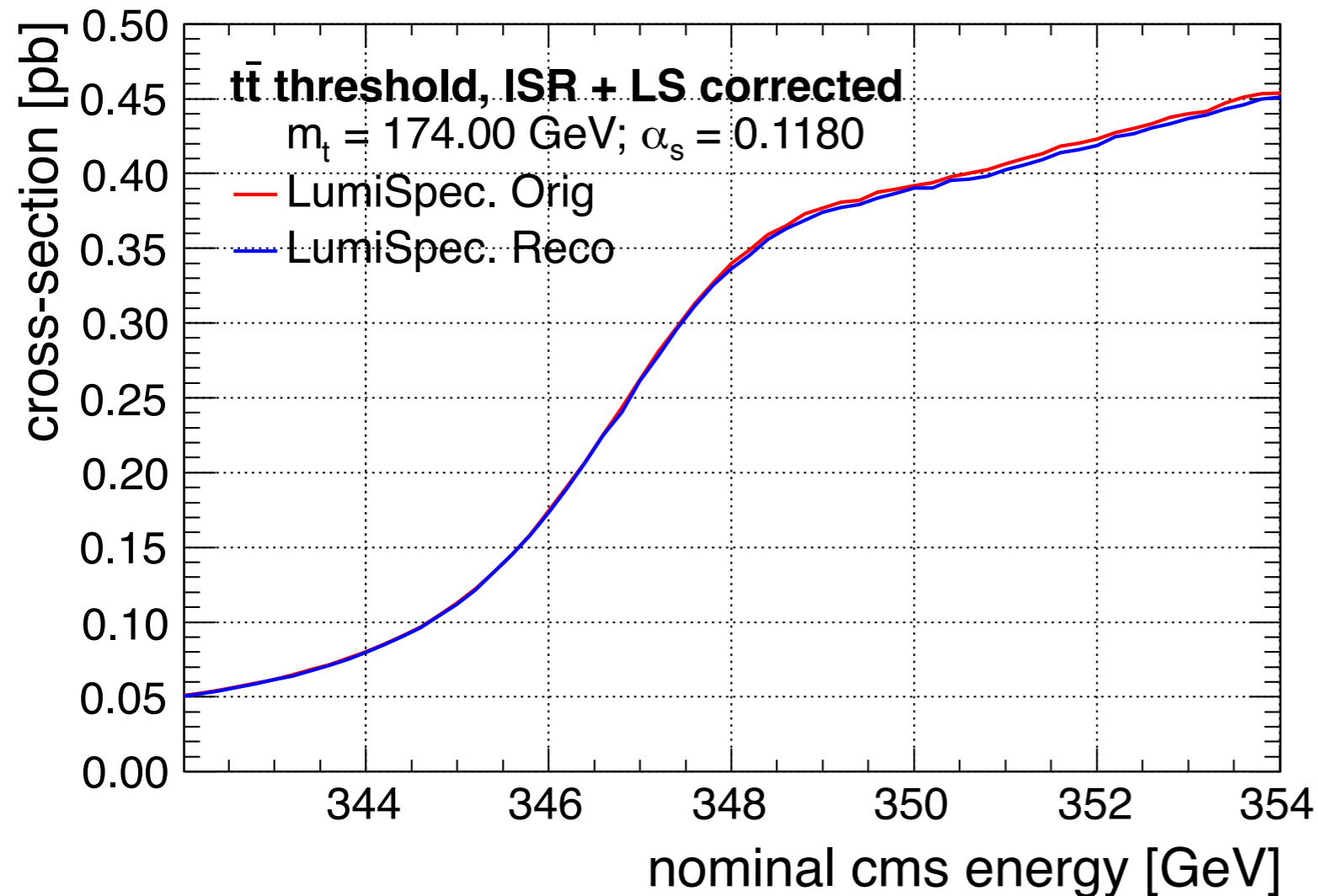
Systematics - Luminosity Spectrum

- Initial back-of-the envelope studies indicated possible systematics of 10s of MeV - mainly related to the shape of the main luminosity peak
- The challenge: Determining the shape (and normalization) of the luminosity spectrum from data
 - Accessible via energy and angle of e^\pm from Bhabha events
 - Parametrized by a complex 19 parameter function, parameters determined from fits to Bhabha events (details: arXiv:1309.0372)

First CLIC study: application of 3 TeV model to 350 GeV - not yet full simulations, scaled uncertainties



Systematics - Luminosity Spectrum



- Impact of reconstructed luminosity spectrum on threshold behavior
 - Currently still a small bias: slightly reduced peak luminosity in model (0.7% too low)
 - ▶ Reason understood, straightforward to correct

Global Results Summary - Luminosity Spectrum uncertainty for CLIC:

1D fit: $\Delta m_t = (\pm 22 \text{ (stat)} \pm \mathbf{5.3} \text{ (lumi parameters)} - \mathbf{22} \text{ (lumi reco)}) \text{ MeV}$

2D fit: $\Delta m_t = (\pm 34 \text{ (stat)} \pm \mathbf{6.0} \text{ (lumi parameters)} + \mathbf{5.5} \text{ (lumi reco)}) \text{ MeV}$

$\Delta \alpha_s = (\pm 9 \text{ (stat)} \pm \mathbf{2.5} \text{ (lumi parameters)} + \mathbf{10} \text{ (lumi reco)}) \times 10^{-4}$