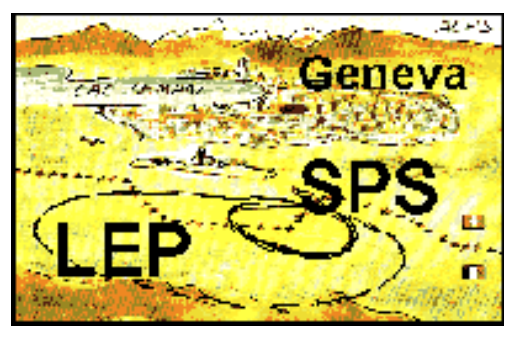
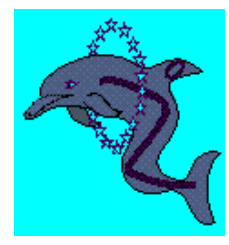
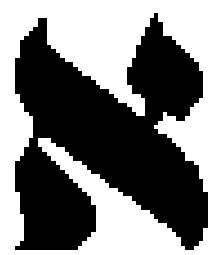
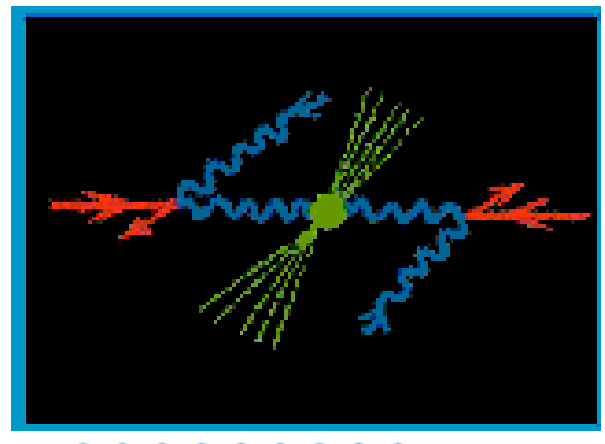


# Photon – Photon Physics

From



to



Richard Nisius (CERN)  
Holzhau, 2–7 October 1

# The programme...

## Introduction

1. The photon and photon structure
2. LEP and a LEP detector
3. The Linear Collider (LC)
4. Advantages of a Photon Collider (PC)
5. Compton backscattering and background

## Photon–photon scattering

1. Total cross-section
2. Jet cross-sections
3. Heavy flavour production

## Deep–inelastic electron–photon scattering

1. QED structure functions
2. The charm structure function  $F_{2,c}^\gamma$
3. Bottom production
4. The hadronic structure function  $F_2^\gamma$
5. Flavour decomposition of  $F_2^\gamma$
6. Polarized structure functions
7. Hadronic structure function for virtual photons

**...continued**

## Interactions of two virtual photons

1. QED signatures
2. BFKL signatures
  - a)  $\gamma^*\gamma^* \rightarrow$  hadrons
  - b)  $J/\psi$  production

## New signatures

1. Higgs production
  - a)  $\gamma\gamma \rightarrow h_0$
  - b) MSSM Higgs
1. Production of W-pairs
2. Production of Z-pairs
3. Single top production

# The 'history' of the photon

Date	Event
8.11.1895	Röntgen discovers the X-rays (first Nobel Prize for physics 1901).
1900	Planck interprets light as 'energy quanta' $E = h\nu$ , with $h = 6.626 \cdot 10^{-34} Js$ .
1905	Einstein explains the photoelectric effect by 'photons'.
1922	Discovery of Compton scattering $e\gamma \rightarrow e'\gamma'$ .
1927	Heisenberg formulates the uncertainty principle e. g. $\Delta E \Delta t \geq \hbar$ .
1930	First attempt to measure photon-photon scattering by Hughes et. al.
1936	First calculation of photon-photon scattering by Euler und Kockel.
1981	First measurement of the hadronic structure function of the photon by PLUTO.
2011	The Higgs Boson will be produced through photon-photon fusion at TESLA?

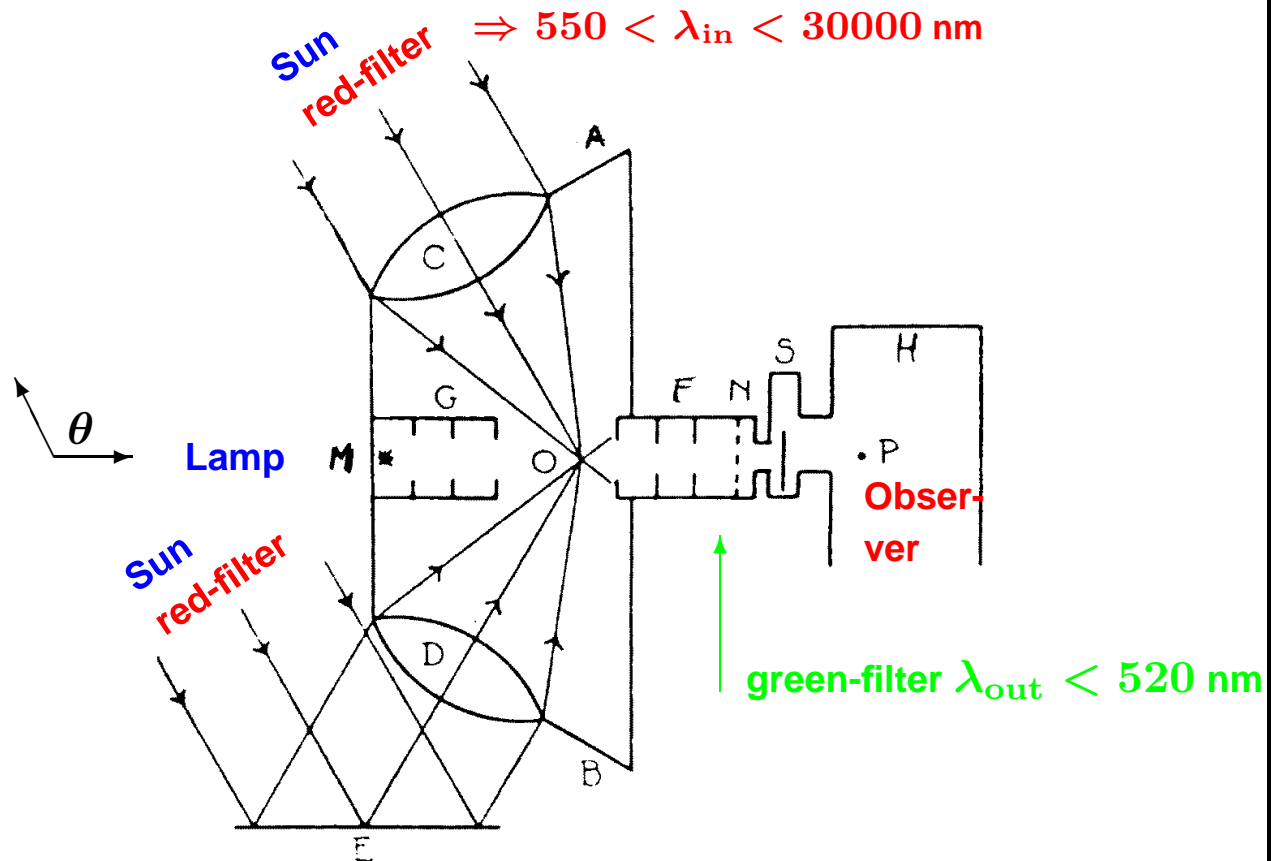
# Properties of the photon

Property	
Mass ( $m$ )	0 ( $m/m_e < 4 \cdot 10^{-22}$ , [1])
Charge ( $Q$ )	0 ( $Q/Q_e < 5 \cdot 10^{-30}$ , [2])
Velocity ( $c$ )	299792458 m/s
Spin parity ( $J^{PC}$ )	$1^{--}$
Coupling ( $\alpha$ )	$1/137.03599976(50)$
Task	Carrier of the electromagnetic interaction, no self-coupling

[1] Roderic Lakes, Phys. Rev. Lett. 80 (1998) 1826.

[2] Georg Raffelt, Phys. Rev. D50 (1994) 7792.

# The 'first' photon – photon collider anno 1930



$$\gamma_1(\lambda_{in})\gamma_2(\lambda_{in}) \rightarrow \gamma'_1(\lambda_{out})\gamma'_2(\lambda_{out})$$

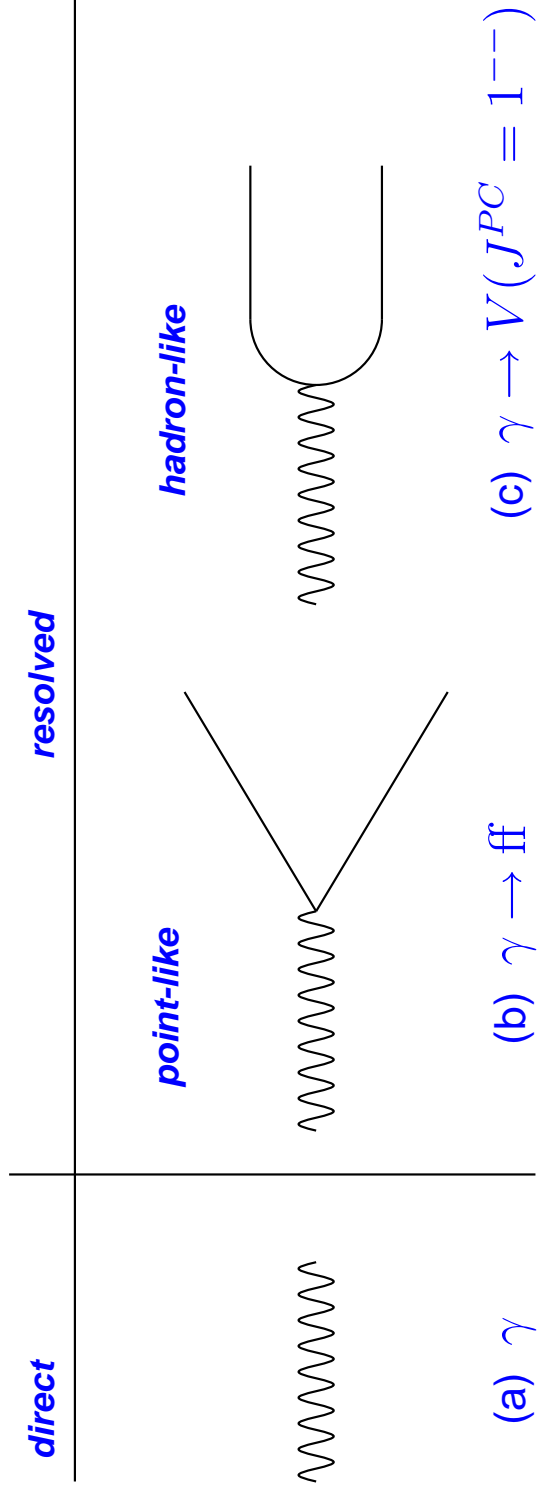
with:  $\lambda_{out} = \lambda_{in}(1 + \cos \theta)$

No light was observed.

$$\Rightarrow \sigma_{\gamma\gamma \rightarrow \gamma\gamma} < 3 \cdot 10^8 \text{ pb}$$

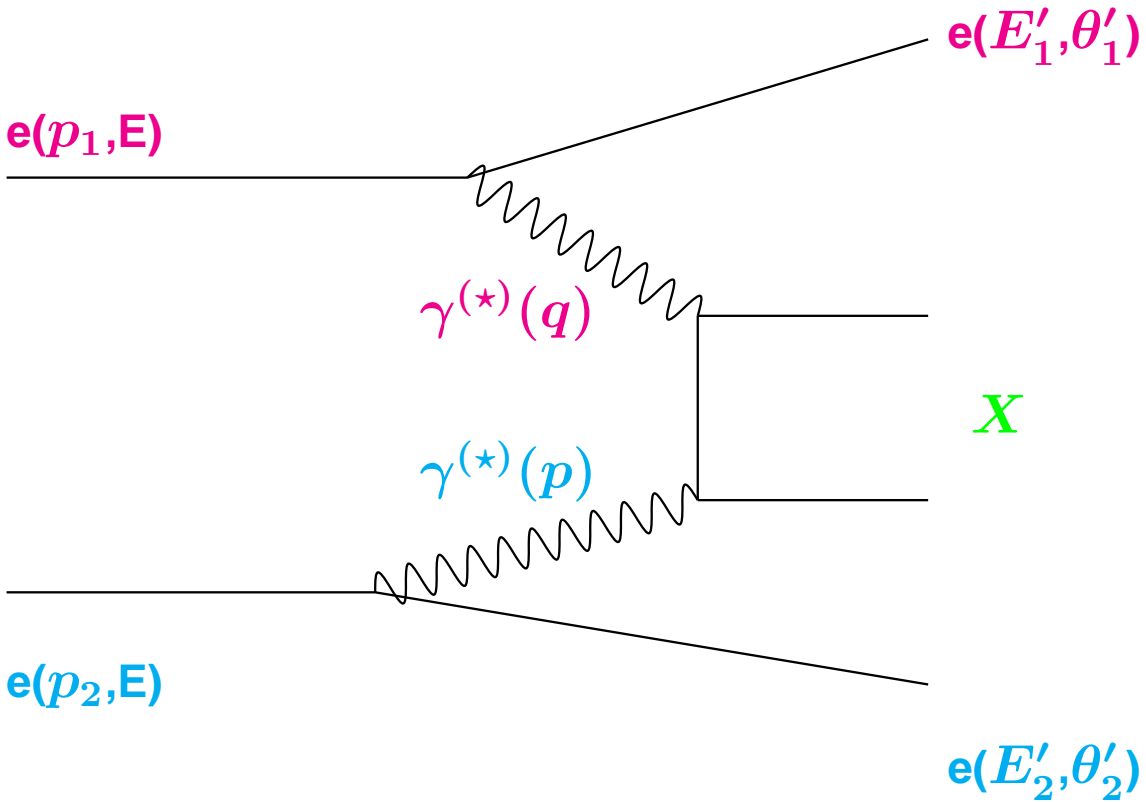
A.L. Hughes and G.E.M. Jauncey, Phys.Rev. 36 (1930) 773.

## Why do we talk about photon structure?



- 1) In (a) the whole photon interacts  $\Rightarrow$  **NO structure.**
- 2) The fluctuations (b,c) exist due to the uncertainty principle  $\Rightarrow$  **photon 'structure'.**
- 3) The typical lifetime of the fluctuations **increases with the photon energy and decreases with the photon virtuality.**

# The reaction $e e \rightarrow e e X$



$$d^6\sigma = \frac{d^3p'_1 d^3p'_2}{E'_1 E'_2} \frac{\alpha^2}{16\pi^4 Q^2 P^2} \left[ \frac{(q \cdot p)^2 - Q^2 P^2}{(p_1 \cdot p_2)^2 - m_e^2 m_e^2} \right]^{1/2}$$

$$\left( 4\rho_1^{++} \rho_2^{++} \sigma_{TT} + 2\rho_1^{++} \rho_2^{00} \sigma_{TL} \right.$$

$$\left. + 2\rho_1^{00} \rho_2^{++} \sigma_{LT} + \rho_1^{00} \rho_2^{00} \sigma_{LL} + \right.$$

$$\left. 2|\rho_1^{+-} \rho_2^{+-}| \tau_{TT} \cos 2\bar{\phi} - 8|\rho_1^{+0} \rho_2^{+0}| \tau_{TL} \cos \bar{\phi} \right)$$

$$Q^2 = -q^2 = 2 E E'_1 (1 - \cos \theta'_1)$$

$$P^2 = -p^2 = 2 E E'_2 (1 - \cos \theta'_2)$$

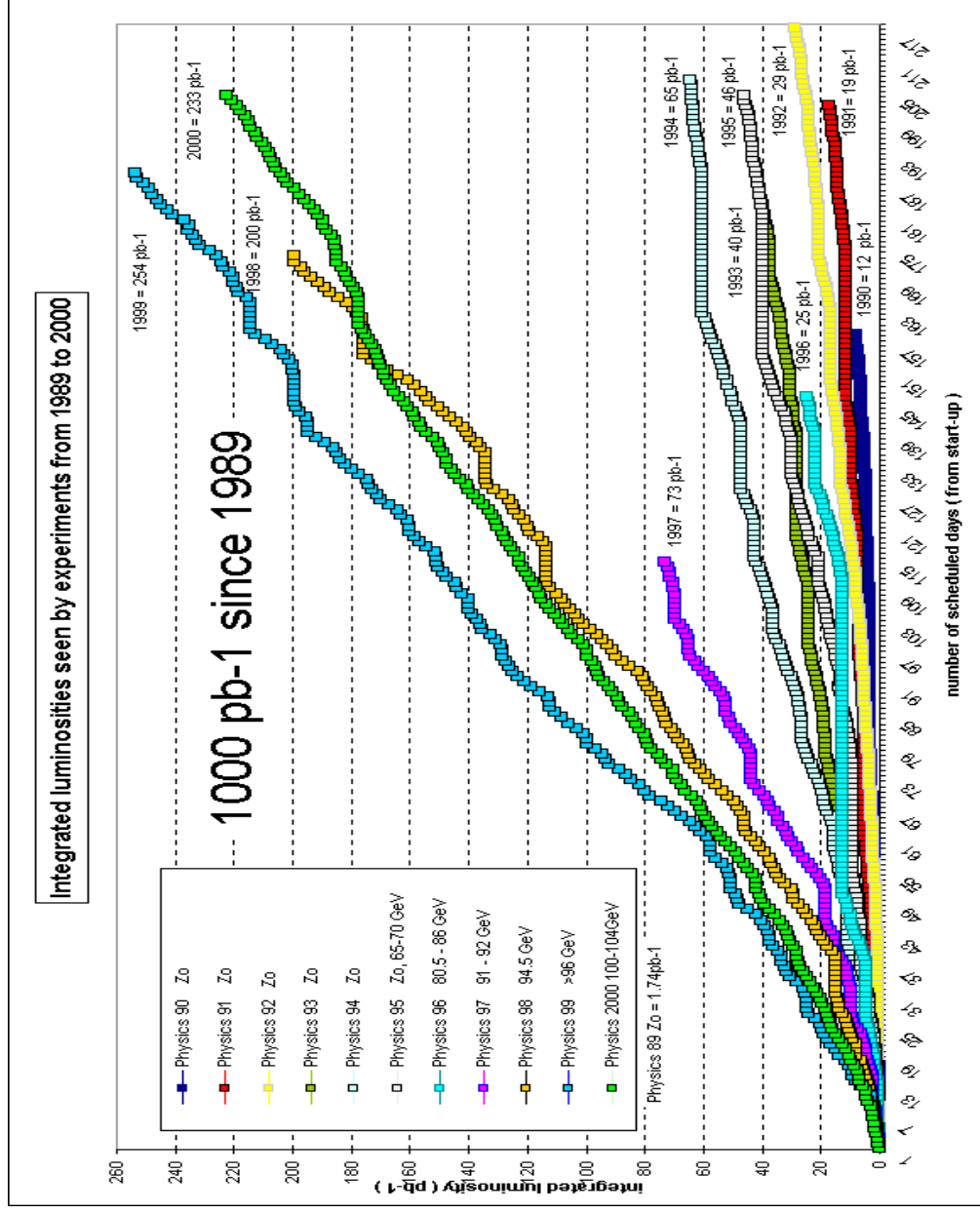
$$x = \frac{Q^2}{Q^2 + W^2 + P^2}$$



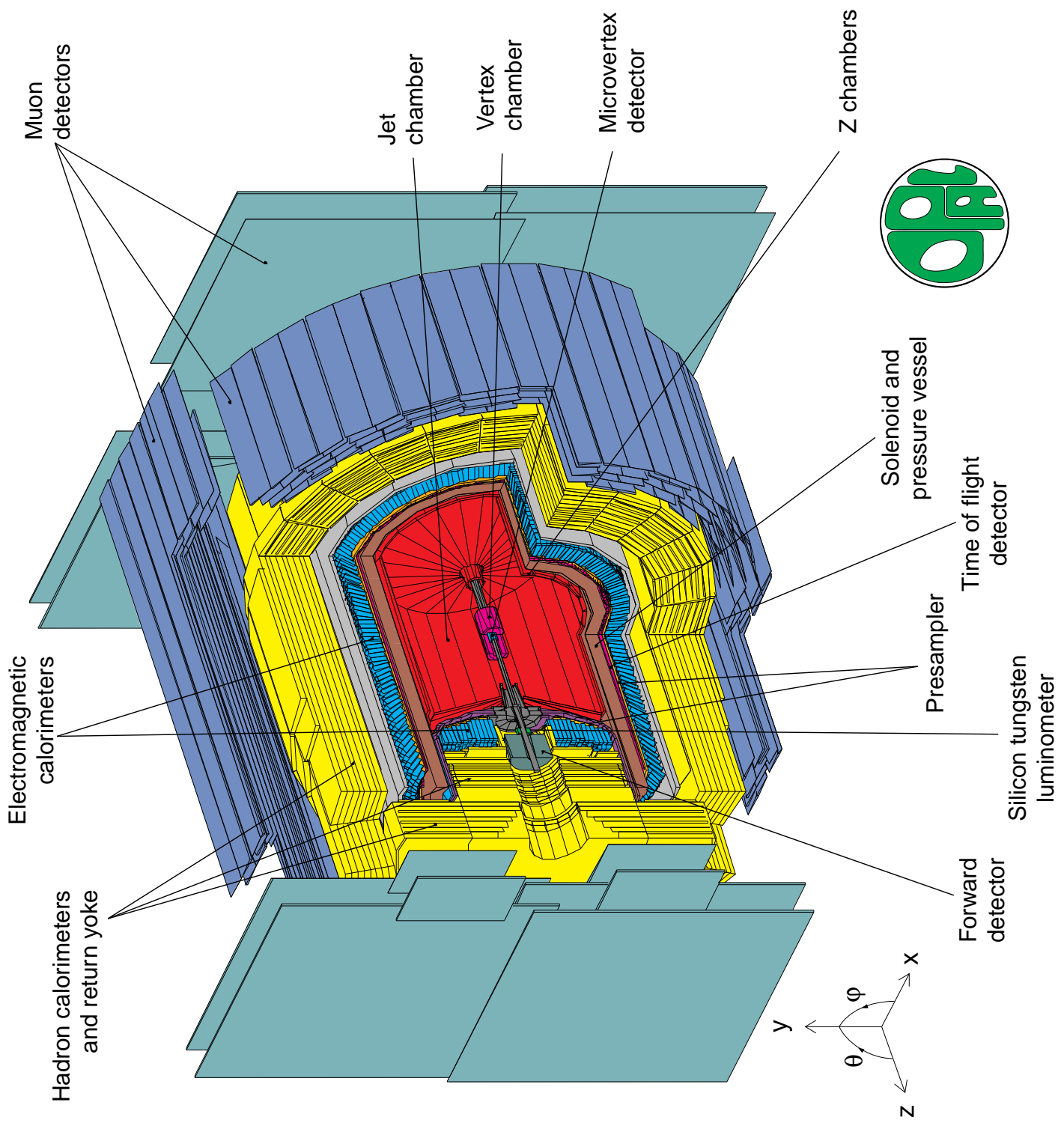
# The LEP Accelerator



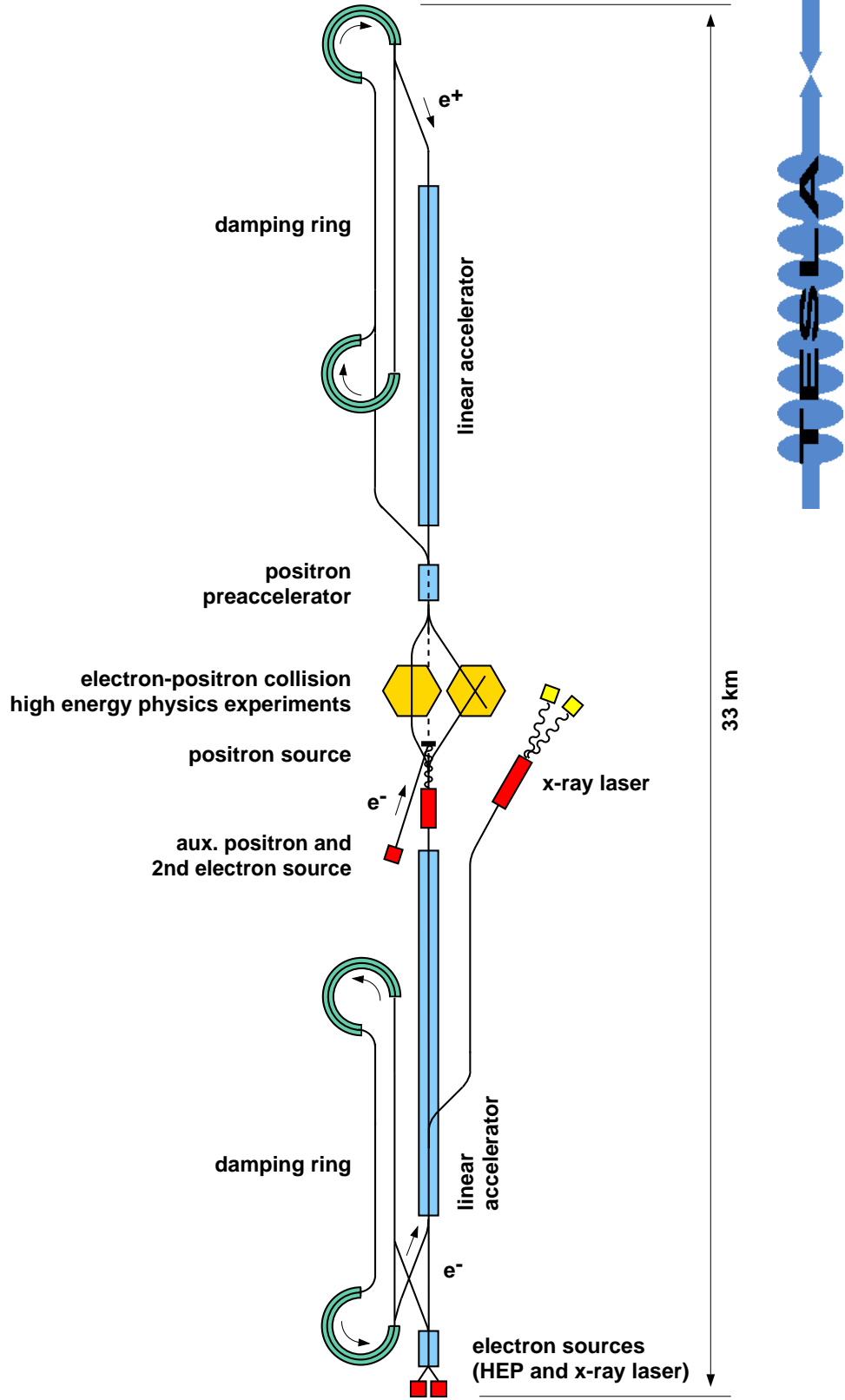
# The integrated luminosities



The integrated luminosity of the LEP programme exceeds 1000 pb<sup>-1</sup>.



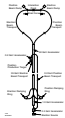
# Layout of a future Linear Collider



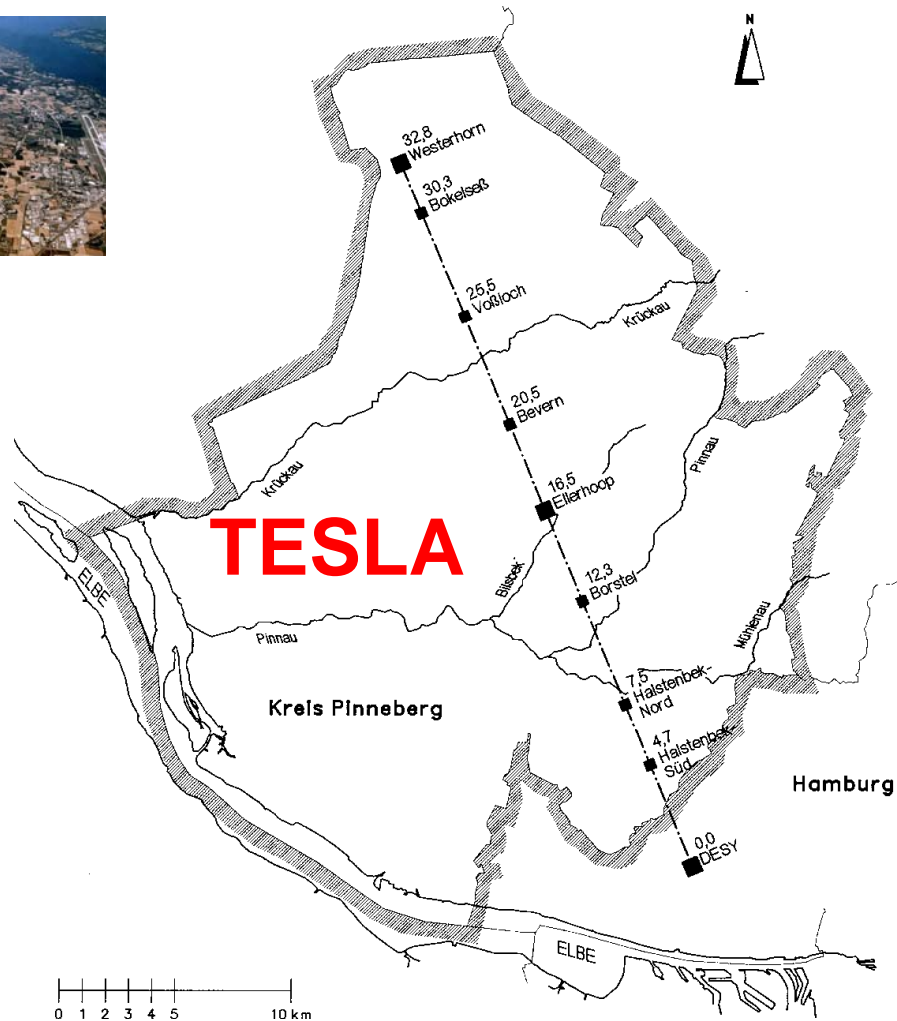
# From LEP/ SLC to TESLA



LEP



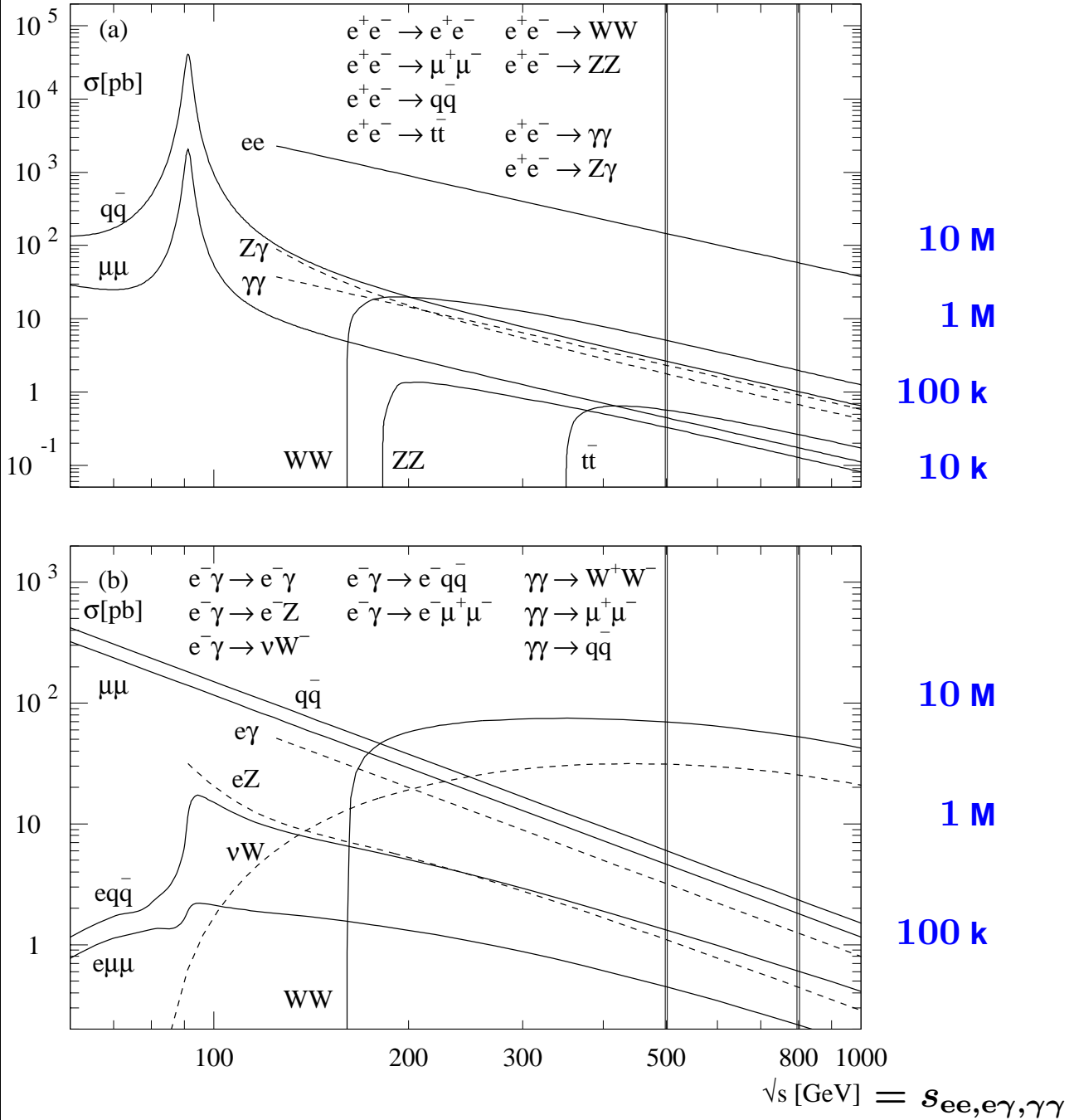
SLC



		LEP	SLC	TESLA
radius	[km]	8.5	$\infty$	$\infty$
length	[km]	26.7	4	33
gradient	[MV/m]	6	10	23.4
$\sigma_x/\sigma_y$	$[\mu\text{m}/\mu\text{m}]$	110 / 5	1.4 / 0.5	0.553/0.005
energy	[GeV]	100	50	250
lumi.	$[10^{31}/\text{cm}^2\text{s}]$	7.4	0.1	3400
$\mathcal{L}_{\text{int}}$	[1/pb y]	250	15	10-100k

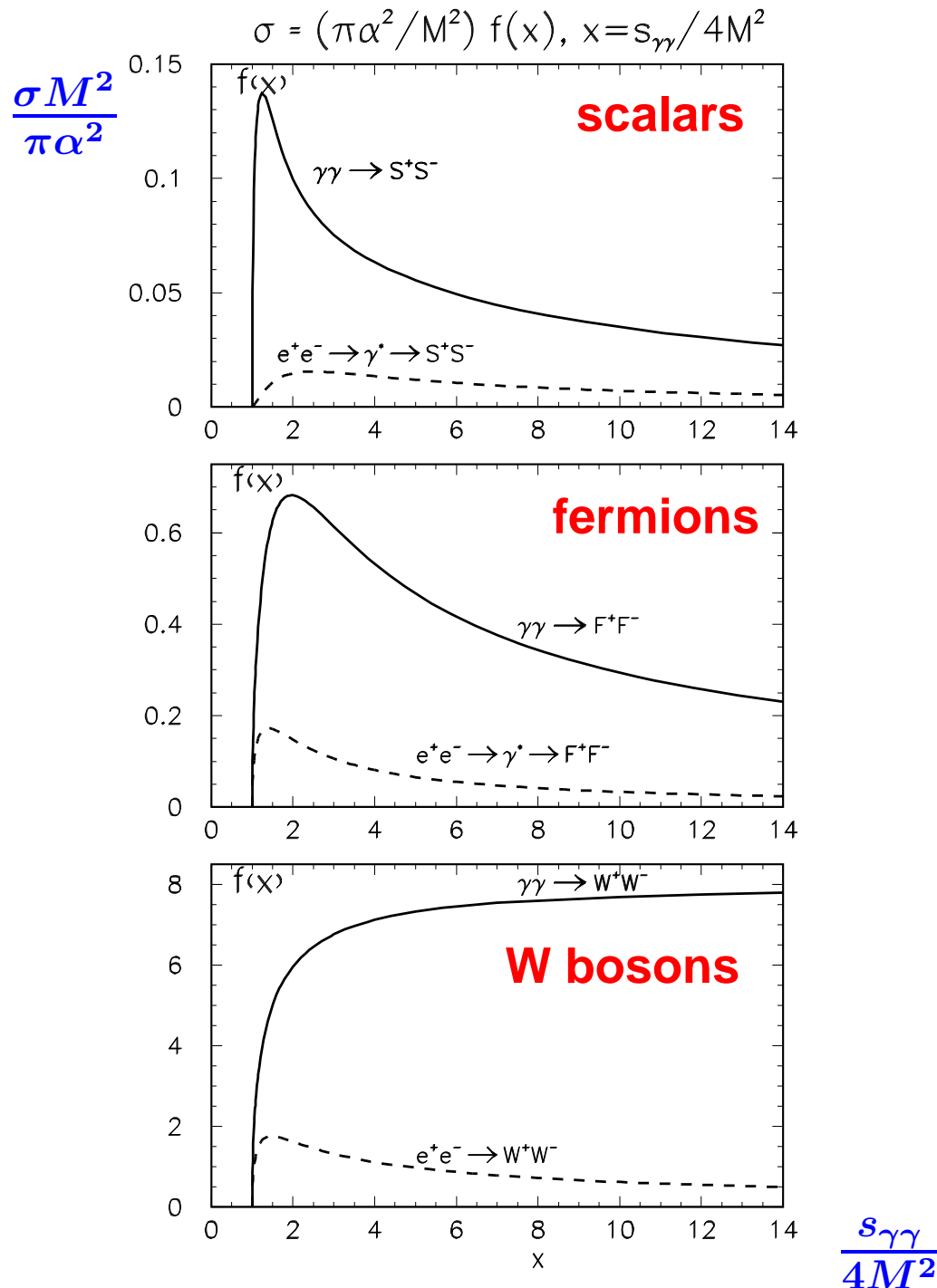
# The expected cross-sections

assume:  $\mathcal{L}_{\text{int}} = 100 \text{ fb}^{-1}/y \Rightarrow$  Events/y



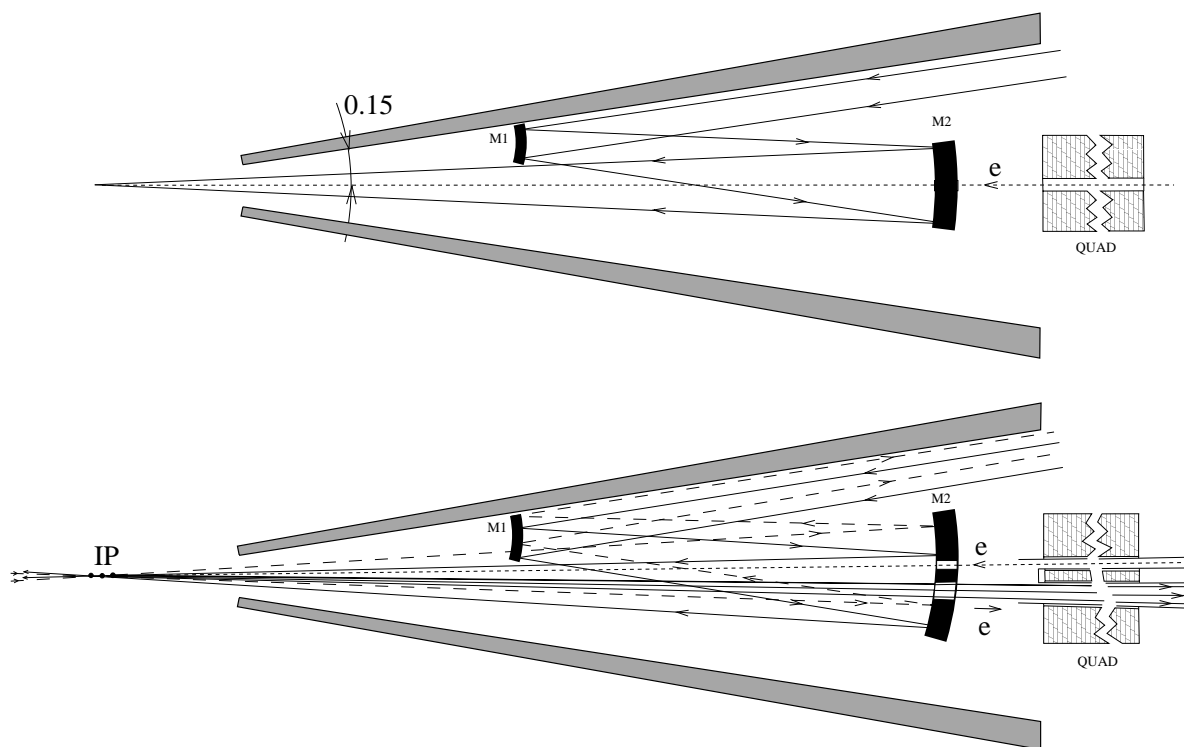
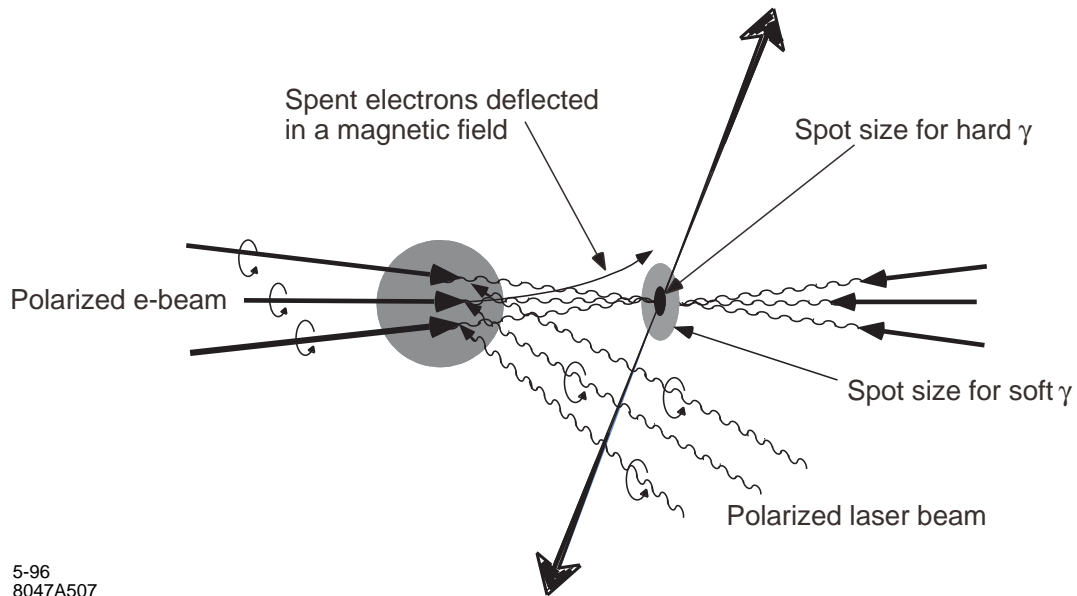
$10 < \theta_i < 170 \text{ deg}, M_{\mu^+\mu^-, q\bar{q}} > 50 \text{ GeV}$

# Charged particle pair production



**The photon collider has larger cross sections than the  $e^+e^-$  collider for several final states.**

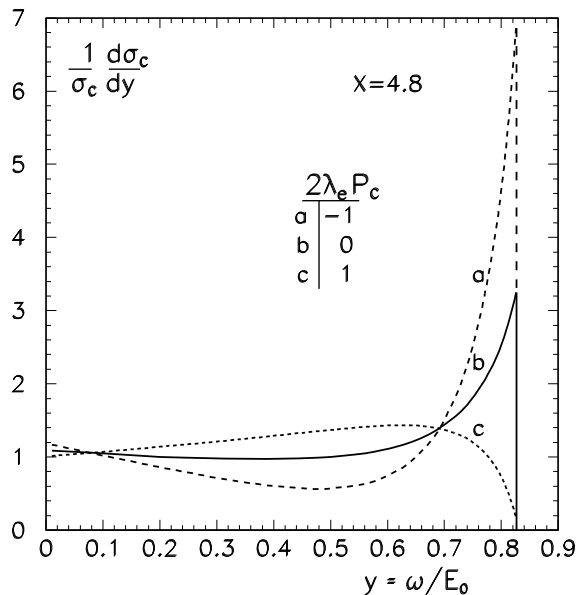
# The creation of the photon beam



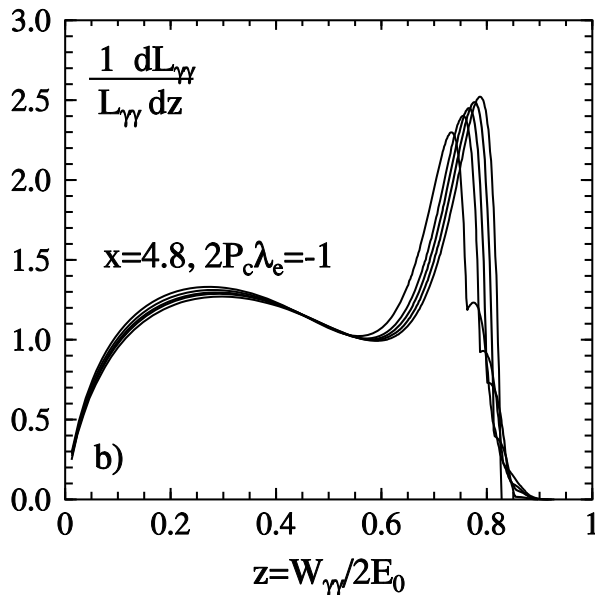


# Some features of a Photon Collider

## helicities

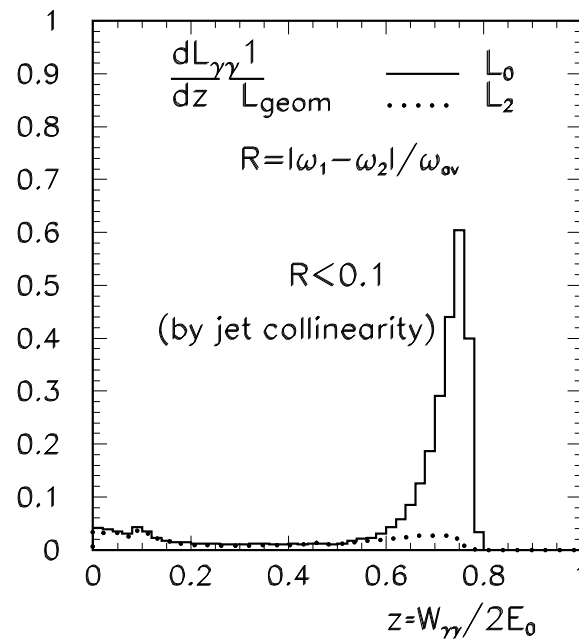
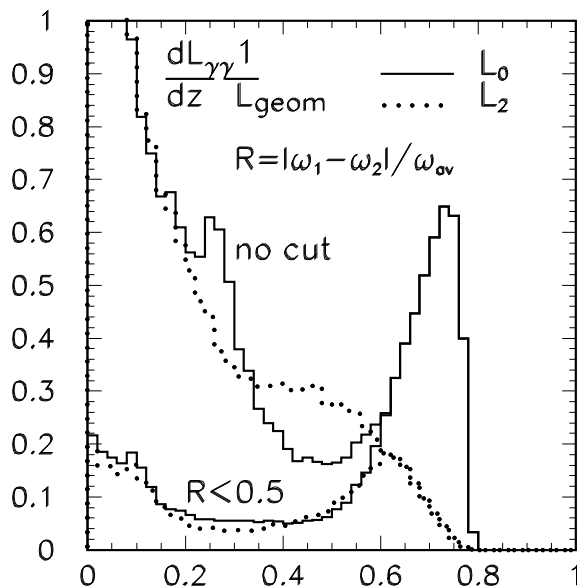


## non-linear effects



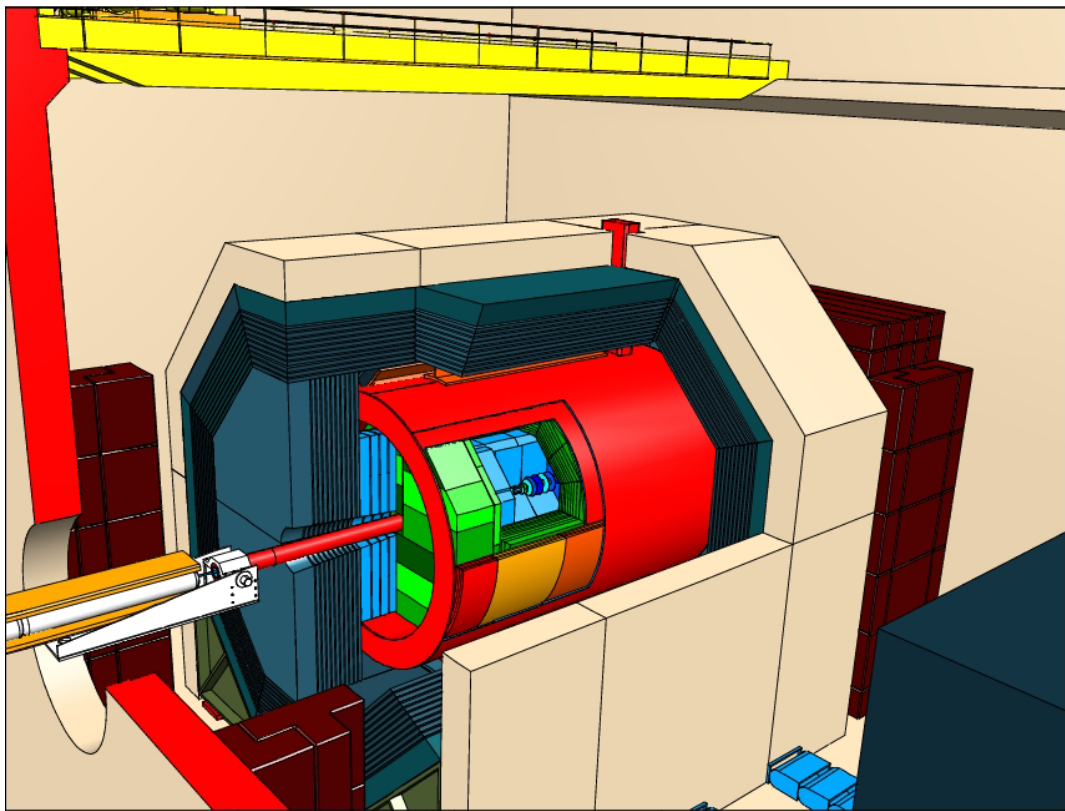
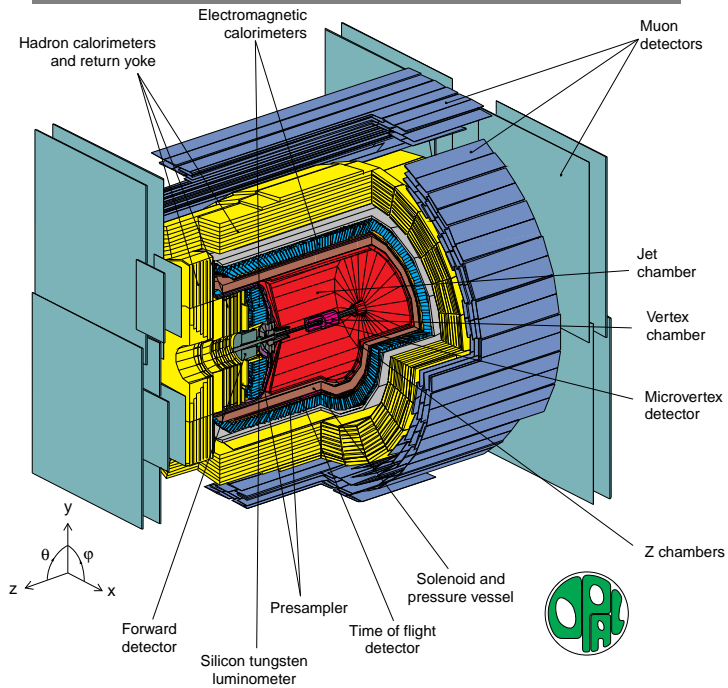
## Photon energy spectra

TESLA(500)

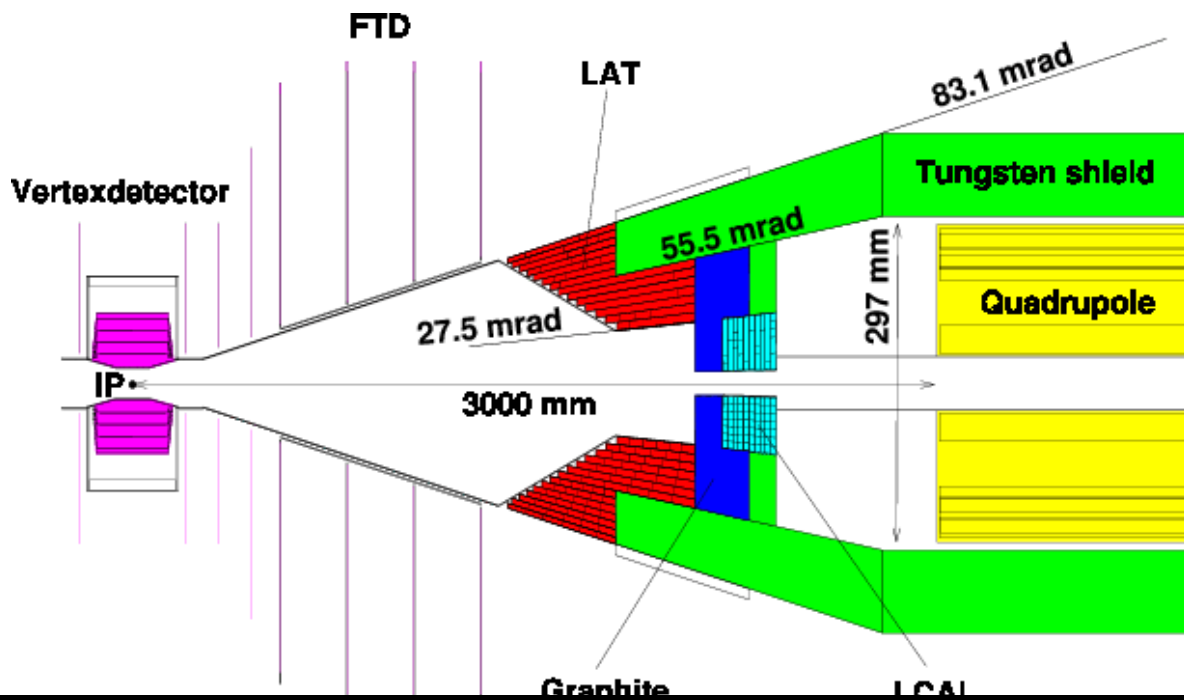
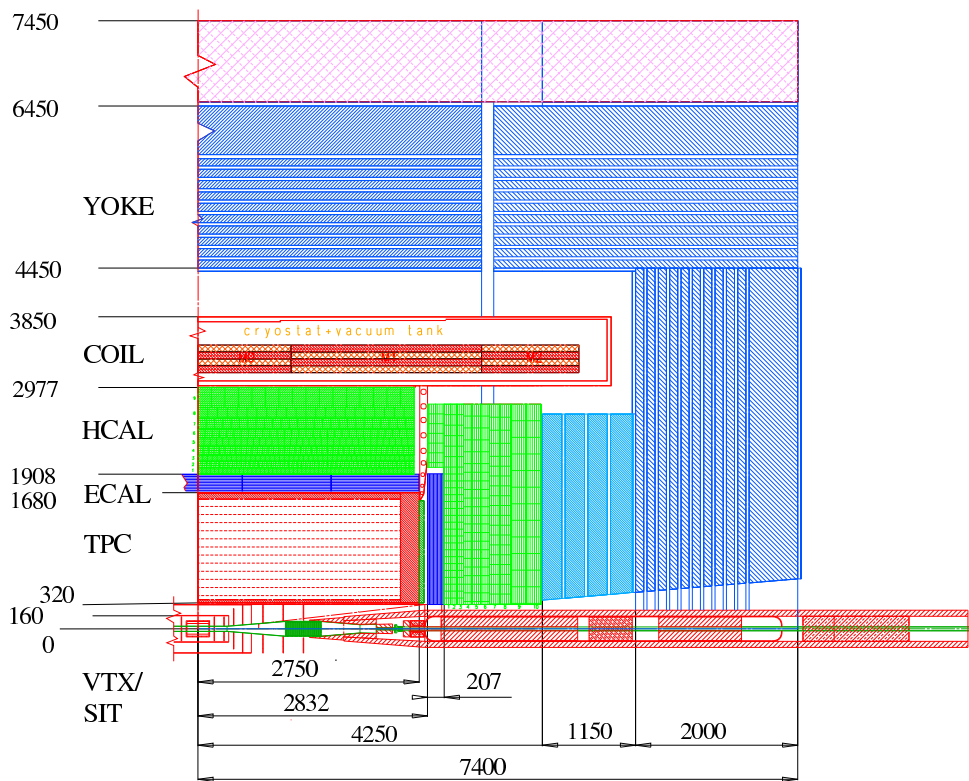


## Luminosity spectra

# From LEP to TESLA the detector



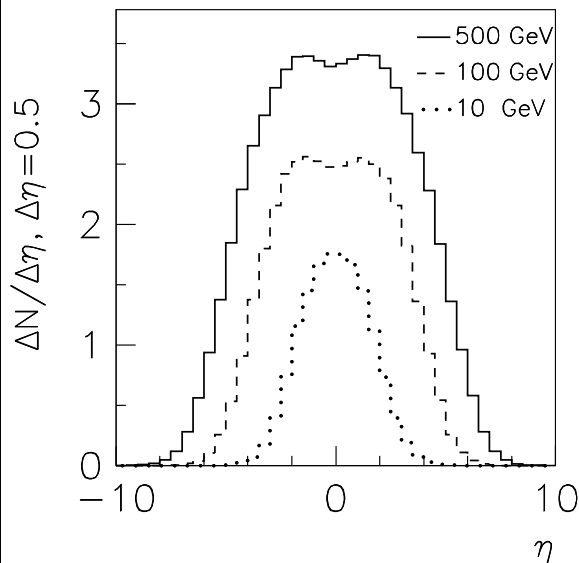
# The general detector concept



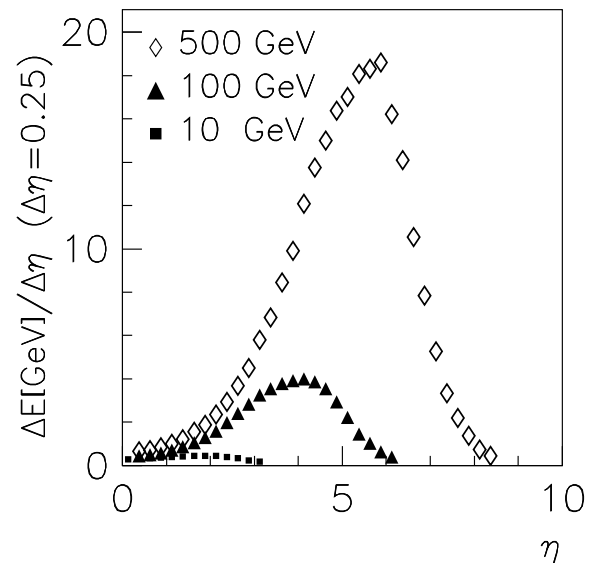
## Some features of the background

$\gamma\gamma \rightarrow$  hadrons

Particle flow



Energy flow



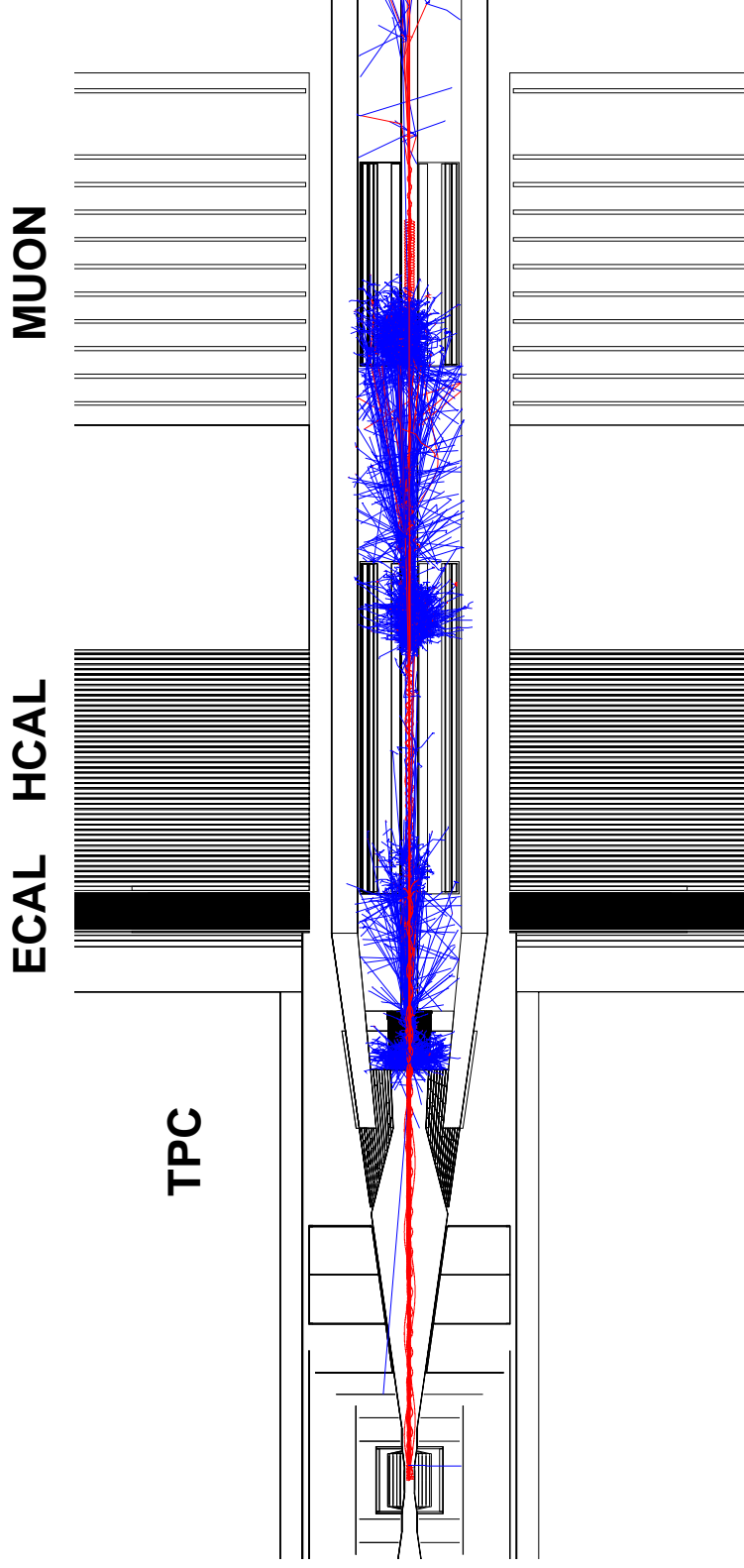
On average this yields 3.7 hadronic events per BX.

For  $W_{\gamma\gamma} = 500 \text{ GeV}$  one expects on average 25 particles within  $-2 \leq \eta \leq 2$  and with  $E_{\text{tot}} \approx 15 \text{ GeV}$ .

Incoherent  $e^+e^-$  pair creation:

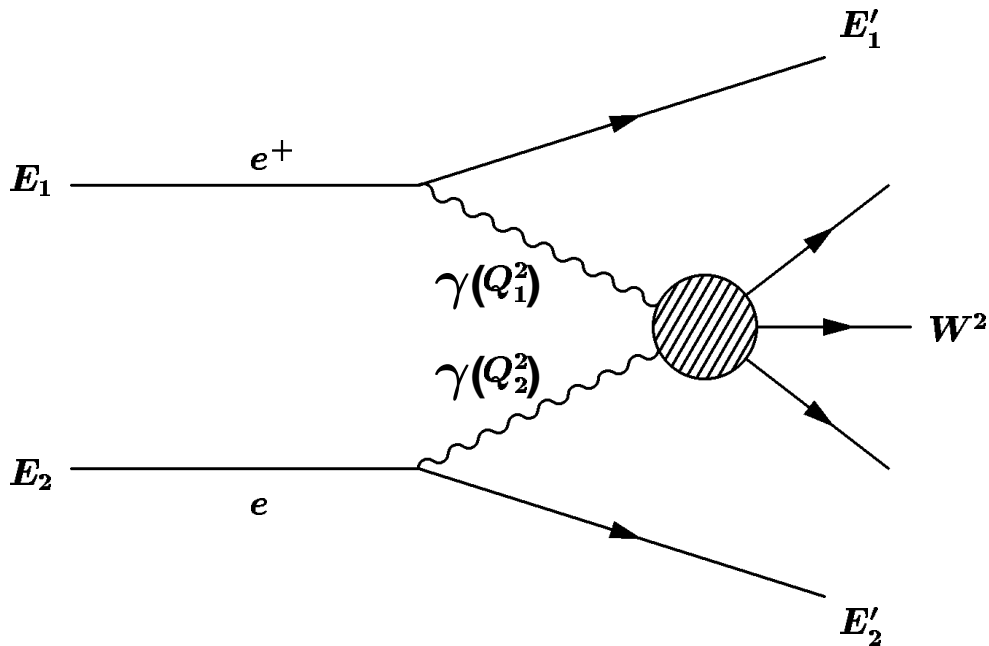
$10^5 e^+e^-$  pairs per BX with  $E_{\text{tot}} = 1.5 \cdot 10^5 \text{ GeV}$ ,  
and within the detector  $E = 2 \cdot 10^4 \text{ GeV}$  for  
 $\theta_e > 10 \text{ mrad}$  and  $p_e < 1 \text{ GeV}$

## The background from $10 e^+ e^-$ pairs



**A very unfriendly environment for the Low Angle Tagger (LAT) and especially for the Luminosity Calorimeter (LCAL)**

# Photon — photon scattering



Interaction of two quasi-real photons

$$\gamma\gamma \rightarrow X$$

e.g.  $X(s_{\gamma\gamma}) = \ell^+\ell^-, q\bar{q}, Q\bar{Q}, z^0z^0, W^+W^-, H$

$$Q_i^2 = 2E_i E'_i (1 - \cos \theta_i) \approx 0$$

$$W^2 = s_{\gamma\gamma} = \left( \sum_h E_h \right)^2 - \left( \sum_h \vec{p}_h \right)^2$$

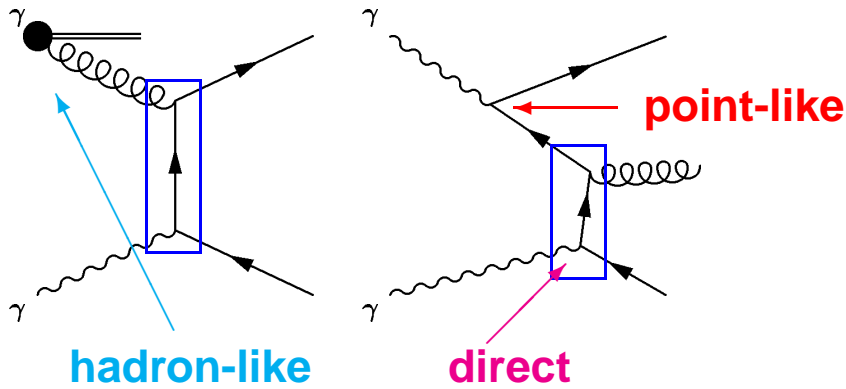
# Leading order diagrams

Direct:

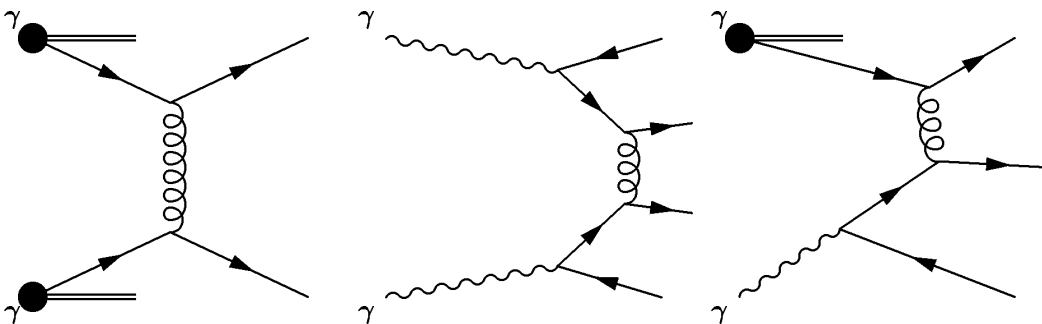


single resolved

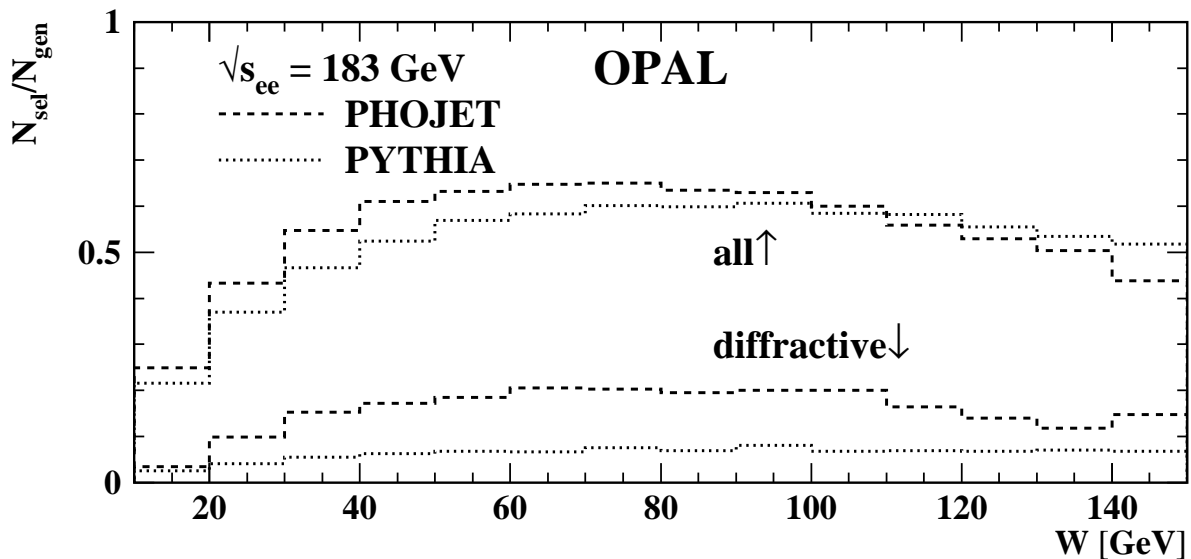
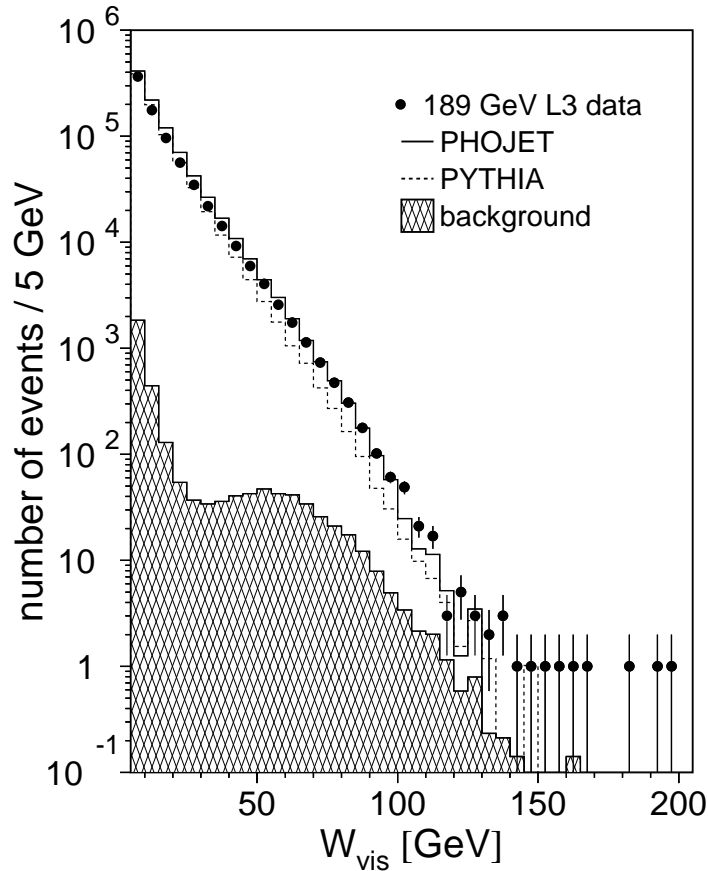
Single-Resolved:



Double-Resolved:



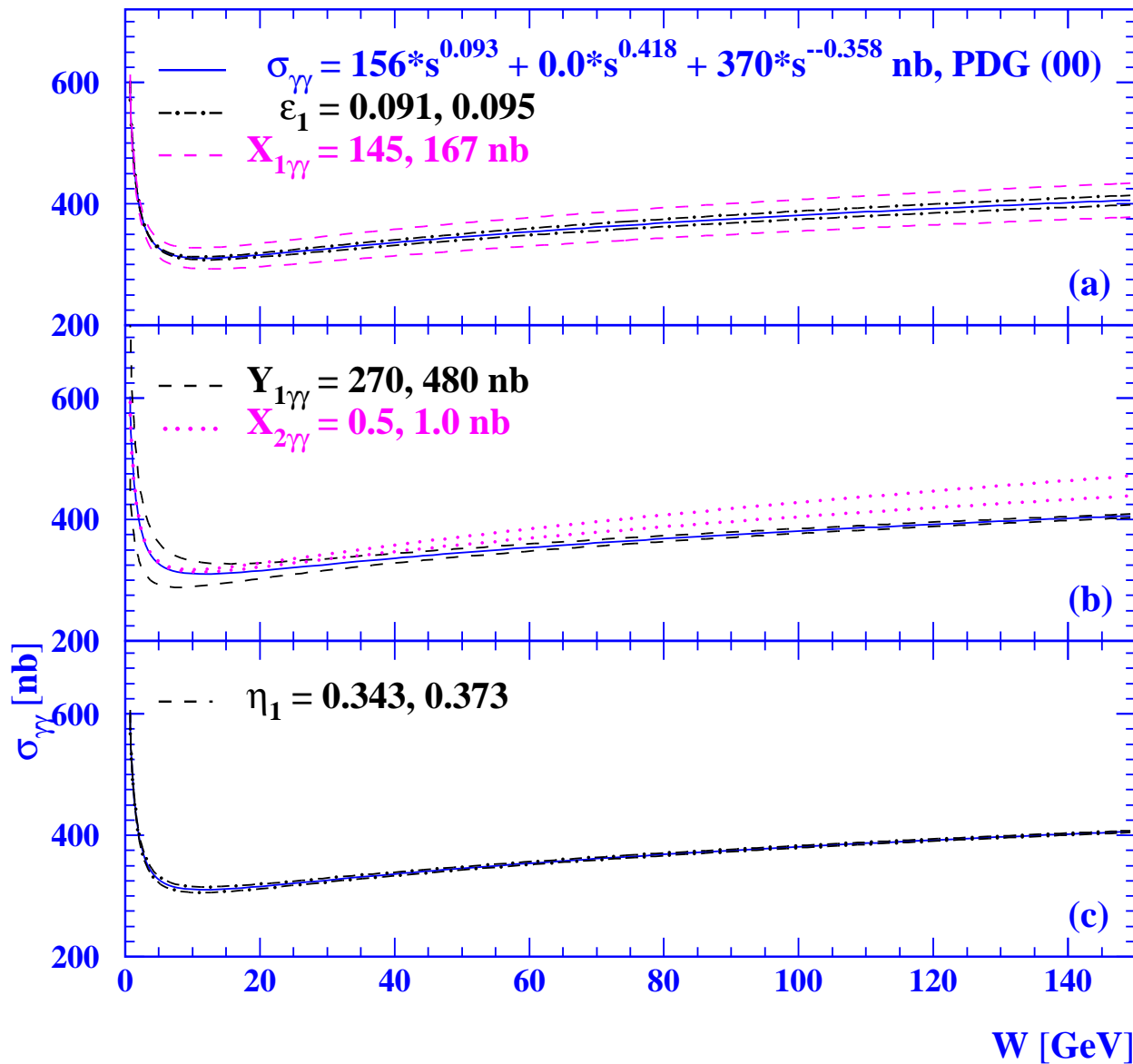
# $W$ distributions for anti-tagged events



The acceptance for diffractive events is very different for the PHOJET and PYTHIA models.

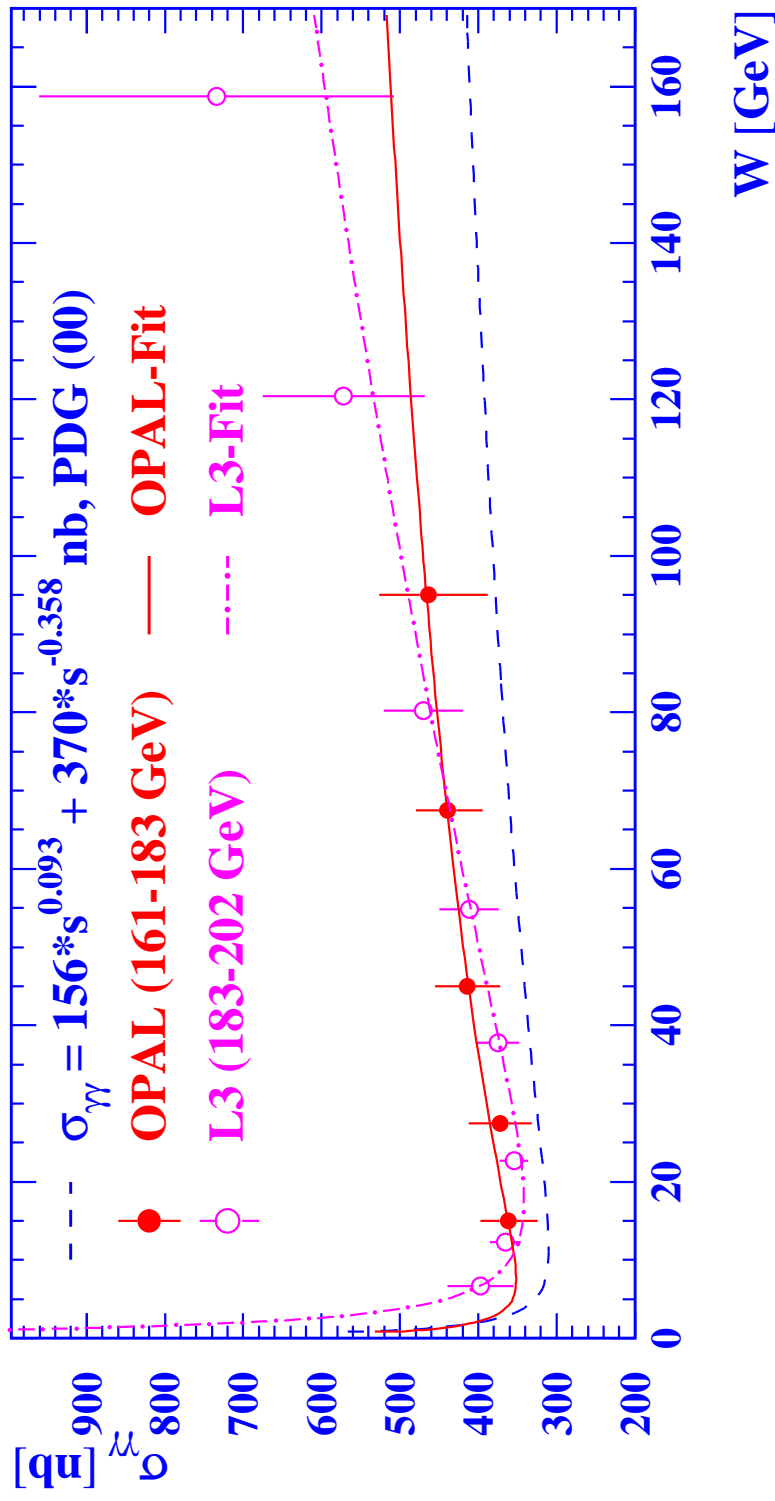


# The total hadronic cross-section $\sigma_{\gamma\gamma}$ from PDG(00)



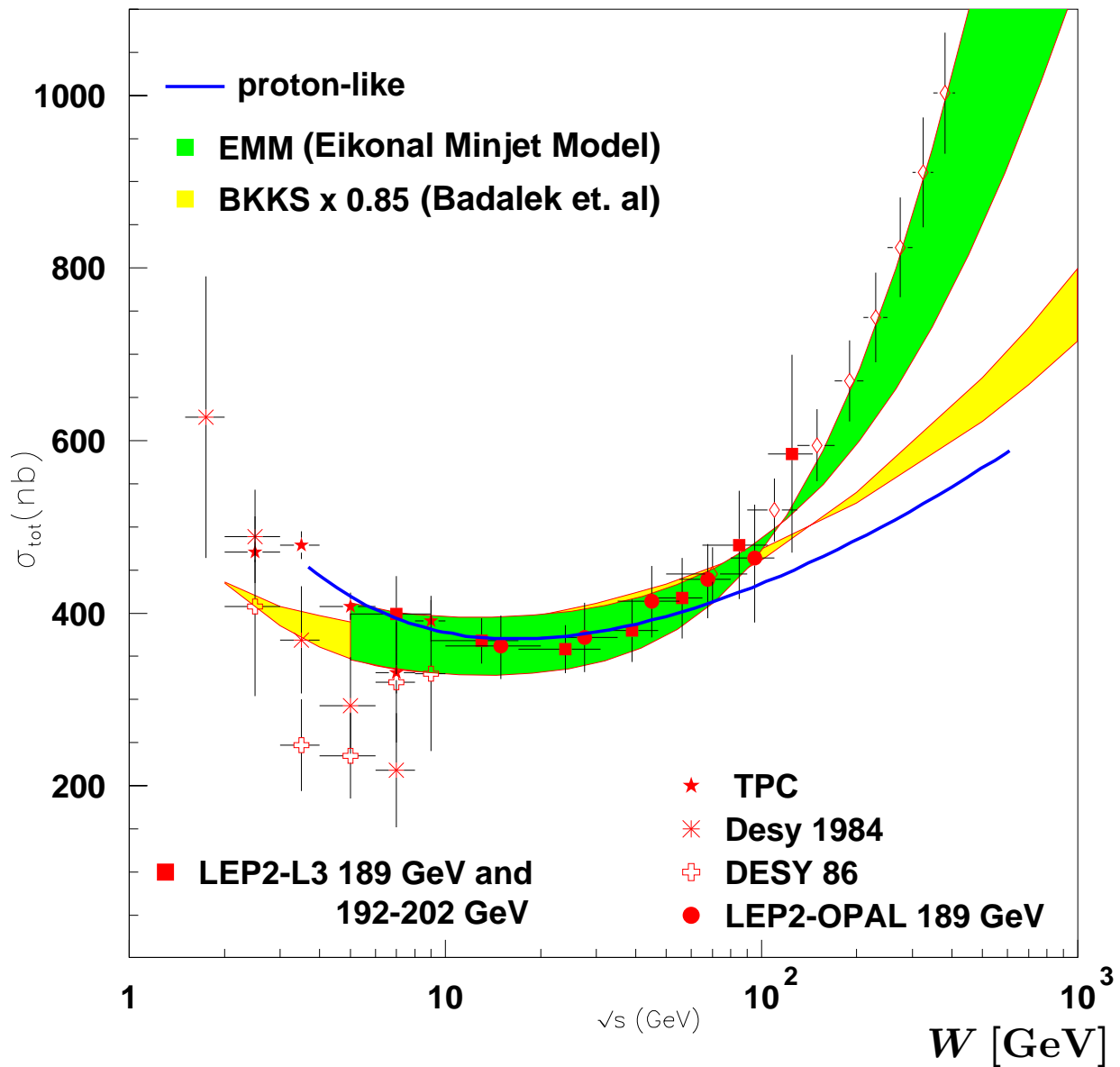
The parameters are strongly correlated.

# The total hadronic cross-section $\sigma_{\gamma\gamma}$



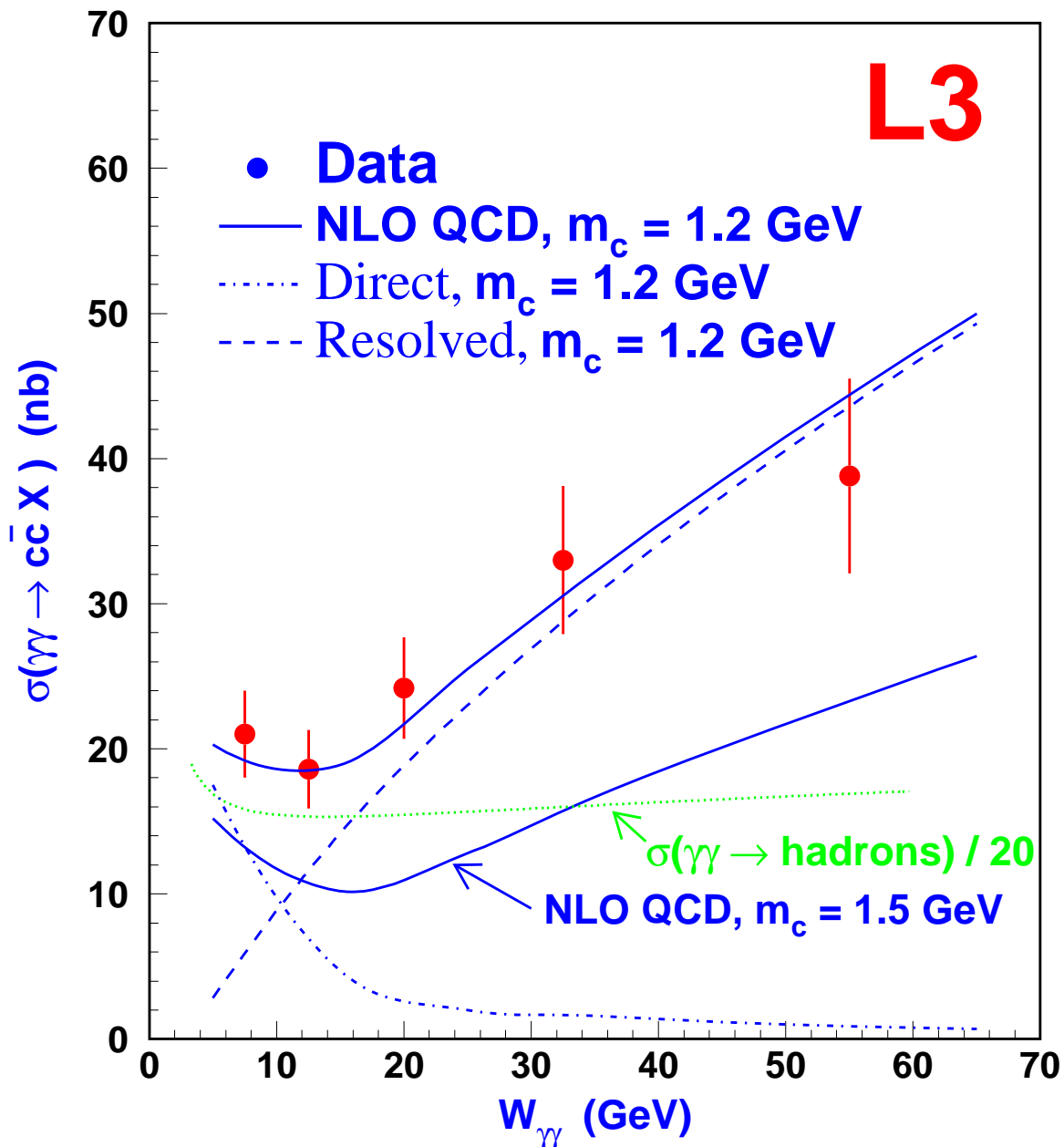
A clear rise of the total cross-section is observed in the data.

# Predictions for the cross-section $\sigma_{\gamma\gamma}$



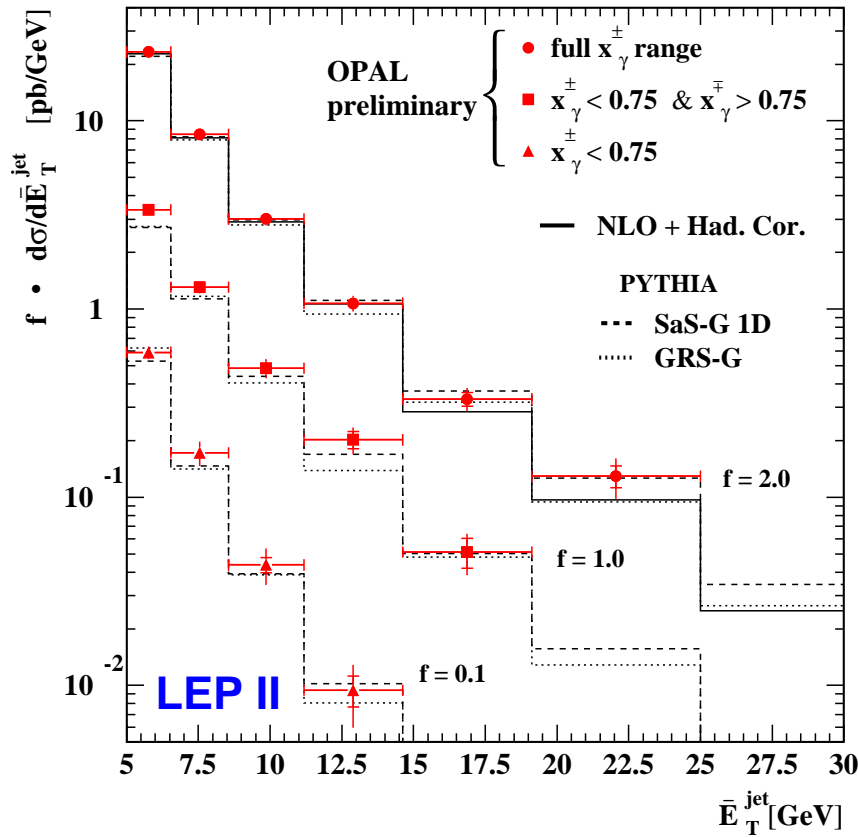
To achieve a 5-10% precision on  $W$  a Photon Collider is needed to avoid the reconstruction of  $W$  from the hadronic final state.

# The rise of the charm cross-section as a function of $W$

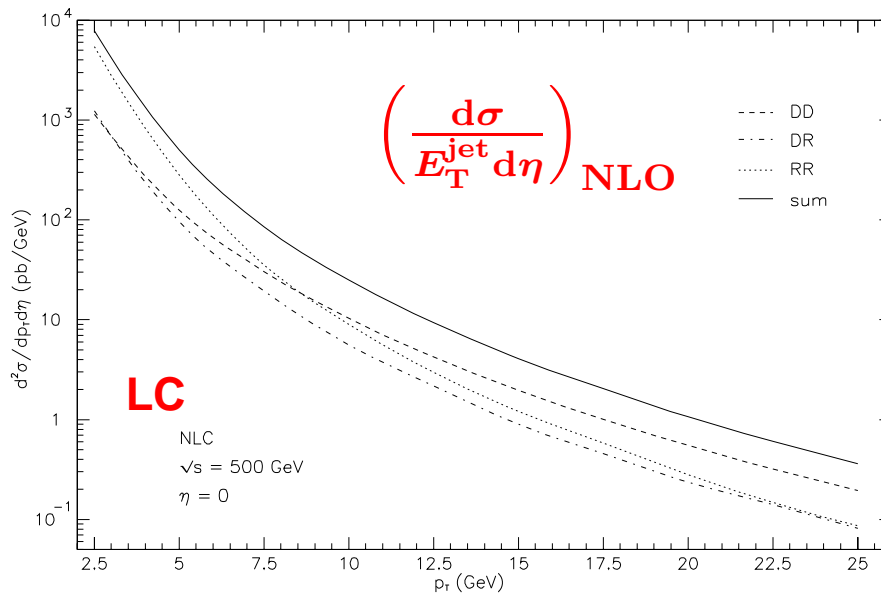


The charm cross-section rises faster than the total hadronic cross-section.

# The inclusive jet cross-sections

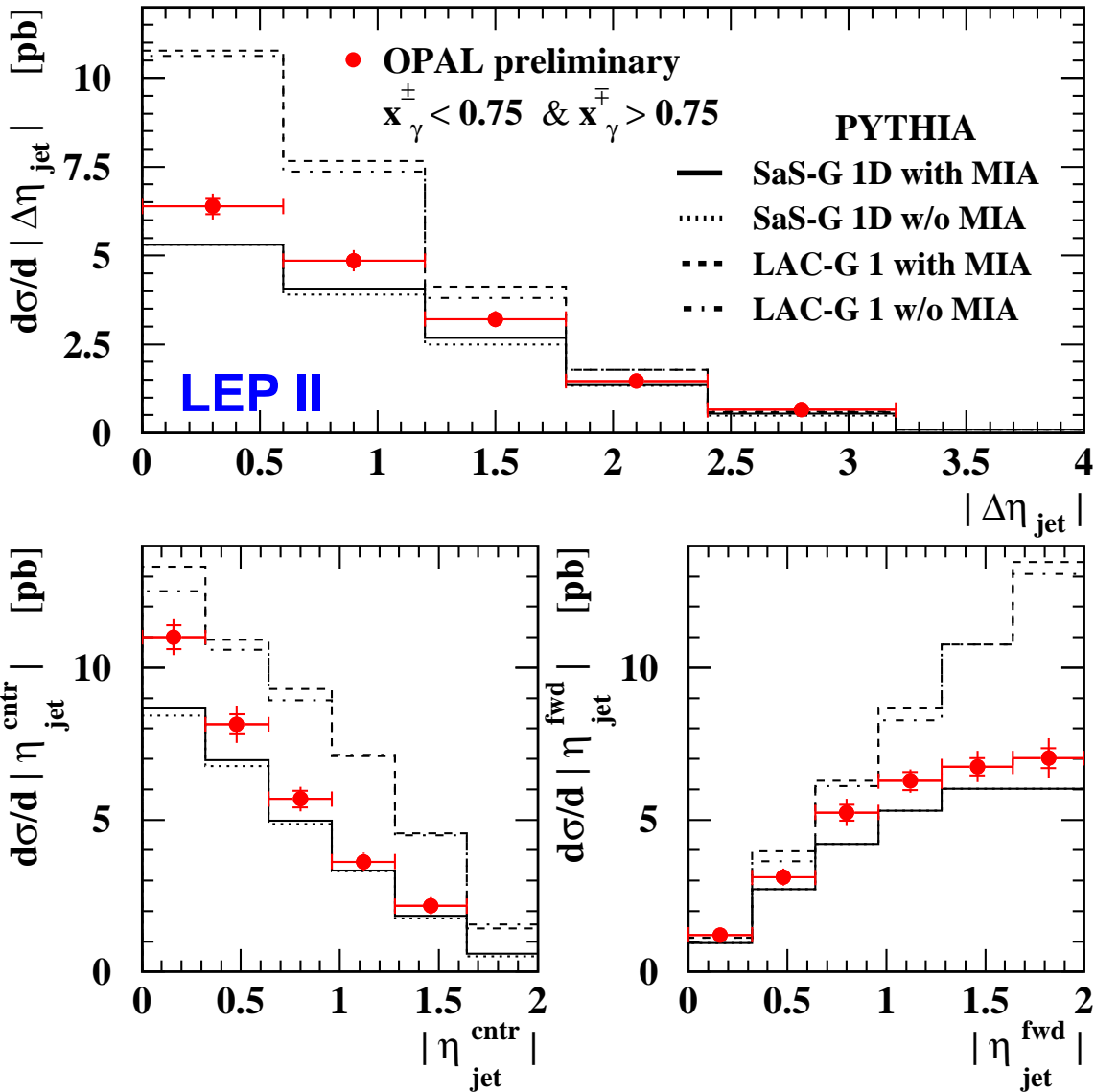


$$x_\gamma^\pm = \frac{\sum_{\text{jets}} (E \pm p_z)}{\sum_{\text{had}} (E \pm p_z)}$$



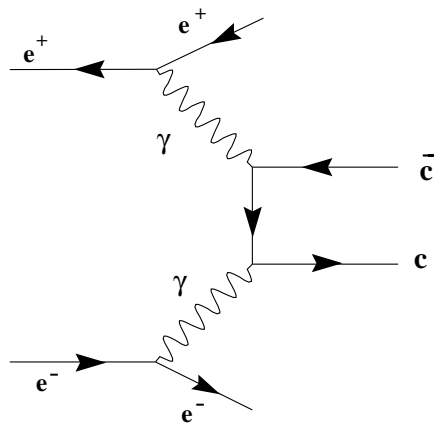
The measurement will be extended to larger  $E_T^{\text{jet}}$

# The sensitivity to parton densities

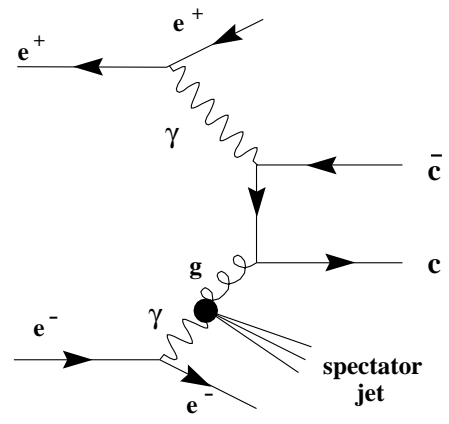


- 1) The gluon density  $f_{g/\gamma}$  in the photon can be constrained.
- 2) The simulation of hadronic final states must be improved.

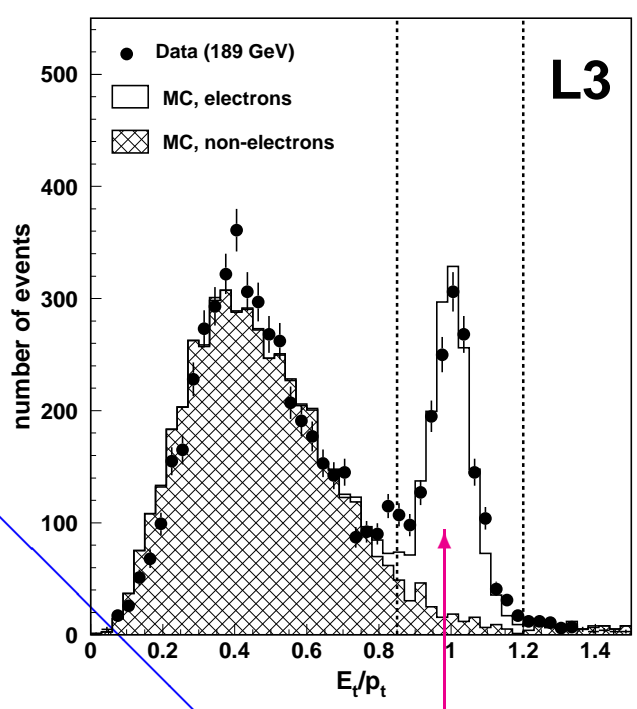
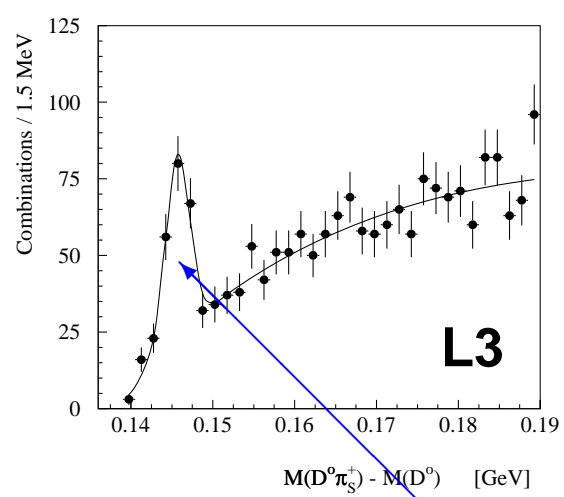
# Inclusive charm production



Direct



Single Resolved

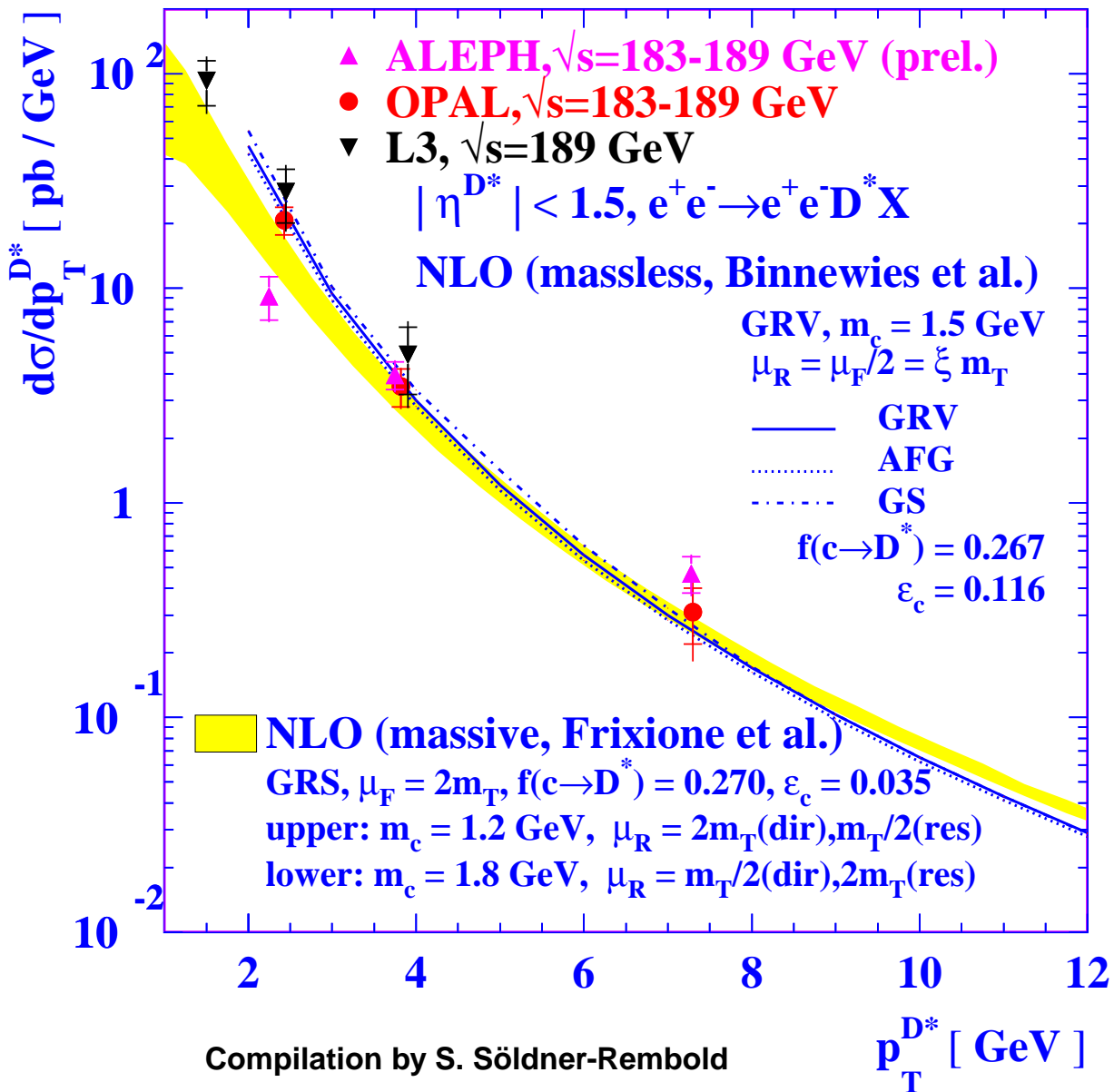


$$D^* \rightarrow D^0 \pi$$

$$D^0 \rightarrow K \pi, K \pi^0, K \pi \pi \pi$$

Clean charm tags can be obtained using leptons from the semileptonic decays or  $D^*$  mesons.

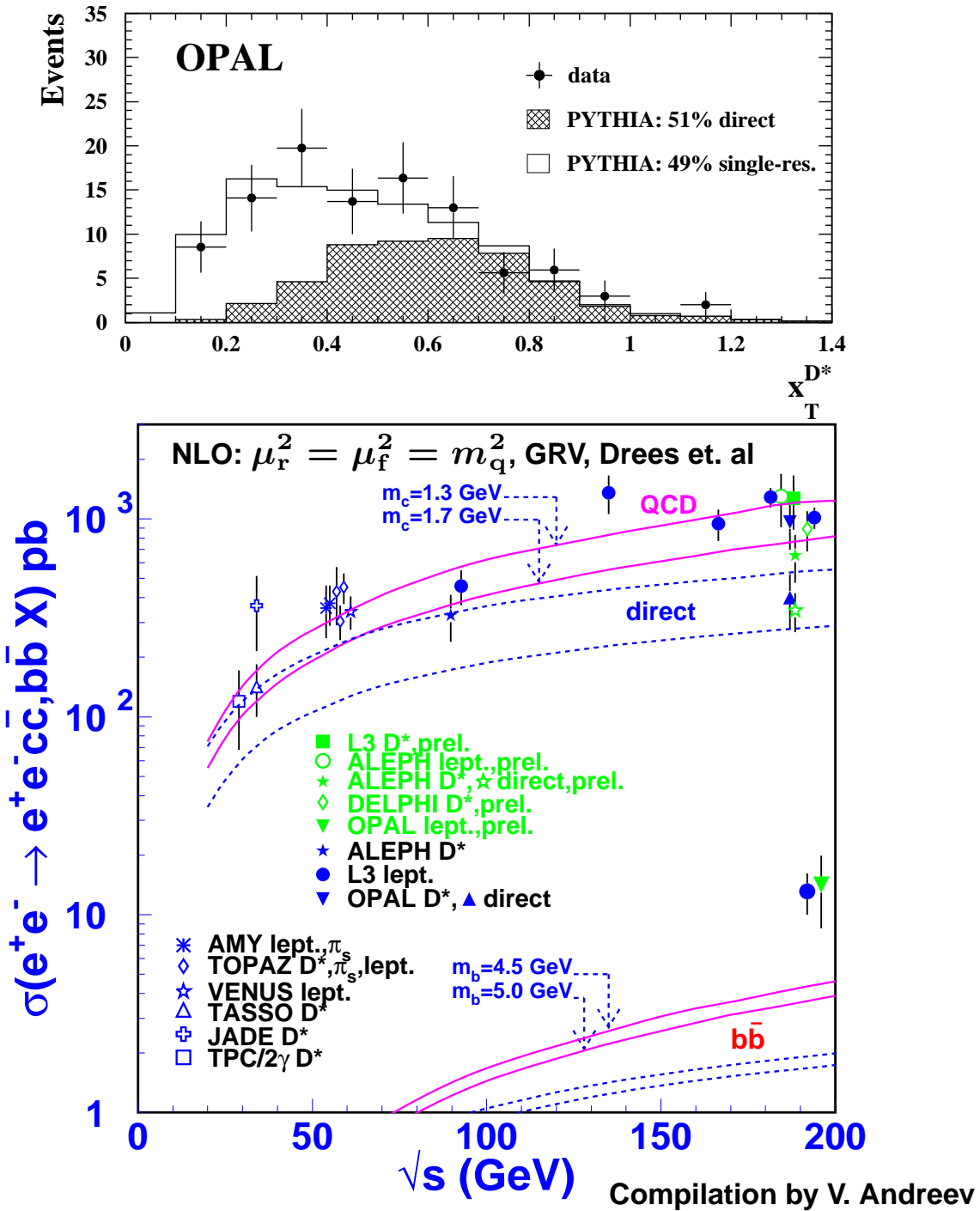
# Differential $D^*$ cross-section



For  $p_T^{D^*} \geq 3$  GeV the data agree well and they are satisfactorily described by the NLO QCD calculations.

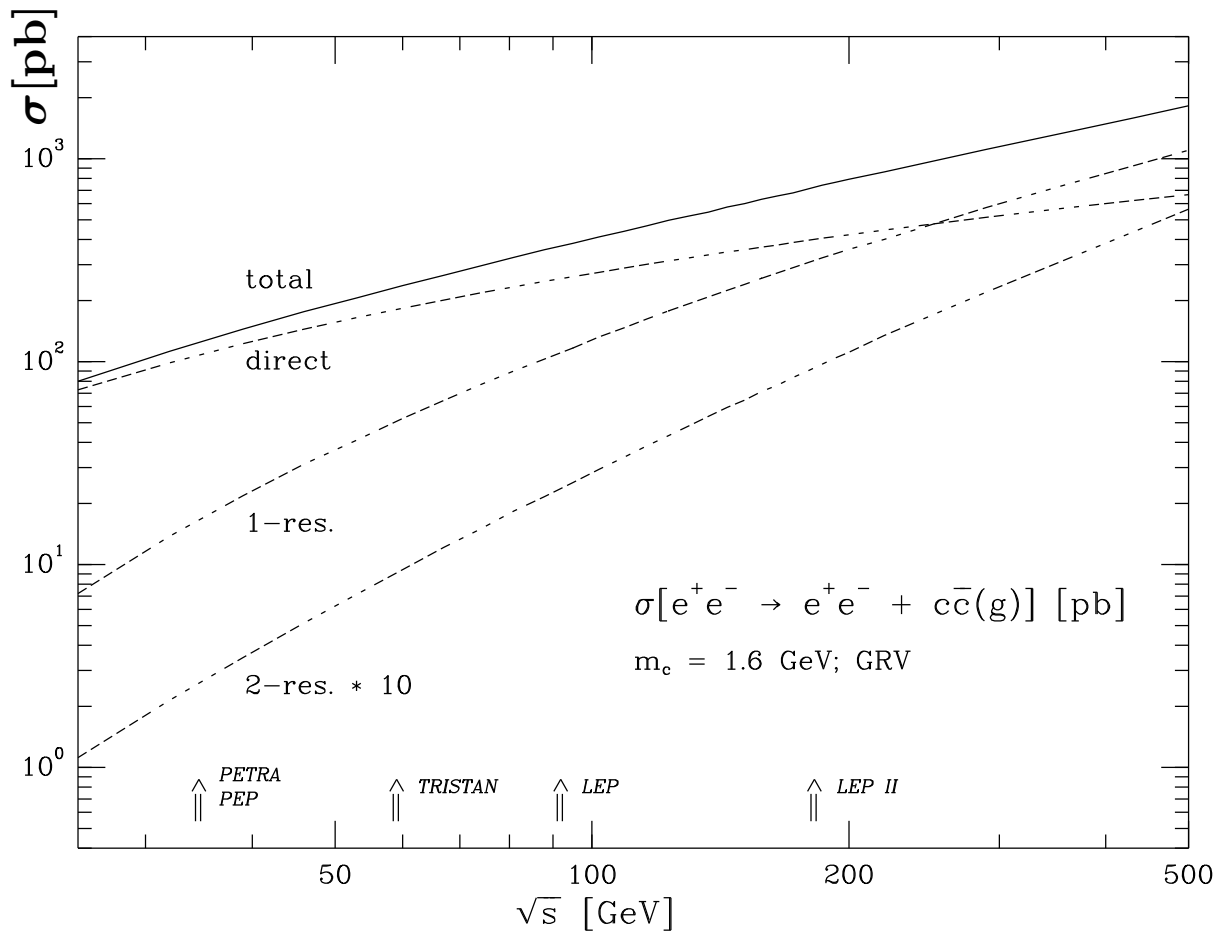


# The heavy quark cross-sections



The direct production of charm quarks is insufficient.

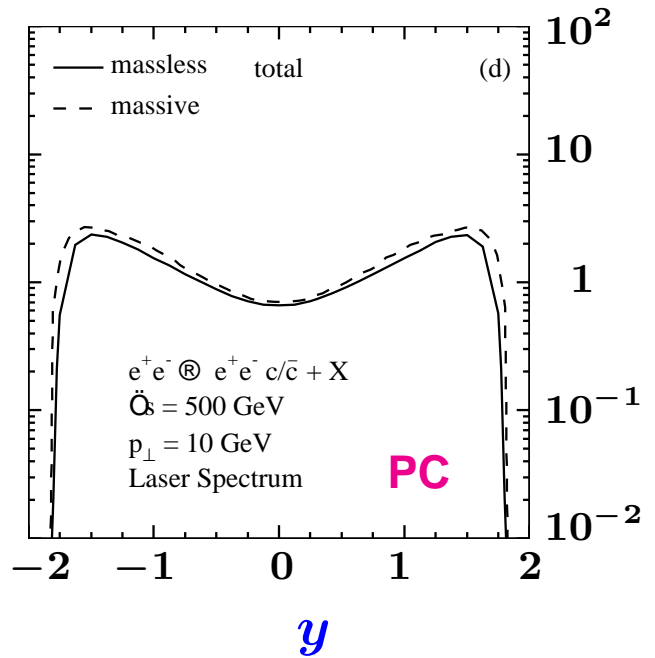
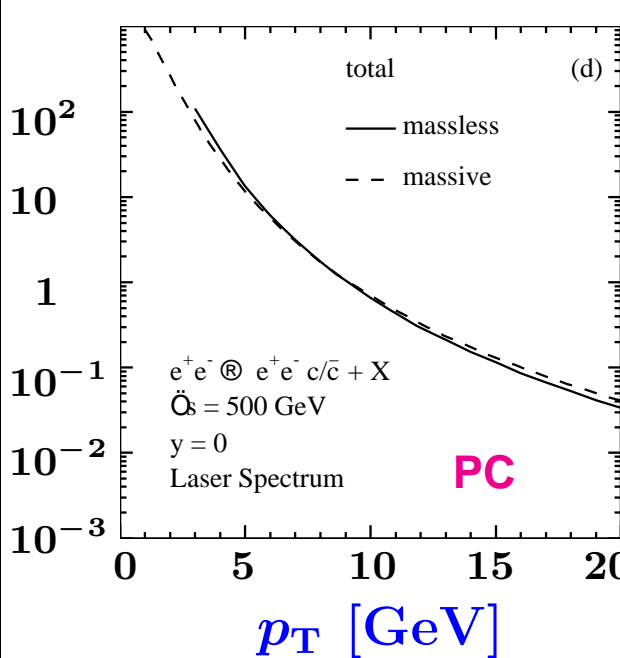
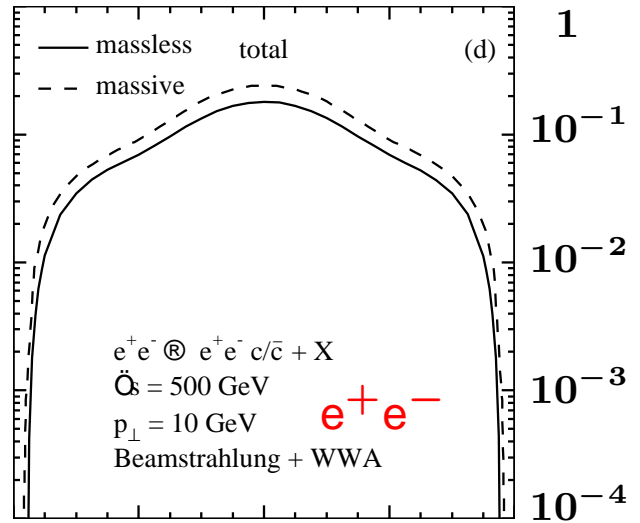
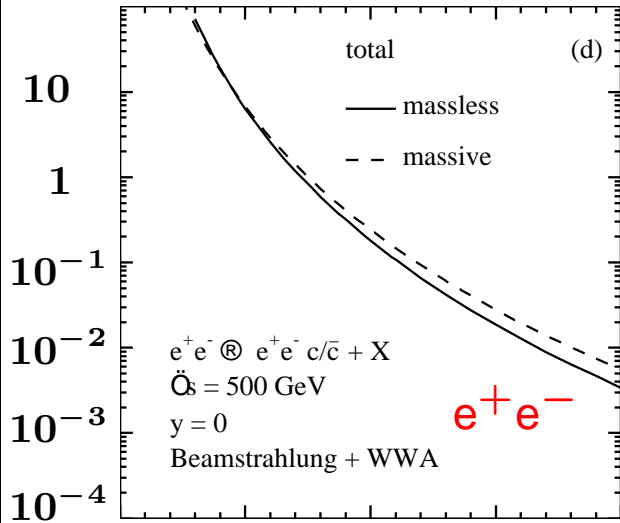
# Charm cross-section in $\gamma\gamma$



1. The calculation for the direct, 1-res (NLO) and 2-res (LO) contributions are based on the EPA.
2.  $\mu^2 = m_c^2/2$ ,  $m_c = 1.6$  GeV,  $W > 3.8$  GeV.
3. One expects about  $10^7$   $c\bar{c}$  events/year.
4. The direct process is a pure QCD prediction with  $\sigma = f(m_c, \alpha_s)$ .

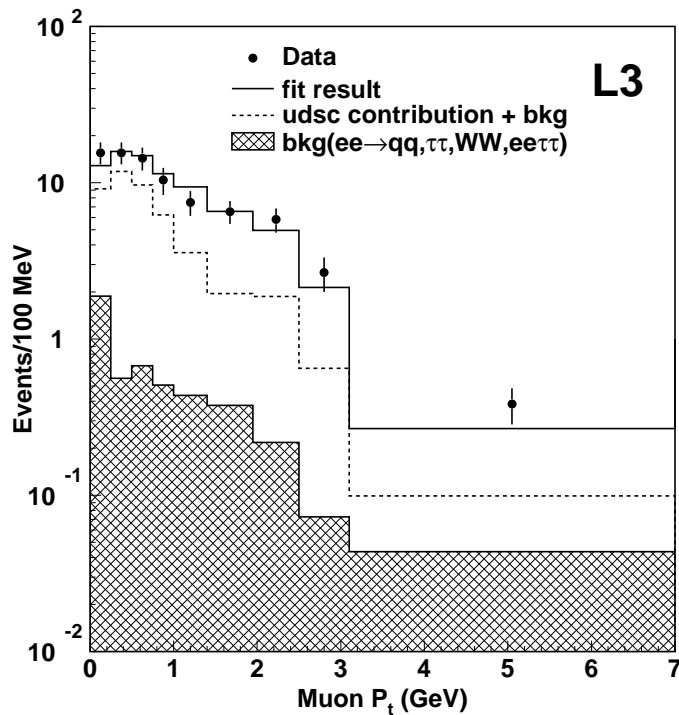
# Charm production in $\gamma\gamma$

$$\frac{d^2\sigma}{dydp_T^2} \left[ \frac{\text{pb}}{\text{GeV}^2} \right]$$



The NLO calculation uses the EPA integrated up to  $\theta_{\text{tag}} = 175 \text{ mrad}$  and  $m_c = 1.5 \text{ GeV}$ .

# Search for bottom production



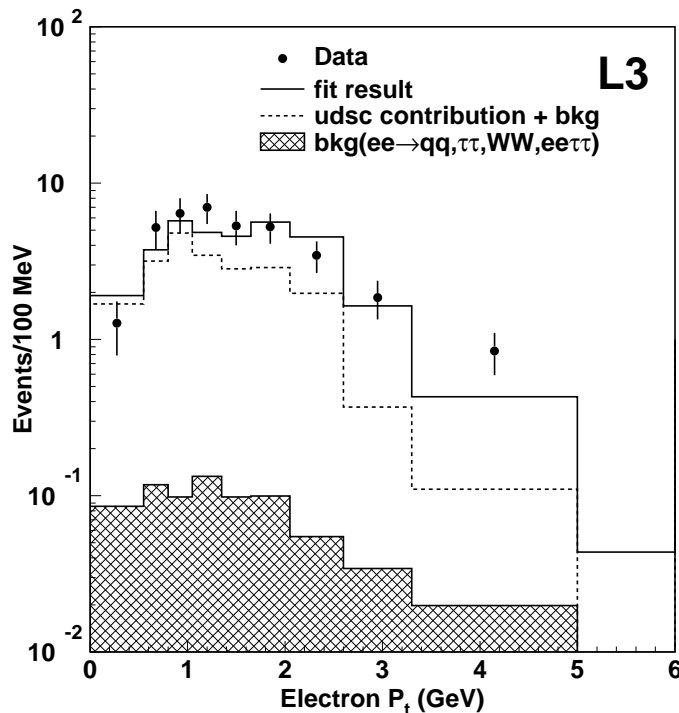
$$p_\mu > 2.0 \text{ GeV}$$

$$|\theta_\mu| < 0.8$$

$$N_{ev} = 269$$

$$\epsilon_b = 2.2\%$$

$$f_b = 52 \pm 10\%$$



$$p_e > 2 \text{ GeV},$$

$$|\theta_e| < 0.725$$

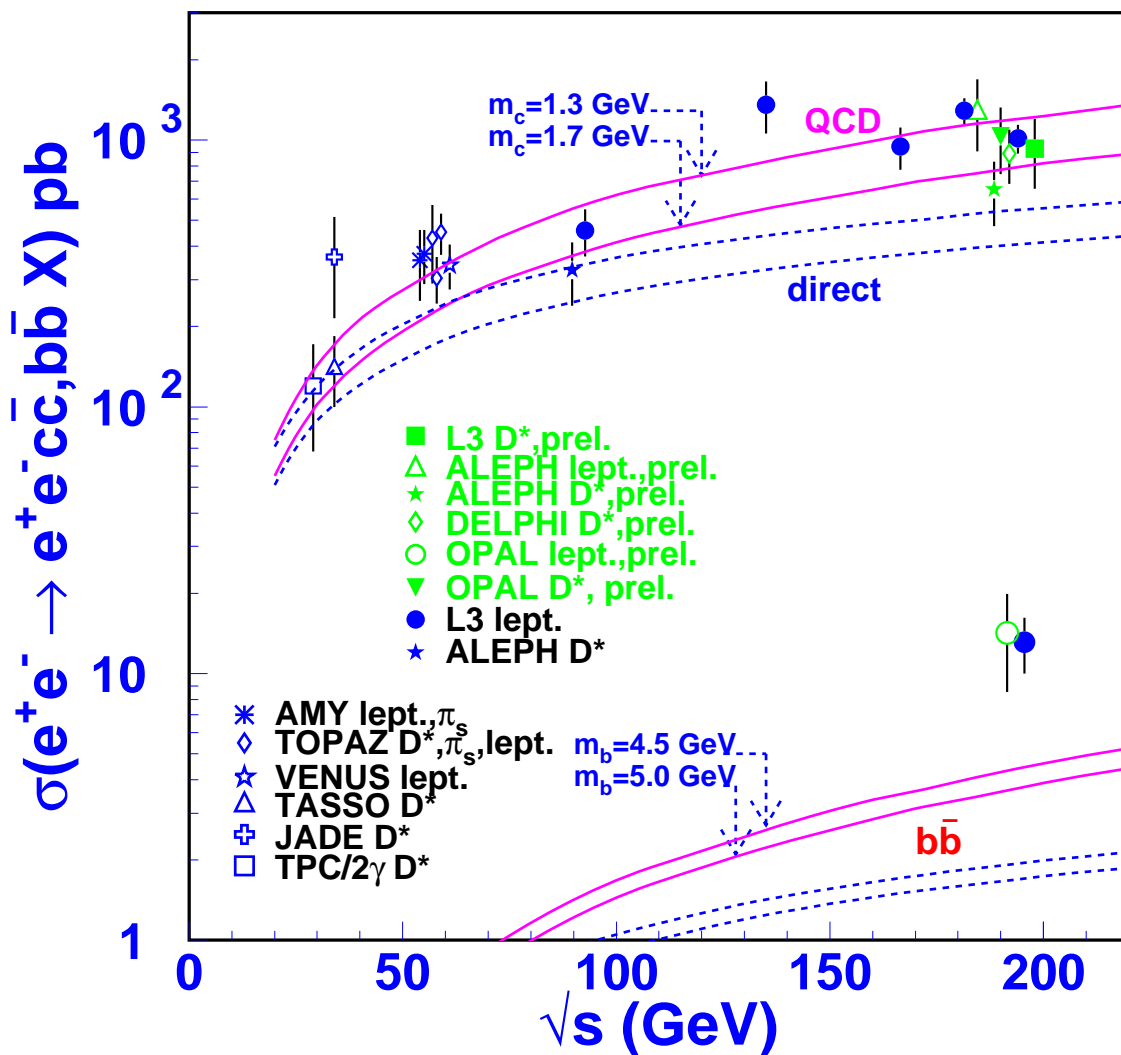
$$N_{ev} = 137$$

$$\epsilon_b = 1.25\%$$

$$f_b = 42 \pm 11\%$$

Look at  $p_t$  of the lepton with respect to the nearest jet to tag bottom production.

# The LEP results on bottom production



$\mu$  tag:  $\sigma_{b\bar{b}}^\mu = 14.9 \pm 2.8(\text{stat}) \pm 2.6(\text{sys})$  pb

$e$  tag:  $\sigma_{b\bar{b}}^e = 10.9 \pm 2.9(\text{stat}) \pm 2.0(\text{sys})$  pb

L3:  $\sigma_{b\bar{b}} = 13.1 \pm 2.0(\text{stat}) \pm 2.4(\text{sys})$  pb

OPAL( $\mu$ ) prel.:  $\sigma_{b\bar{b}} = 14.2 \pm 2.5(\text{stat}) \begin{matrix} +5.3 \\ -4.8 \end{matrix}(\text{sys})$  pb

**The NLO QCD prediction falls short by  $4\sigma$ !**

## The limit of deep inelastic electron-photon scattering

Using:

$$2xF_T^\gamma = \frac{Q^2}{4\pi^2\alpha} \sigma_{TT}(x, Q^2)$$

$$F_L^\gamma = \frac{Q^2}{4\pi^2\alpha} \sigma_{LT}(x, Q^2)$$

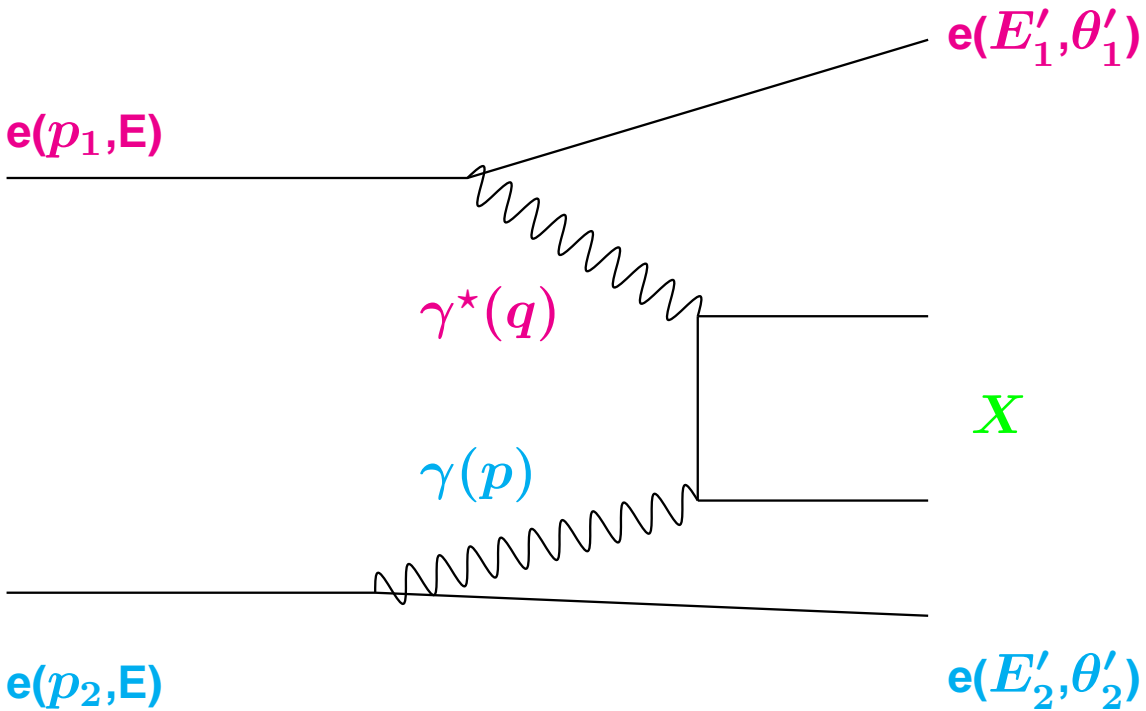
$$F_2^\gamma = 2xF_T^\gamma + F_L^\gamma$$

and the limit  $(p \cdot q)^2 - Q^2 P^2 \approx (p \cdot q)^2$  the cross section reduces to:

$$\frac{d^4\sigma}{dx dQ^2 dz dP^2} = \frac{d^2 N_\gamma^T}{dz dP^2} \cdot \frac{2\pi\alpha^2}{x Q^4} \cdot [1 + (1-y)^2] \cdot \underbrace{\left[ 2xF_T^\gamma(x, Q^2) + \frac{2(1-y)}{1+(1-y)^2} F_L^\gamma(x, Q^2) \right]}_{\rightarrow F_2^\gamma \text{ for } y \ll 1}$$

$$\text{with: } \frac{d^2 N_\gamma^T}{dz dP^2} = \frac{\alpha}{2\pi} \left[ \frac{1+(1-z)^2}{z} - \frac{1}{P^2} - \frac{2m_e^2 z}{P^4} \right]$$

# Electron-photon scattering



$$\frac{d^4\sigma}{dx dQ^2 dz dP^2} \propto \frac{d^2 N_\gamma^T}{dz dP^2} \cdot \frac{2\pi\alpha^2}{x Q^4} \cdot f_y \cdot F_2^\gamma(x, Q^2)$$

with:  $f_y = 1 + (1 - y)^2$

$$Q^2 = -q^2 = 2 E E'_1 (1 - \cos \theta'_1)$$

$$x = \frac{Q^2}{Q^2 + W^2 + P^2}$$

$$P^2 = -p^2 = 2 E E'_2 (1 - \cos \theta'_2) \ll Q^2$$

$$\frac{d^2 N_\gamma^T}{dz dP^2} = \frac{\alpha}{2\pi} \left[ \frac{1 + (1 - z)^2}{z} \frac{1}{P^2} - \frac{2 m_e^2 z}{P^4} \right]$$

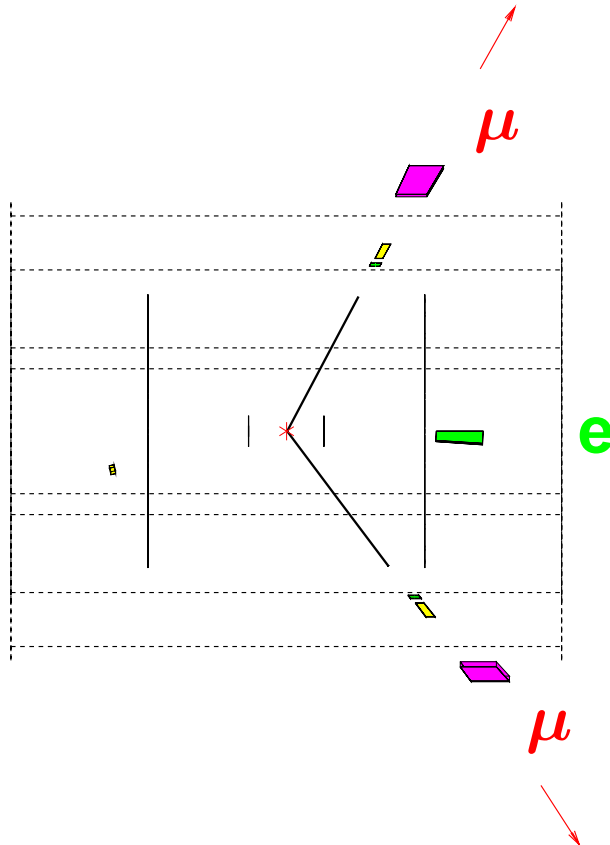
# The muon pair final state

```
Run:event 5198:229277 Date 940625 Time 211645 Ctrk(N= 2 Sump= 7.3) Ecal(N= 3 SumE= 1.4) Hcal(N= 4 SumE= 3.3)
Ebeam 45.62 Evis 10.5 Emiss 80.7 Vtx ( -0.02, 0.04, 0.47) Muon(N= 2) Sec Vtx(N= 0) Fdet(N= 0 SumE= 0.0)
Bz=4.029 Bunchlet 1/1 Thrust=0.8469 Aplan=0.0012 Oblat=0.4878 Spher=0.4109
```



## Event type bits

```
4 Low mult presel
12 Tagged two phot
22 S phot muon veto
32 "Phys1" selection
1 Z0 type physics
```

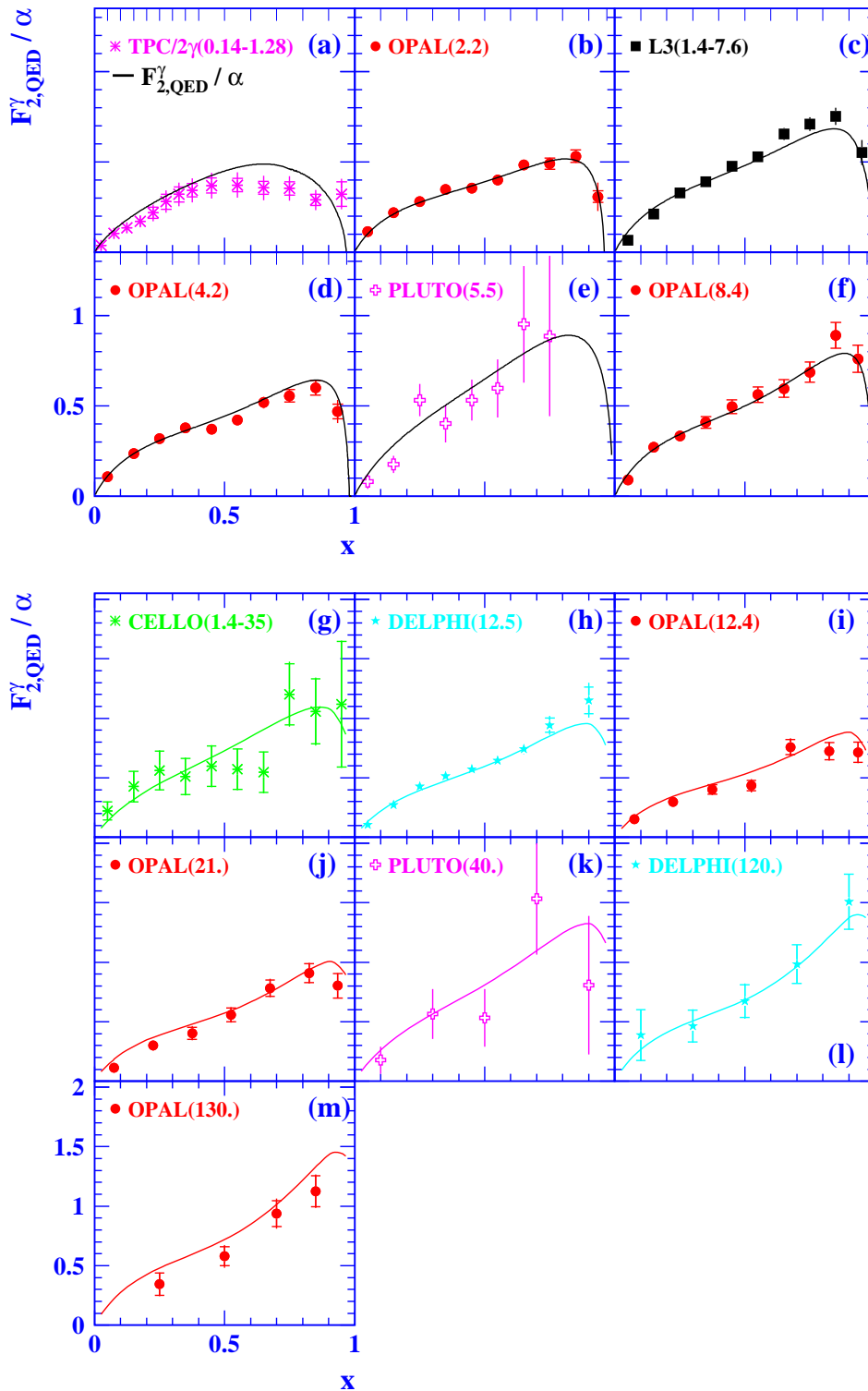


Centre of screen is ( 0.0000, 0.0000, 0.0000)      200. cm.      510 20 50 GeV

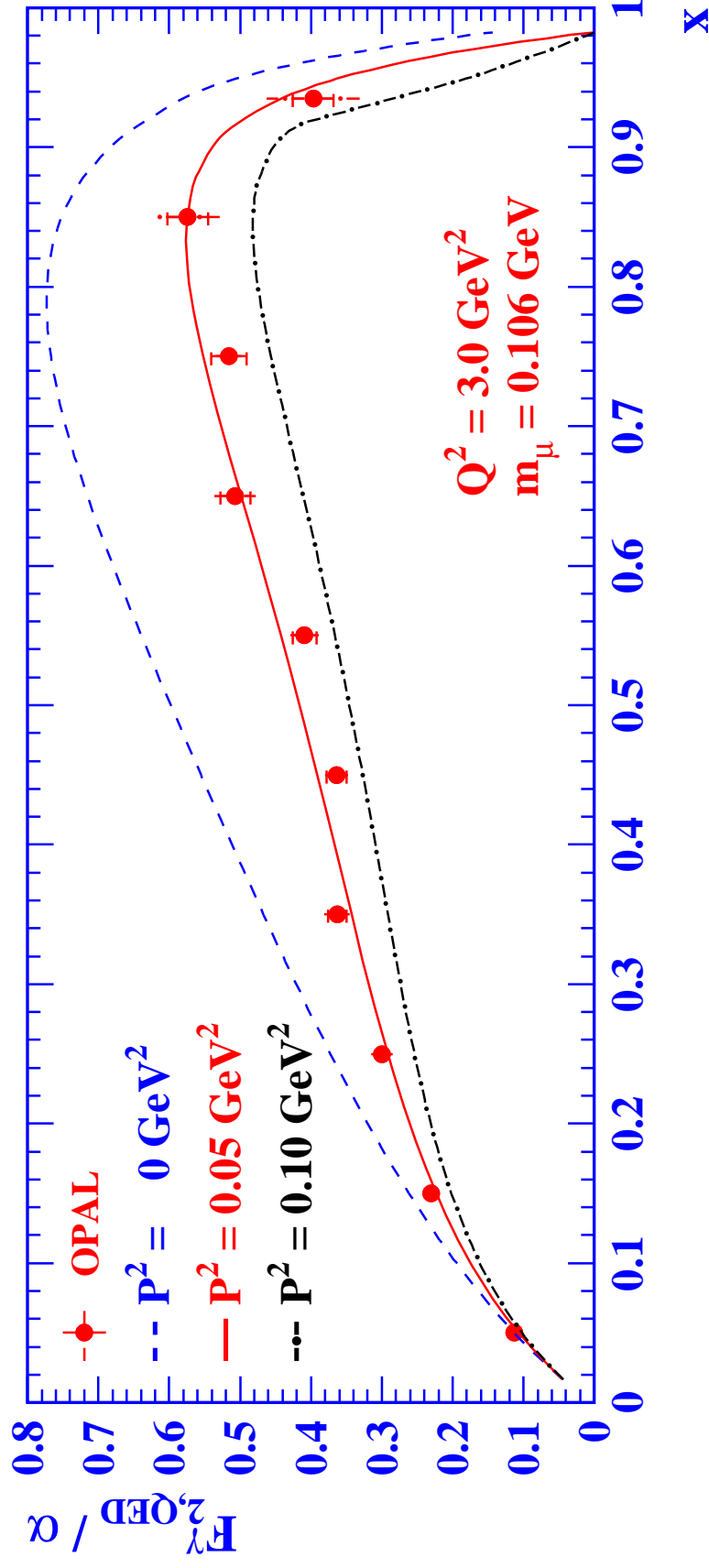
**The muon pair final state is a clear topology with good mass resolution.**



# The world data on $F_{2,QED}^\gamma$

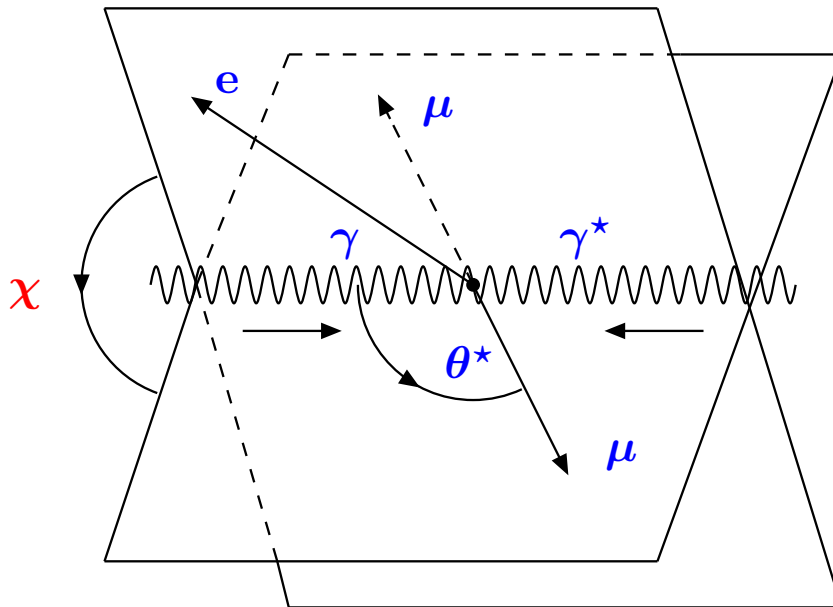


## The $P^2$ dependence of $F_2^\gamma$



The suppression of the photon structure with the photon virtuality  $P^2$  is clearly observed in the data.

## Azimuthal correlations



$$e\gamma \rightarrow e\mu\mu$$

$$d\sigma \propto 1 - \rho(y) F_A^\gamma / F_2^\gamma \cos \chi + \frac{1}{2} \epsilon(y) F_B^\gamma / F_2^\gamma \cos 2\chi$$

$$\epsilon(y) = \frac{2(1-y)}{1+(1-y)^2} \approx 1, \quad \rho(y) = \frac{(2-y)\sqrt{1-y}}{1+(1-y)^2} \approx 1$$

### Helicity structure:

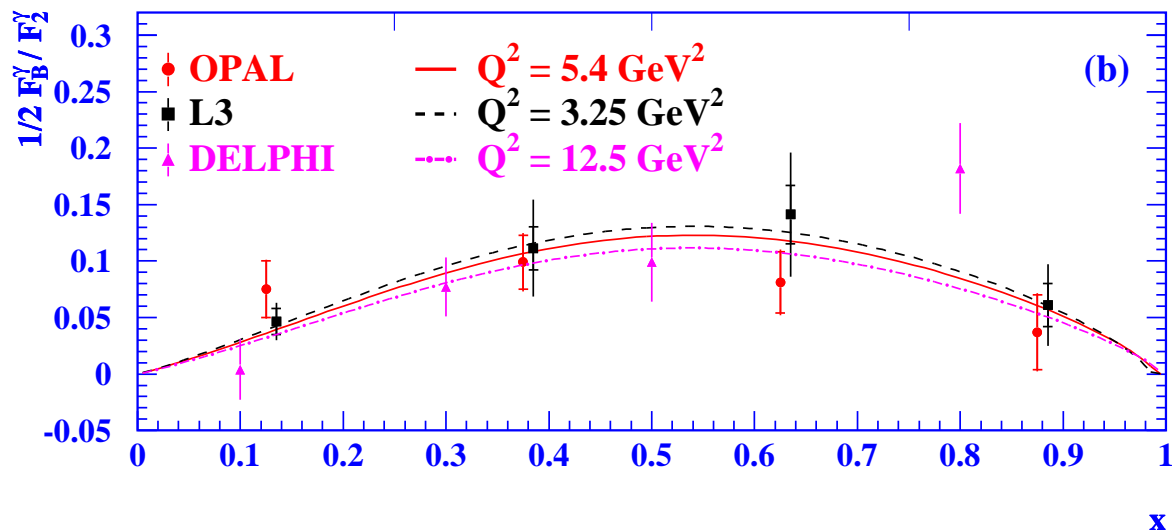
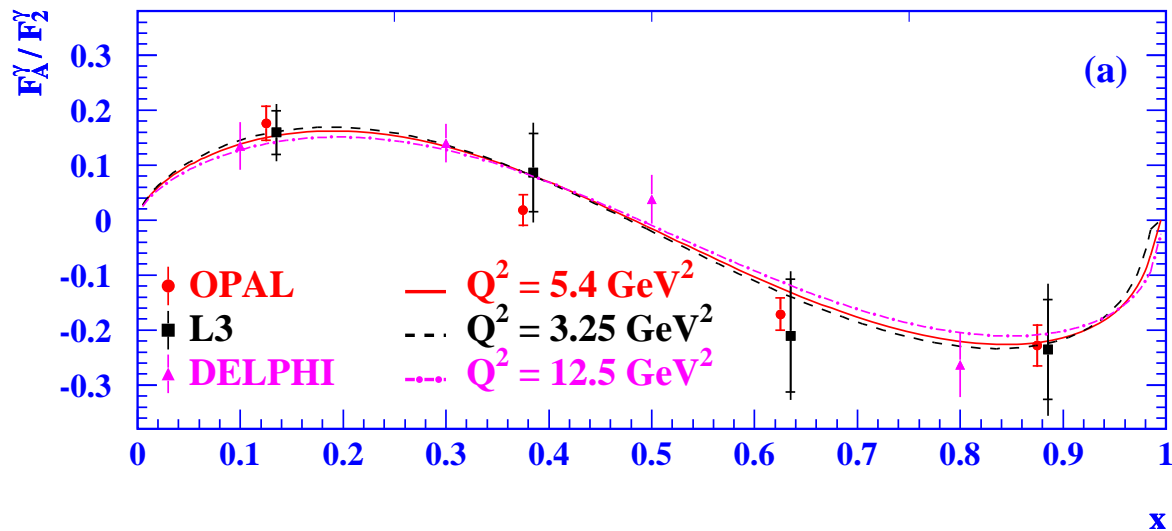
$F_A^\gamma$ : transverse–longitudinal interference

$F_B^\gamma$ : transverse–transverse interference

The  $\chi$  dependence gives access to other structure functions besides  $F_2^\gamma$ .

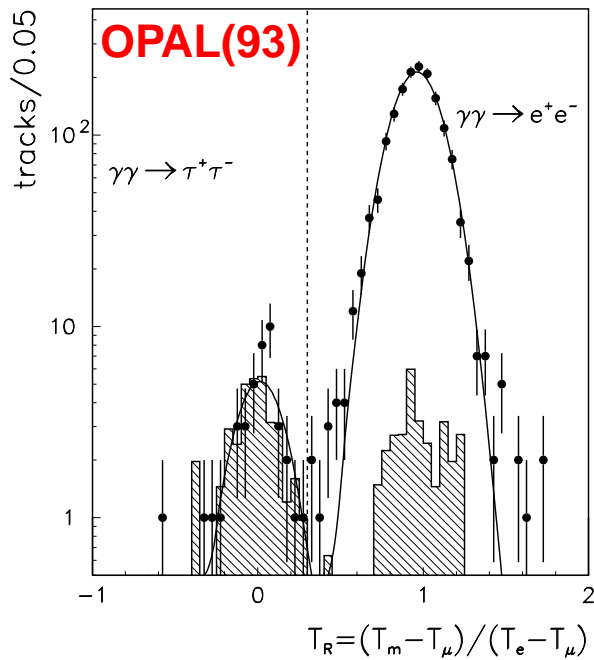
# The structure functions

$$F_A^\gamma \text{ and } F_B^\gamma$$

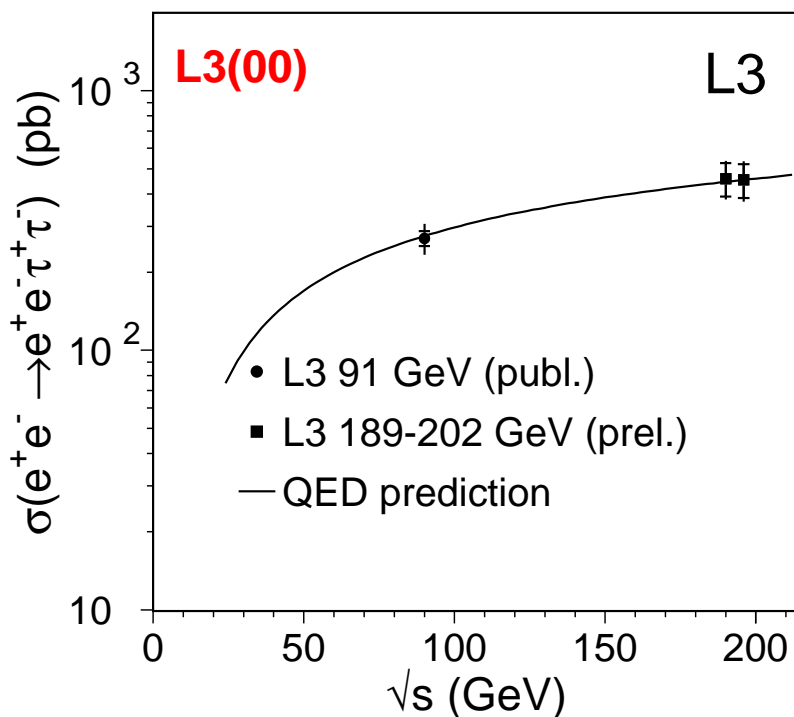


**First measurement that goes further than measuring the differential cross-section and gives more information on the helicity structure of the interaction.**

# Production of tau pairs at LEP



First seen in  $\gamma\gamma^* \rightarrow \tau\tau$   
 $\tau\tau \rightarrow (e\bar{\nu}_e\nu_\tau)(\mu\bar{\nu}_\mu\nu_\tau)$   
 Leptons identified by  $dE/dx$



Cross-section for  
 $\gamma\gamma \rightarrow \tau\tau$  using  
 $\tau\tau$  decays into  
 $(e\bar{\nu}_e\nu_\tau)(\pi\pi^0\nu_\tau)$

**Tau pair production has been measured at LEP.**

# The hadronic final state

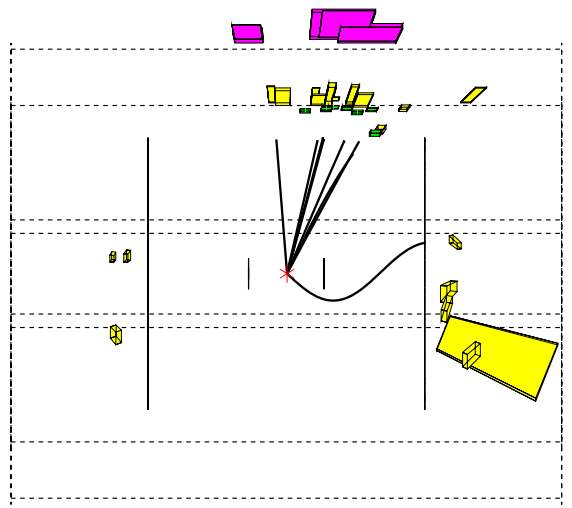
```
Run:event 6422: 47694 Date 950817 Time 155240 Ctrk(N= 8 Sump= 12.4) Ecal(N= 19 SumE= 46.8) Hcal(N= 6 SumE= 3.4)
Ebeam 45.64 Evis 58.0 Emiss 33.3 Vtx ( -0.05, 0.11, 1.11) Muon(N= 0) Sec Vtx(N= 0) Fdet(N= 0 SumE= 0.0)
Bz=4.028 Bunchlet 3/3 Thrust=0.7845 Aplan=0.0006 Oblat=0.4769 Spher=0.0370
```



## Event type bits

- 4 Low mult presele
- 8 Singl phot presele
- 12 Tagged two phot
- 13 Higgs high mult
- 24 S phot EM ass TCF
- 25 S phot EM and TCF
- 26 S phot In-time TCF
- 27 S phot EM clus
- 28 S phot High pT trk
- 30 S phot no H+MU vet
- 31 Long-lived decays
- 32 "Phys1" selection
- 1 Z0 type physics

## hadrons

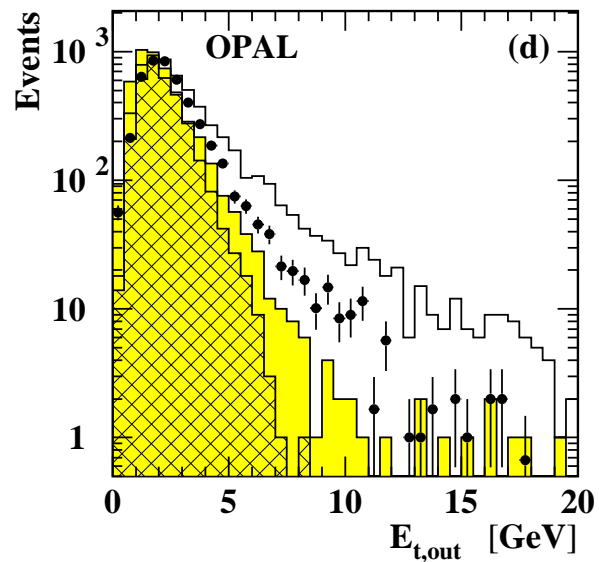
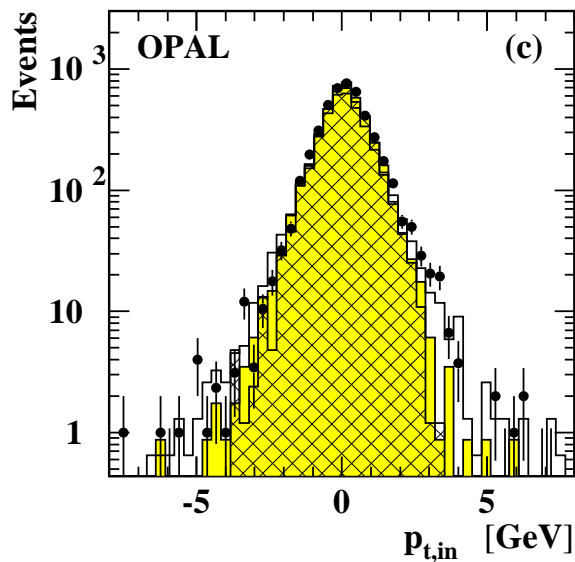
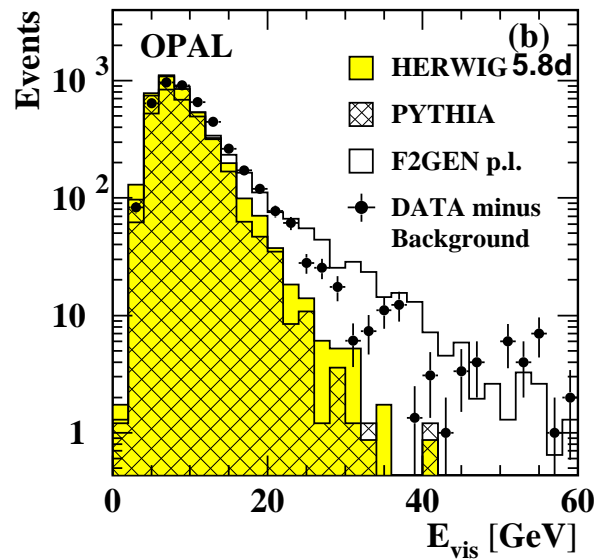
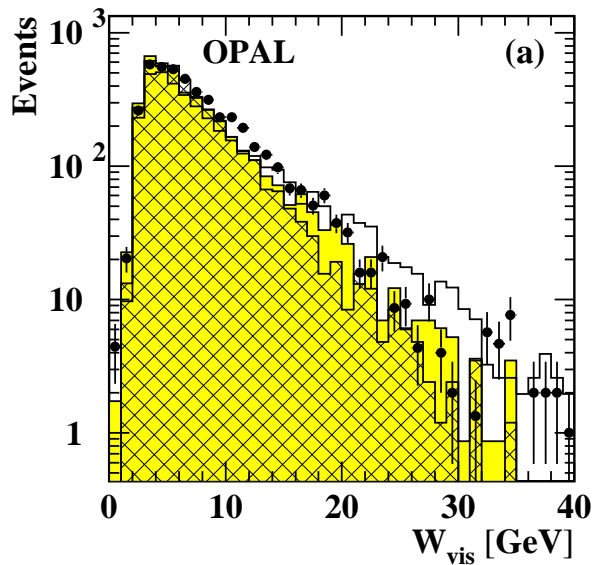


Centre of screen is ( 0.0000, 0.0000, 0.0000)



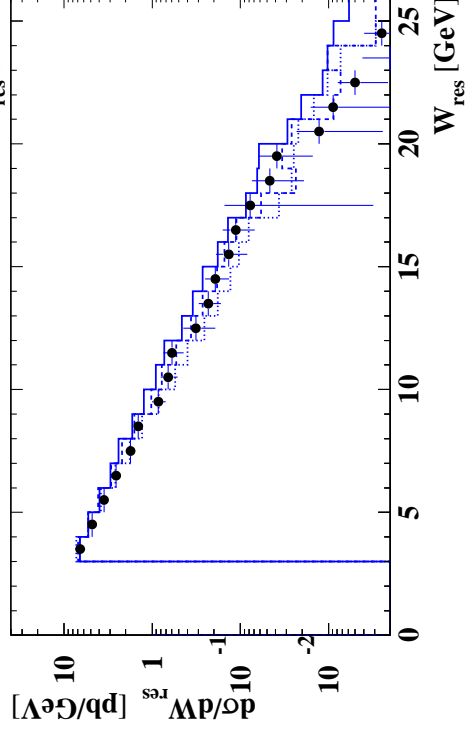
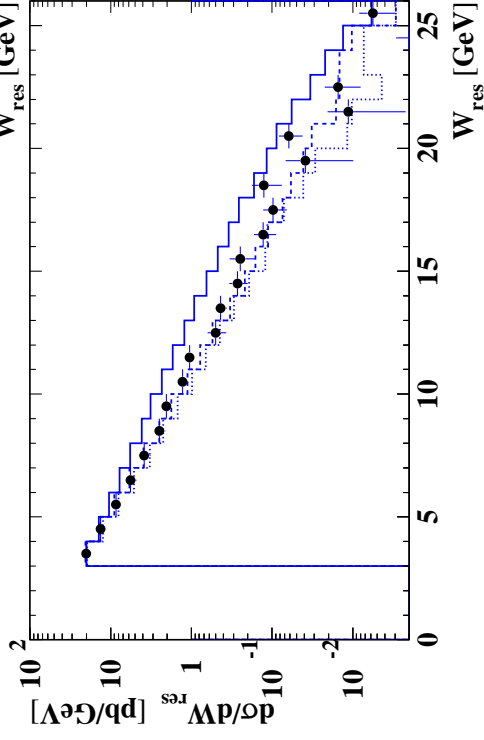
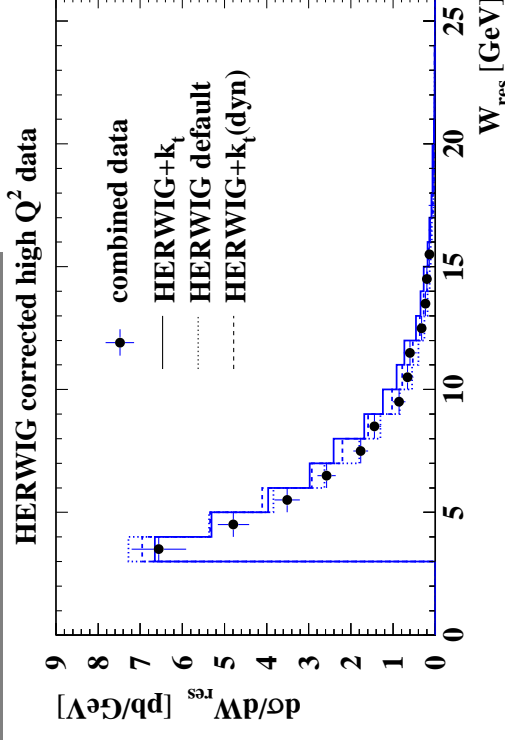
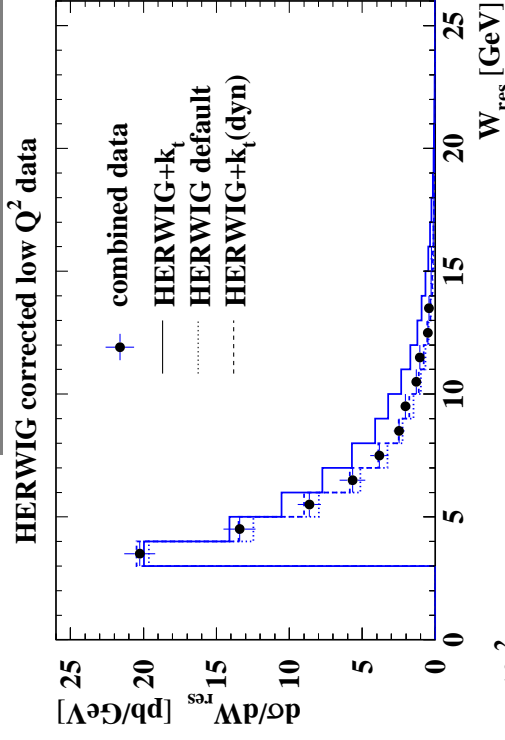
**The scattered electron is clearly visible.  
However, the hadronic final state may partly disappear  
along the beam axis.**

# The description of the hadronic final state



There are significant differences between the data and the Monte Carlo predictions (OPAL '96)

# Comparison to LEP combined data

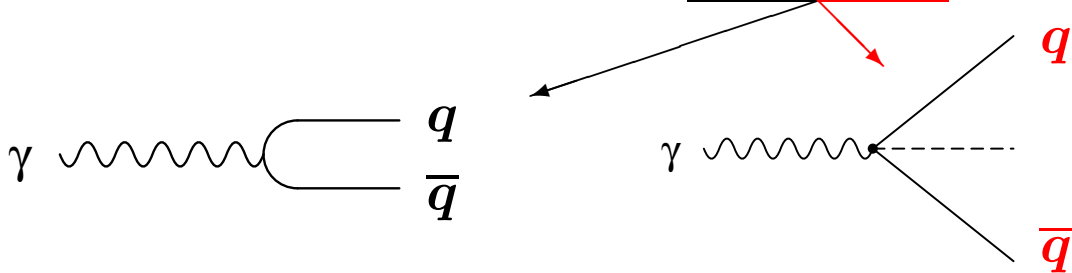


**The combined data are a valuable input to constrain the Monte Carlo models  
(LEP Two-Photon WG CERN-EP-2000-109)**



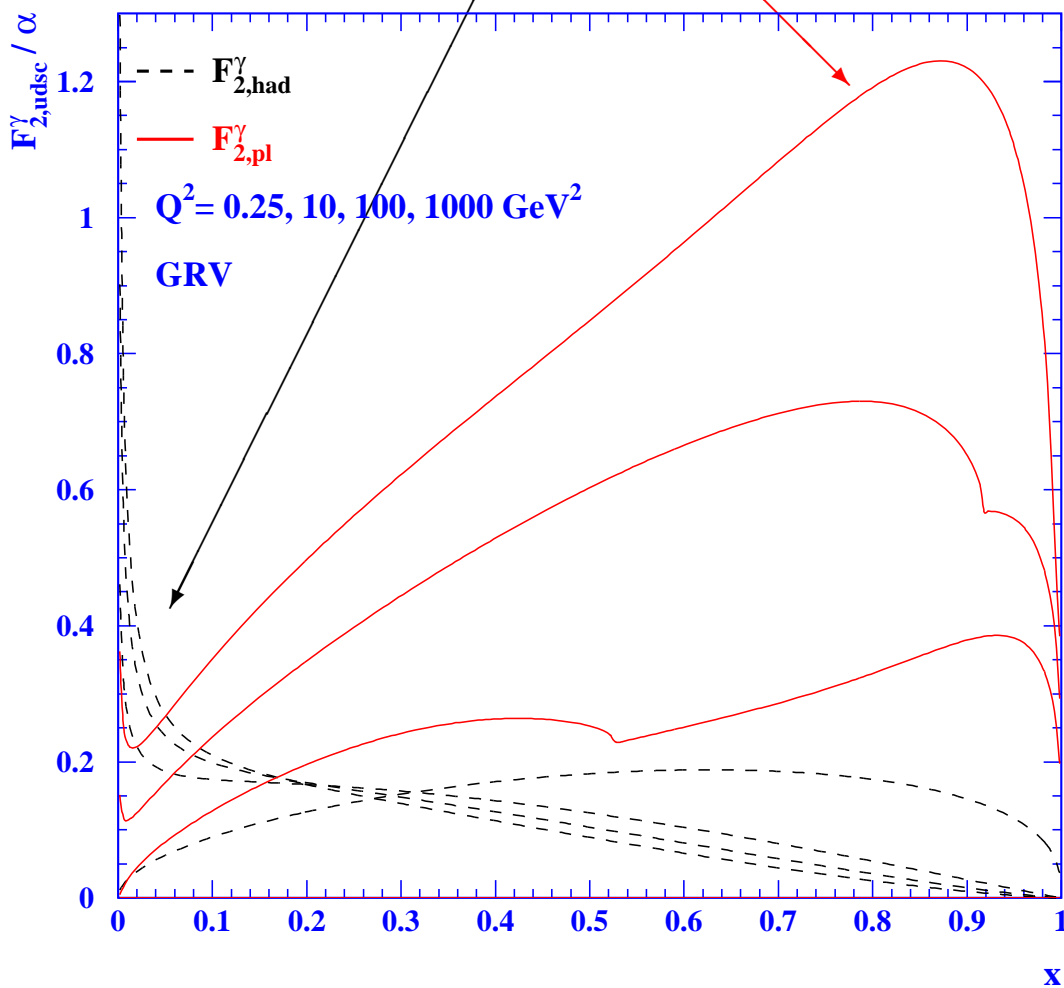
# The contributions to $F_2^\gamma(x, Q^2)$

$$F_2^\gamma(x, Q^2) = x \sum_{c,f} e_q^2 f_{q,\gamma}(x, Q^2)$$

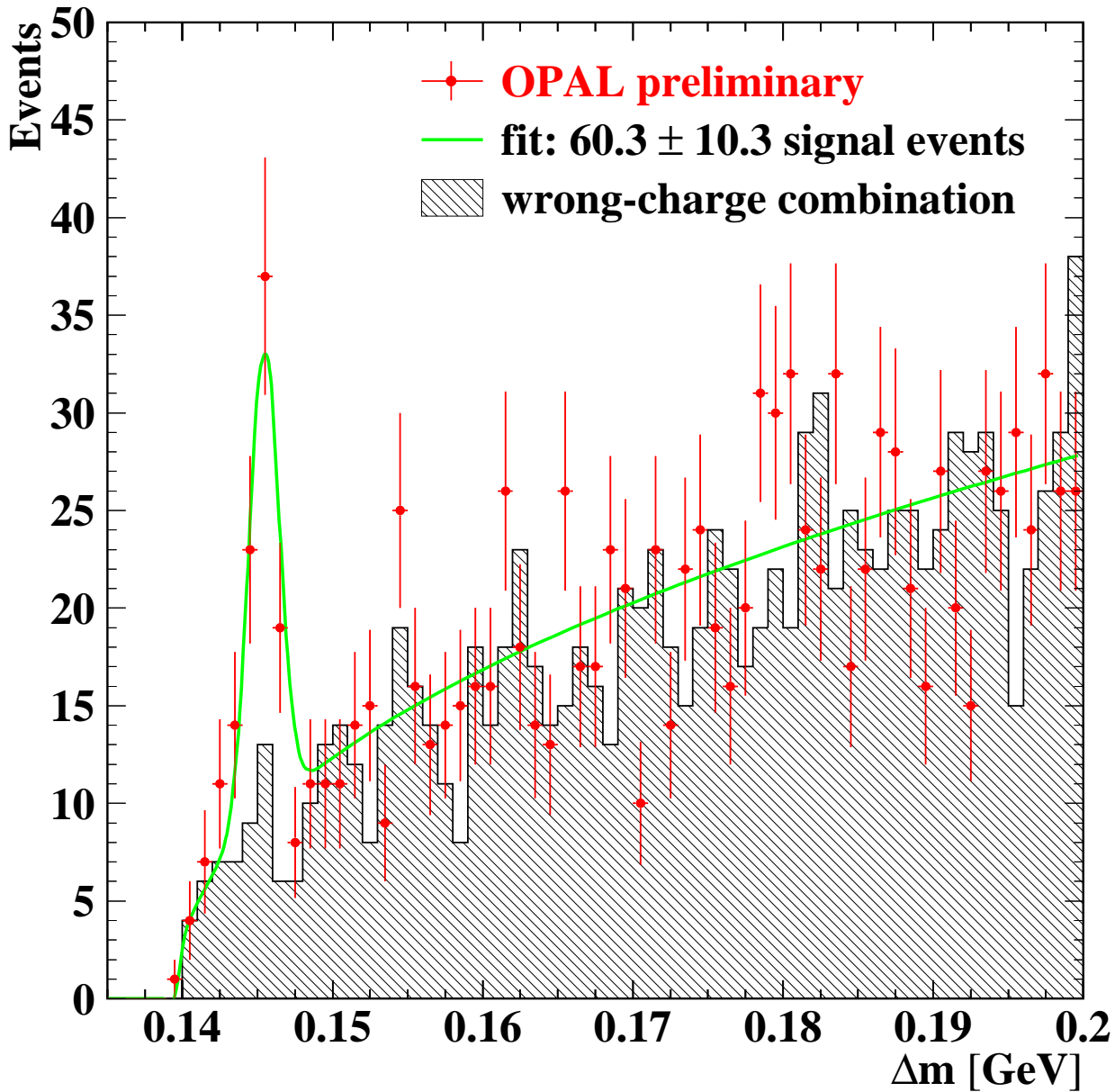


hadron-like, non-perturbative  
e.g. VMD( $\rho, \omega, \phi$ ), low- $x$

point-like, perturbative  
high- $x$

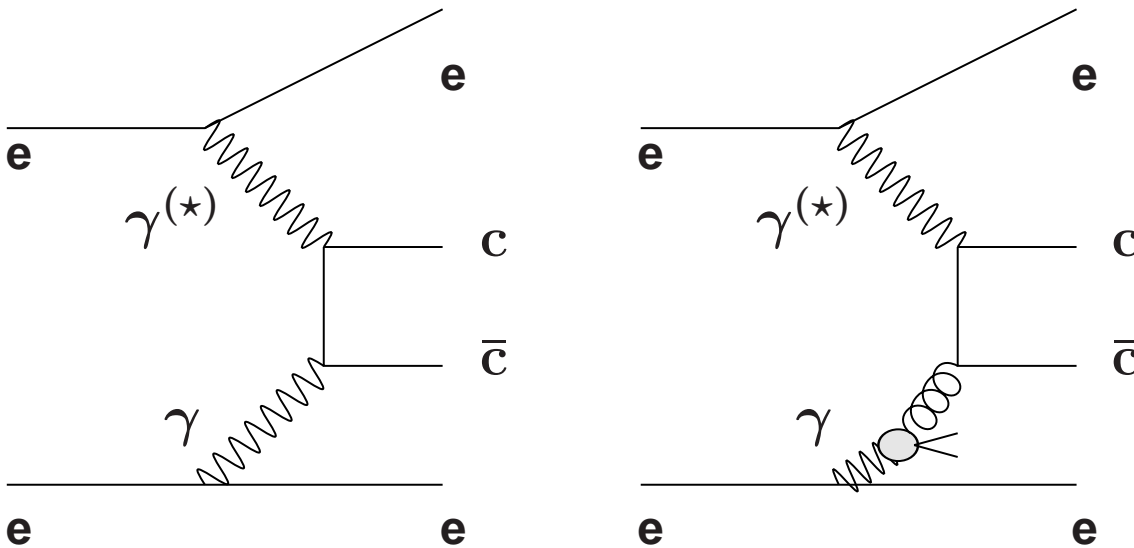


# Charm production tagged by $D^*$ s



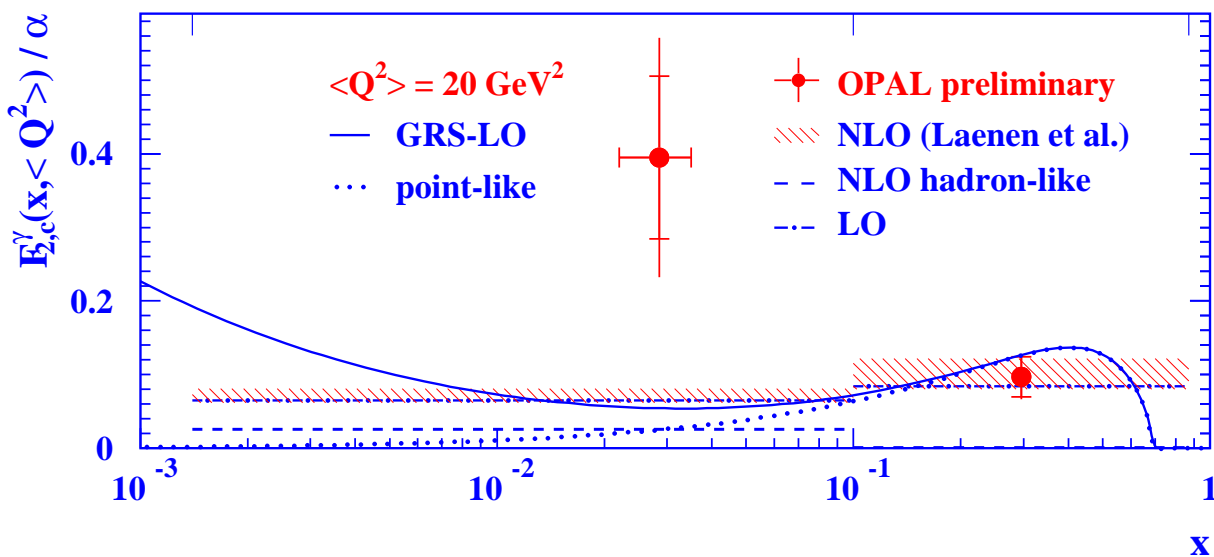
**A clear signal in the  $\Delta m = M(D^*) - M(D^0)$  mass spectrum is seen.**

# The first measurement of $F_{2,c}^\gamma$



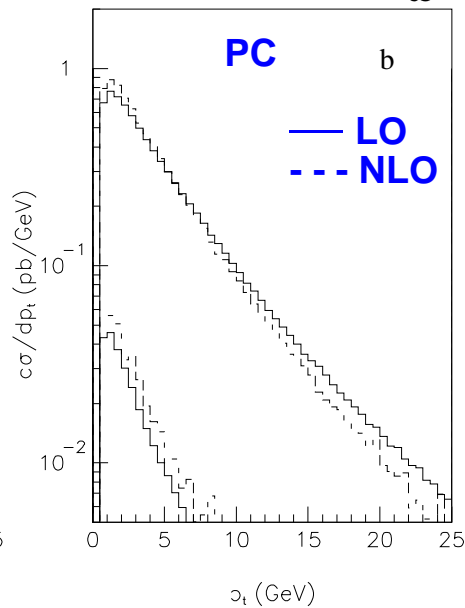
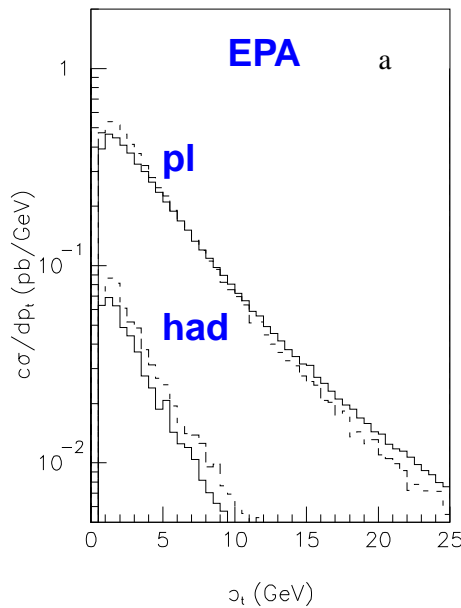
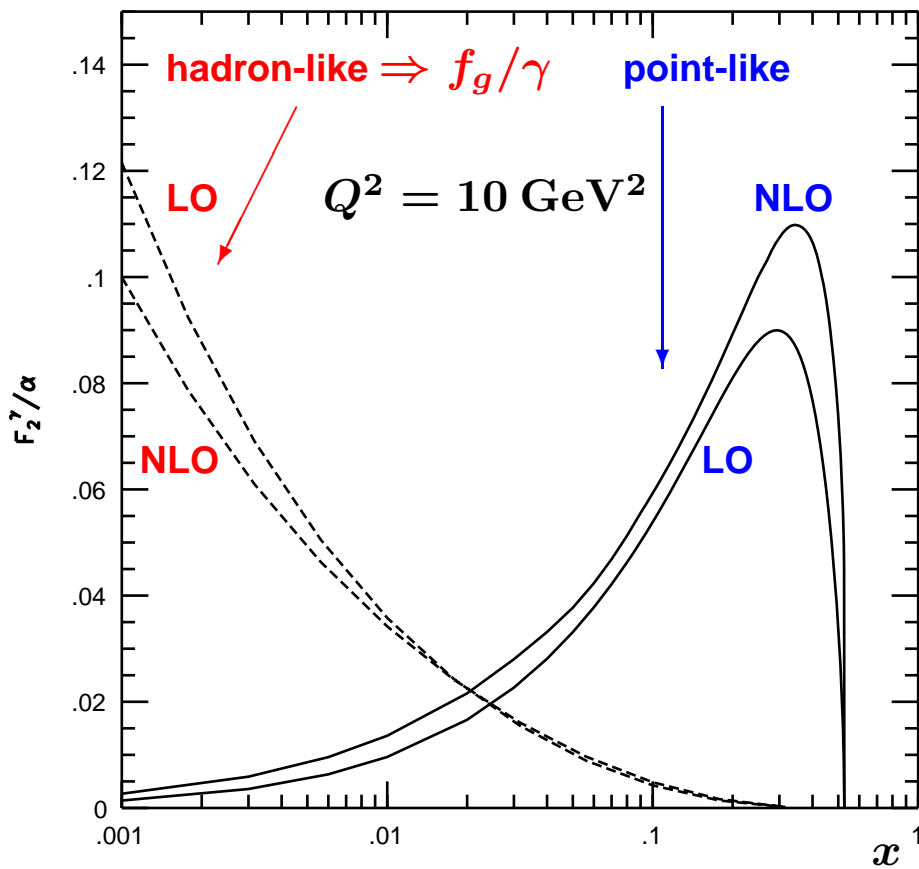
**point-like**, purely perturbative QCD prediction, dominates at **high- $x$**

**hadron-like**, depends on  $f_g^\gamma$ , dominates at **low- $x$**



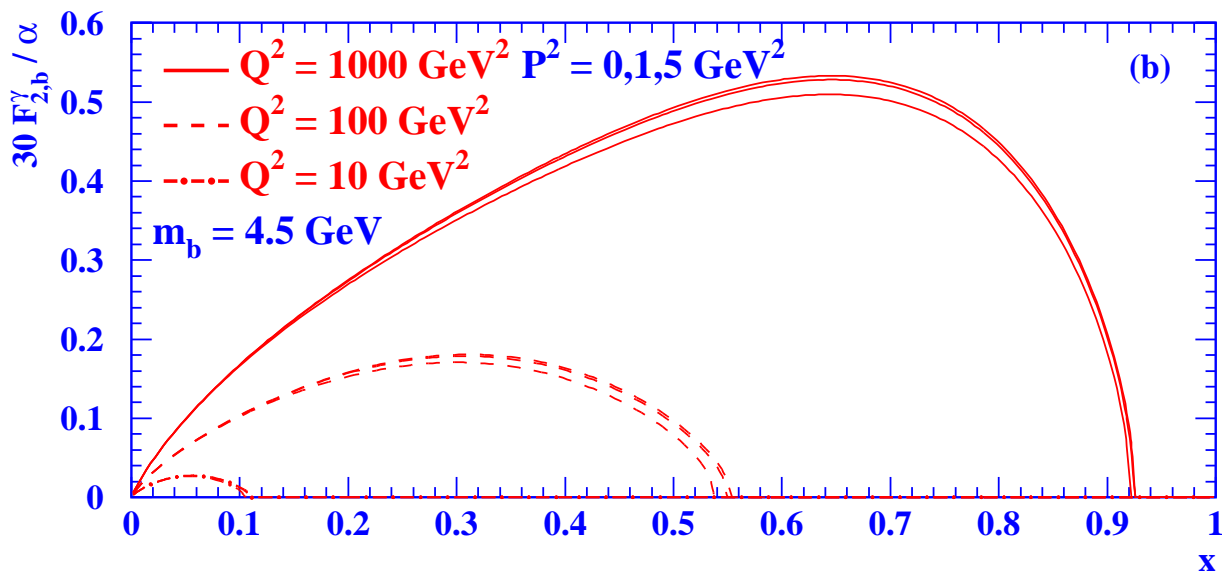
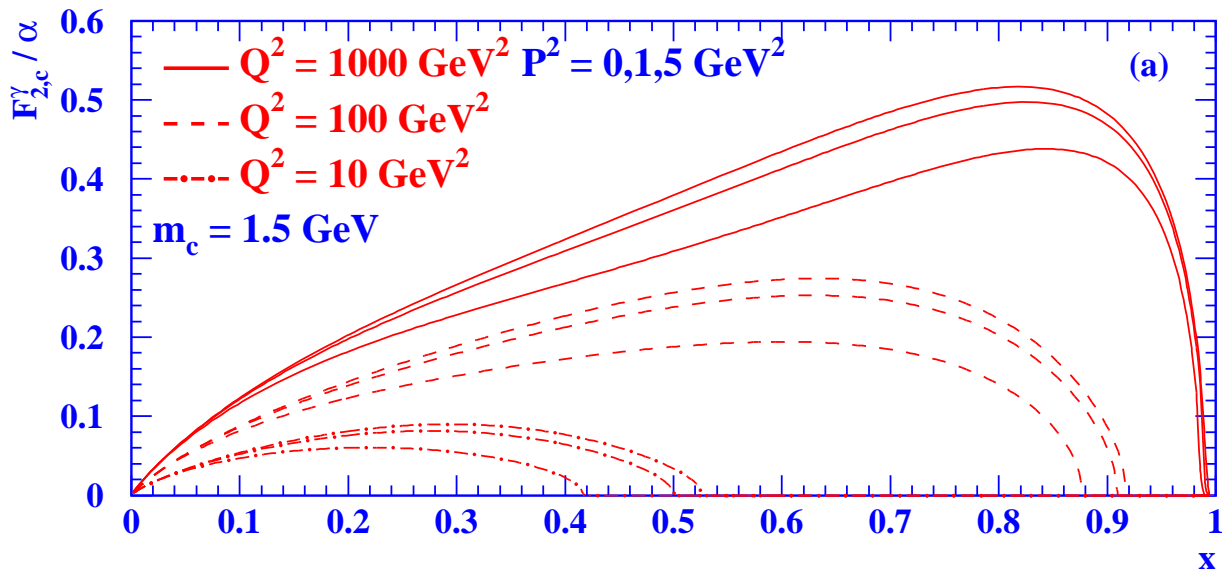
OPAL Collab., Eur. Phys. J. C16 (2000) 579. (updated)

# $F_{2,c}^\gamma$ at the Linear Collider



$E_{\text{tag}}/E_b > 0.5, \theta_{\text{tag}} > 40 \text{ mrad}, m_c = 1.5 \text{ GeV}, \mu = Q$

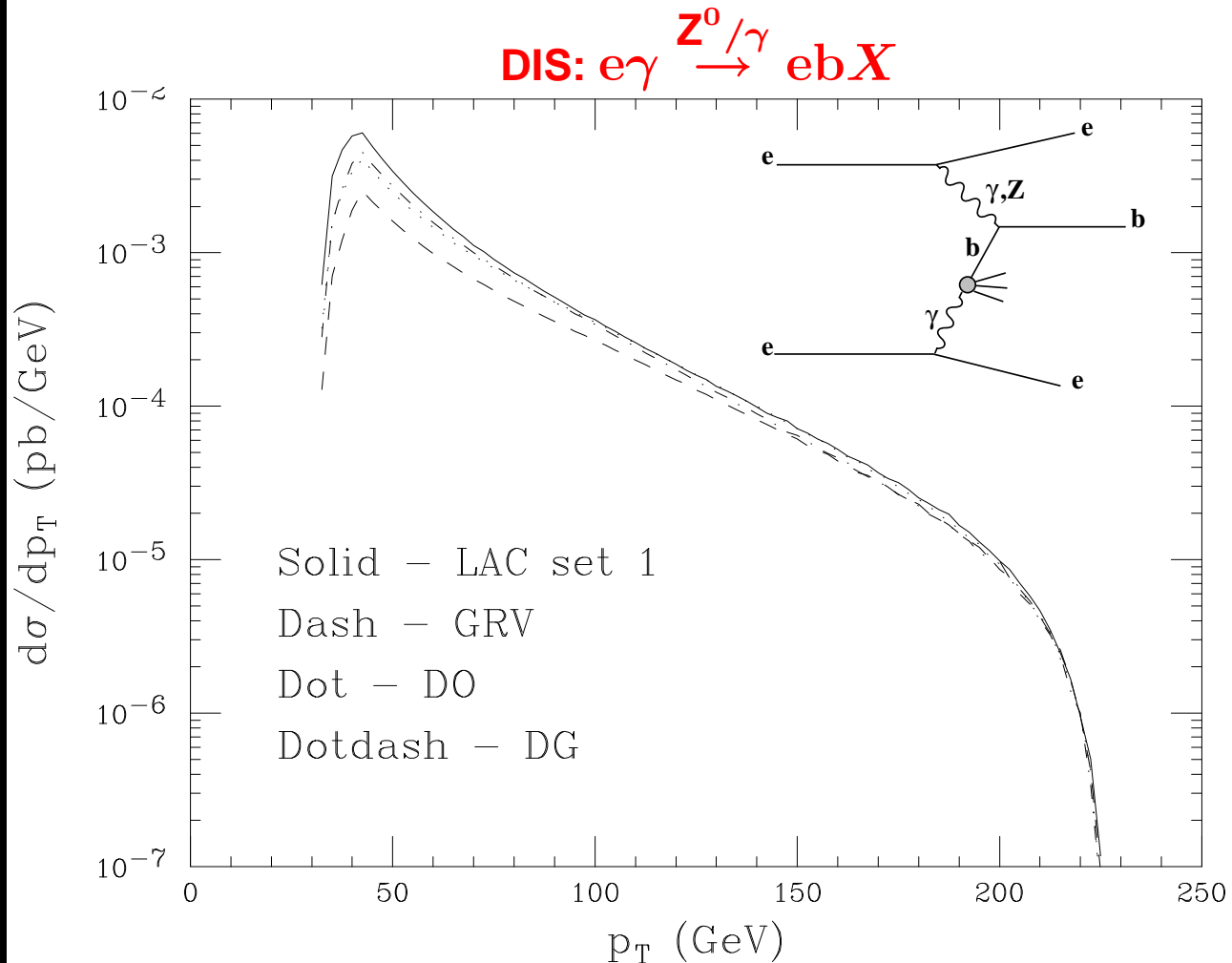
# The pointlike contribution to $F_{2,h}^\gamma$ charm versus bottom



**Bottom is heavier and also disfavoured by the charge.  
It may still be possible to measure  $F_{2,b}^\gamma$  at a Photon  
Collider.**

# Single bottom production at the LC

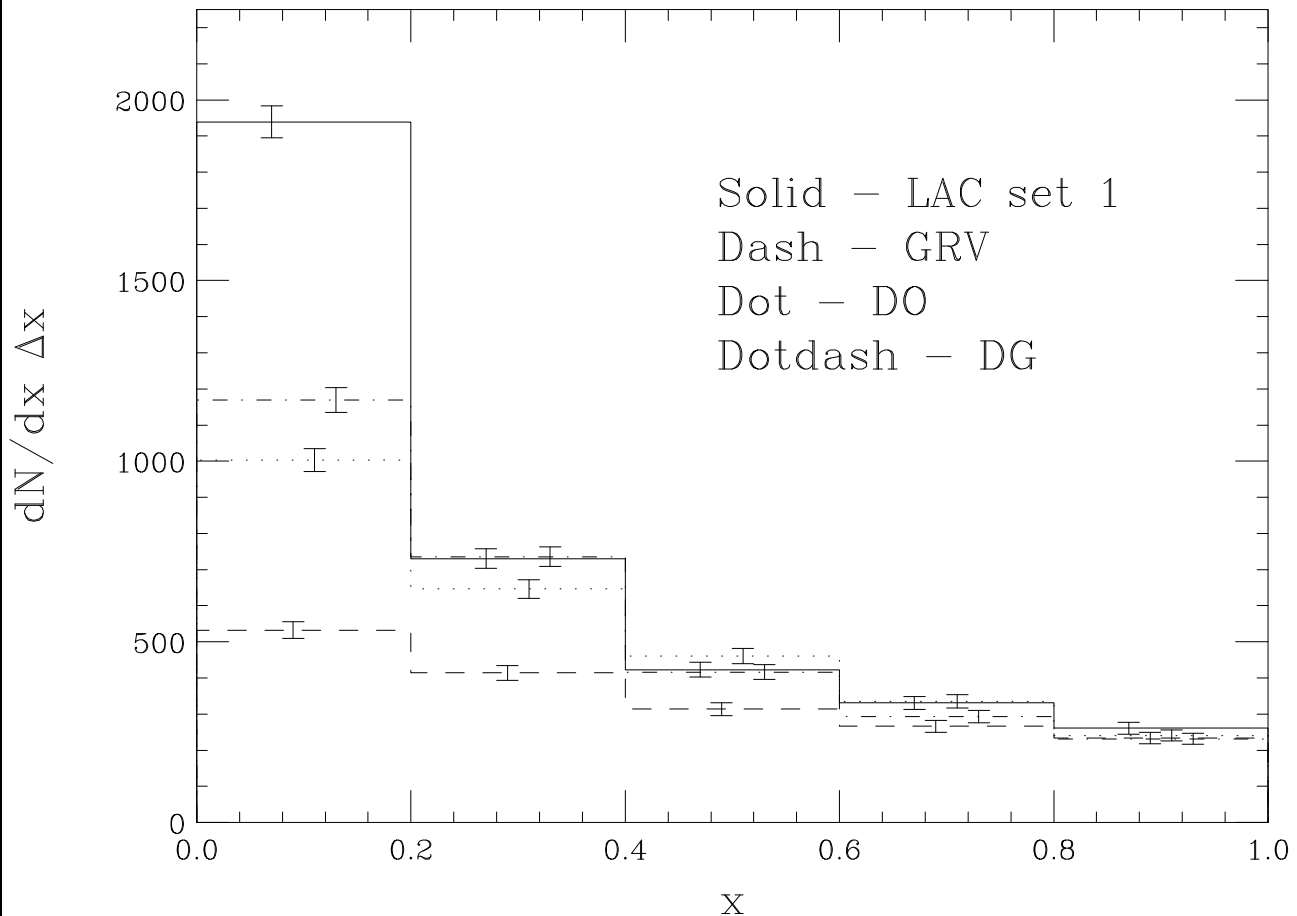
## 1) The method



**By virtue of the hard scale  $p_{t,b} > 40 \text{ GeV} \gg m_b$ ,  
bottom is treated as a massless quark distribution  
function of the photon.**

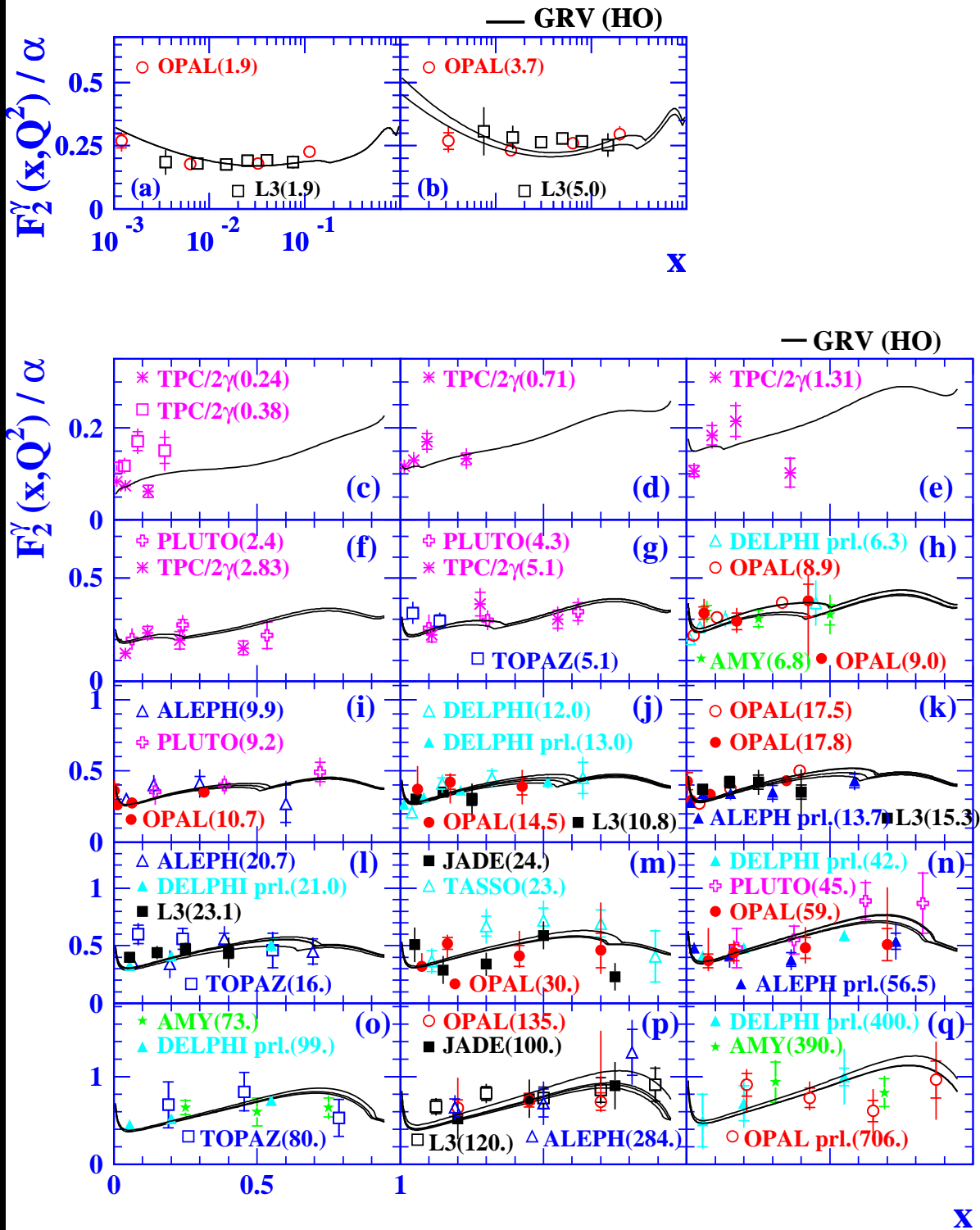
# Single bottom production at the LC

## 2) Event rates



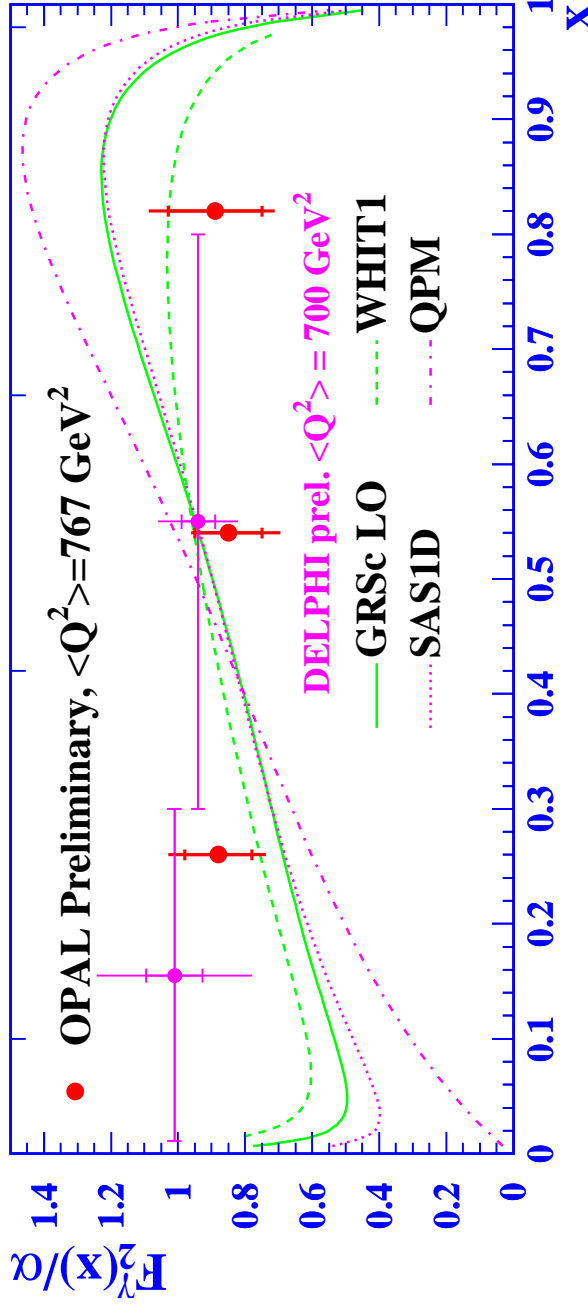
**Assuming  $\epsilon_b^\mu = 50\%$  for  $|\theta_b| < 0.85$  a distinction between several predictions of bottom distribution functions should be possible at a Photon Collider.**

# The world data on $F_2^\gamma$



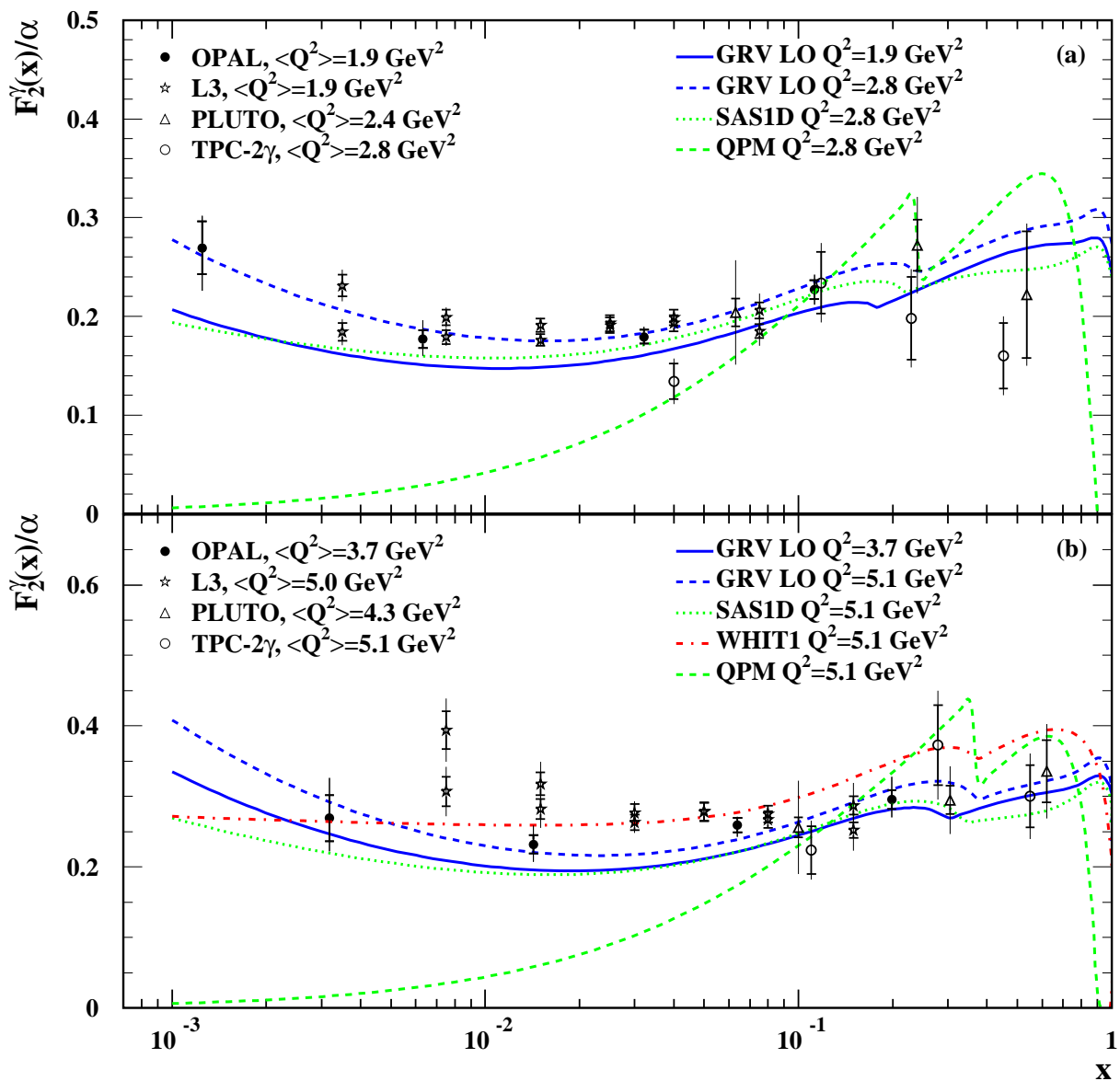


## The high $Q^2$ reach of $F_2^\gamma$ at LEP



- 1) We start to look at factorisation scales of about  $1000 \text{ GeV}^2$ .
- 2)  $F_2^\gamma$  is measured with 15-20% precision at  $Q^2 \approx 750 \text{ GeV}^2$ .
- 3) For  $x > 0.1$  the precision of the measurement is mainly limited by the statistical error. Get ADOL together to improve on the statistical error.

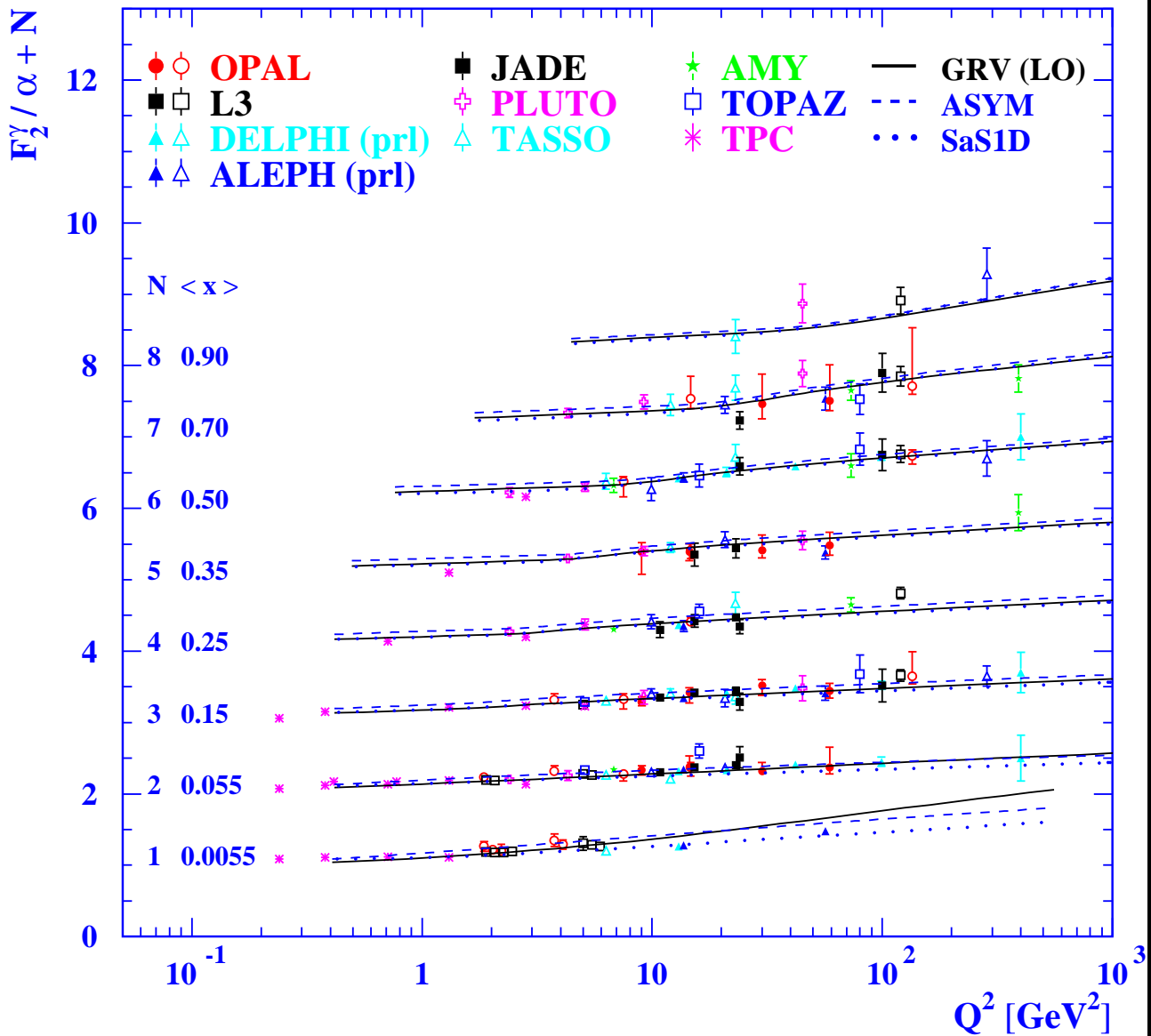
# Measurements at low $Q^2$ and $x$



**GRV(LO) and SaS1D are slightly too low compared to the data.**

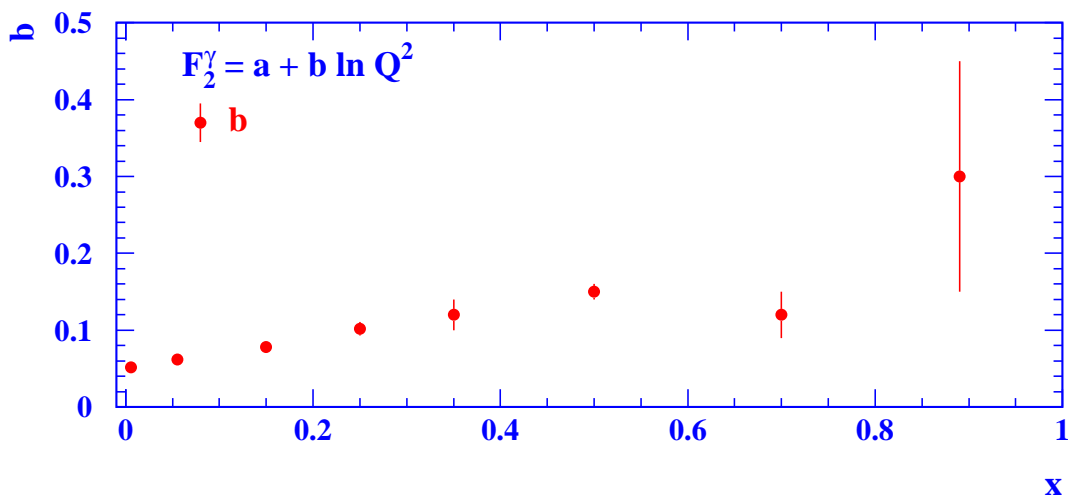
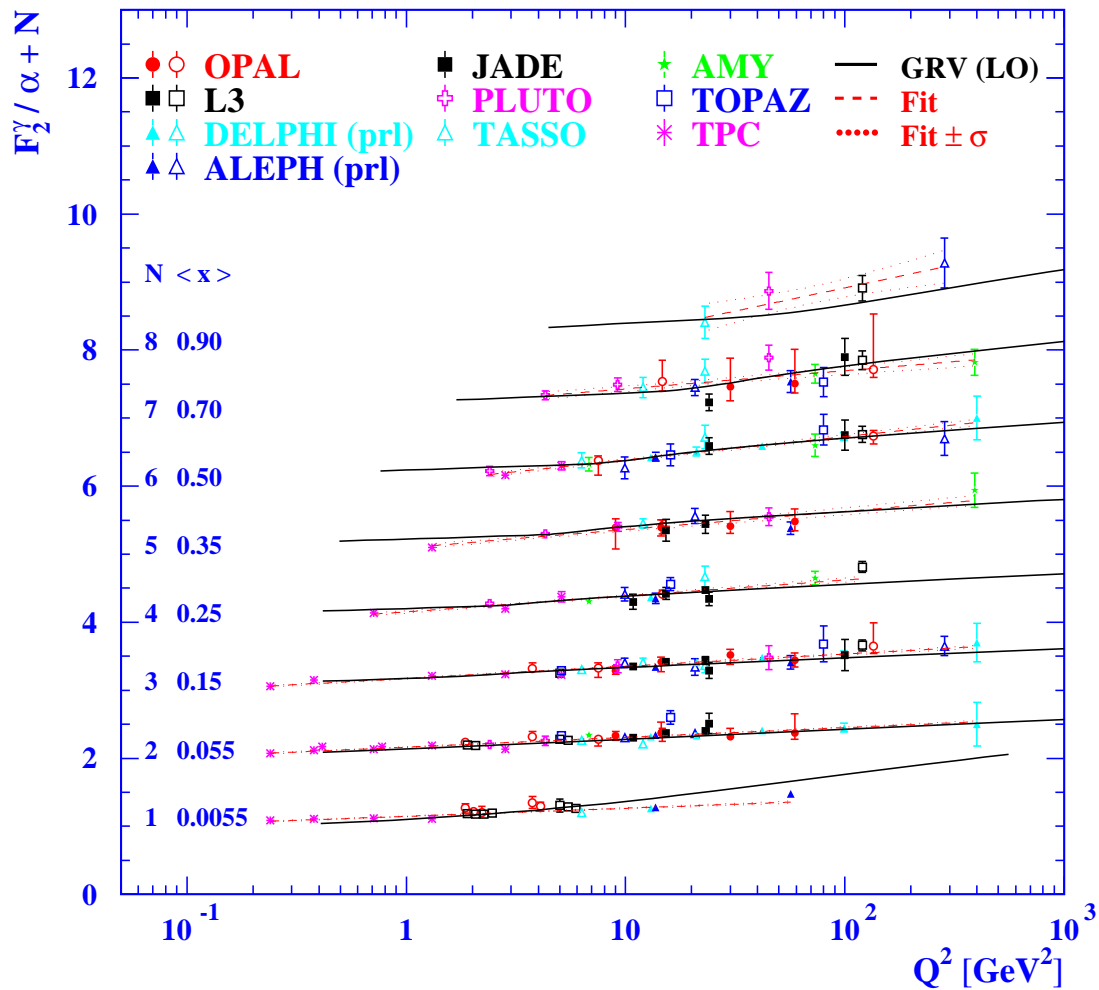
OPAL Collab., Eur. Phys. J. C18 (2000) 15.

# The $Q^2$ evolution of $F_2^{\gamma}$ for $n_f = 4$



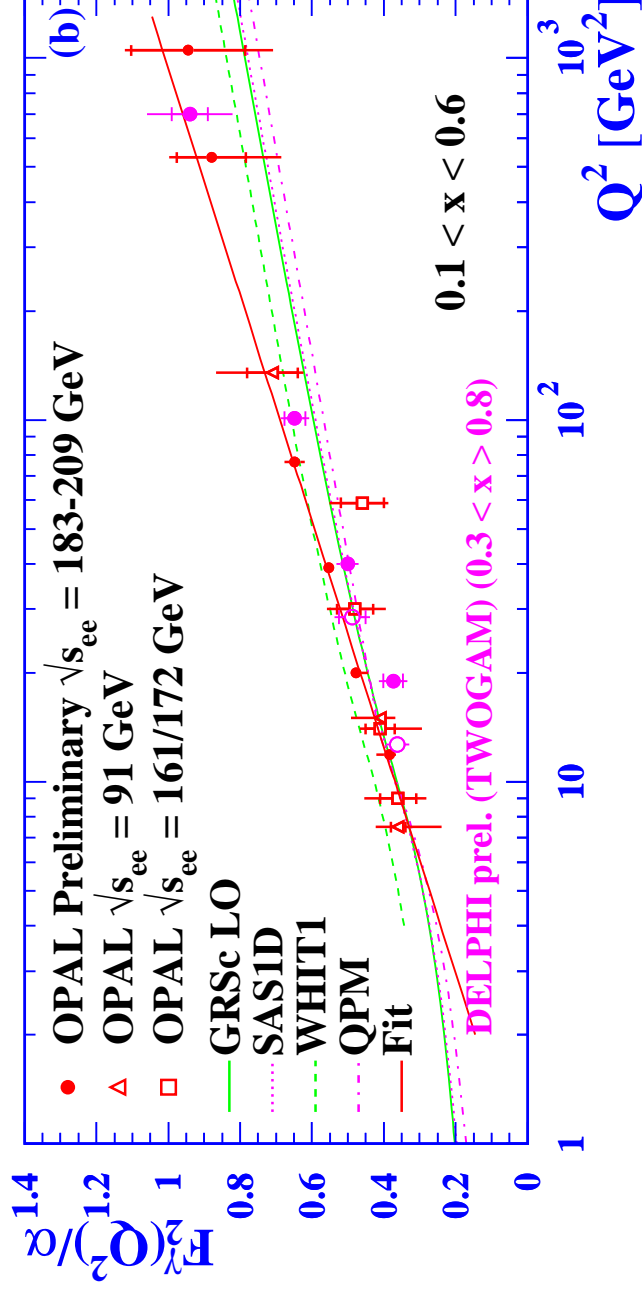
The general trend of the data is followed by the parametrisations.

# $Q^2$ evolution compared to linear fits



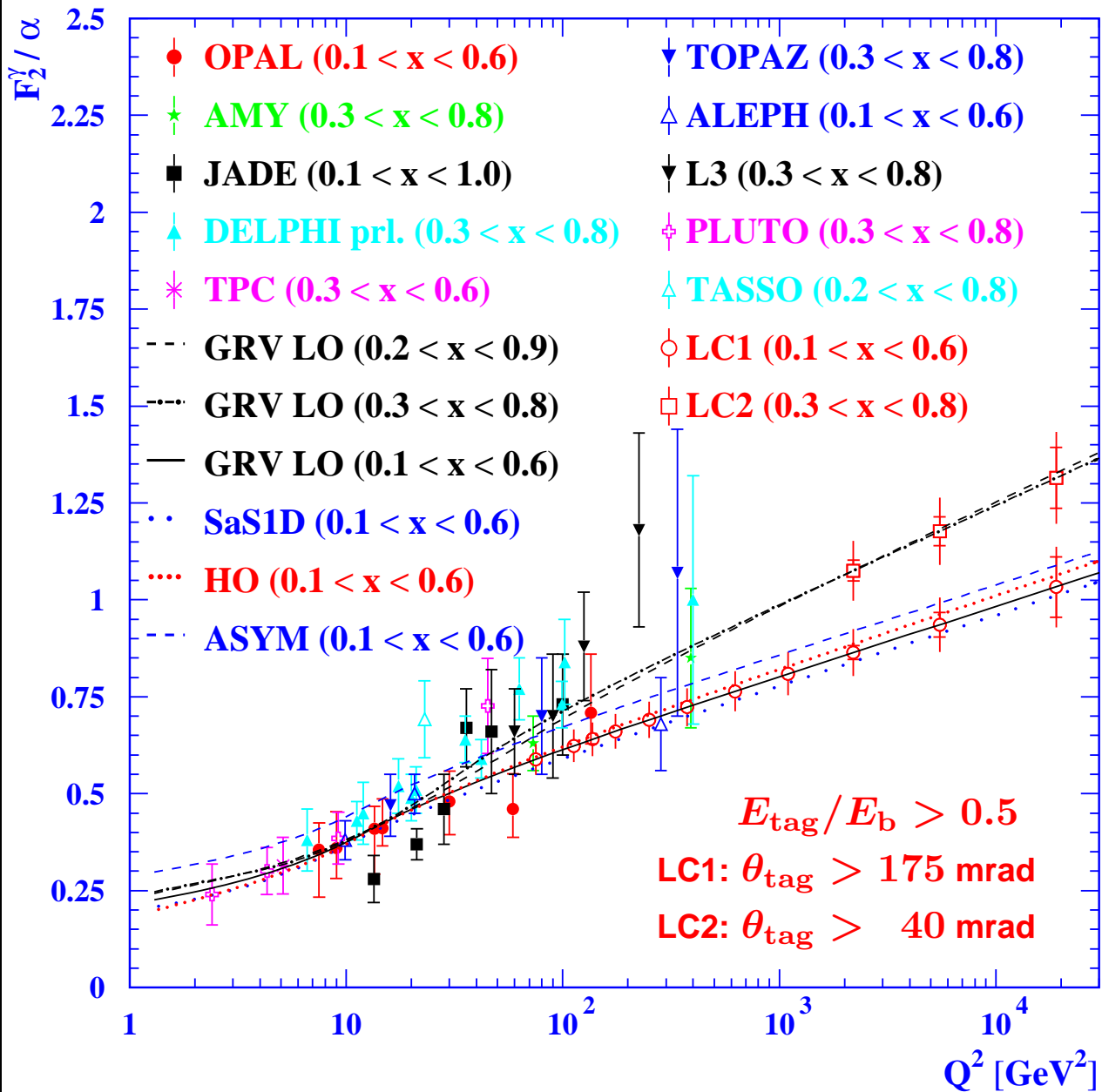
An increasing slope as a function of  $x$  is observed.

# Latest news on the $Q^2$ evolution of $F_2^\gamma$



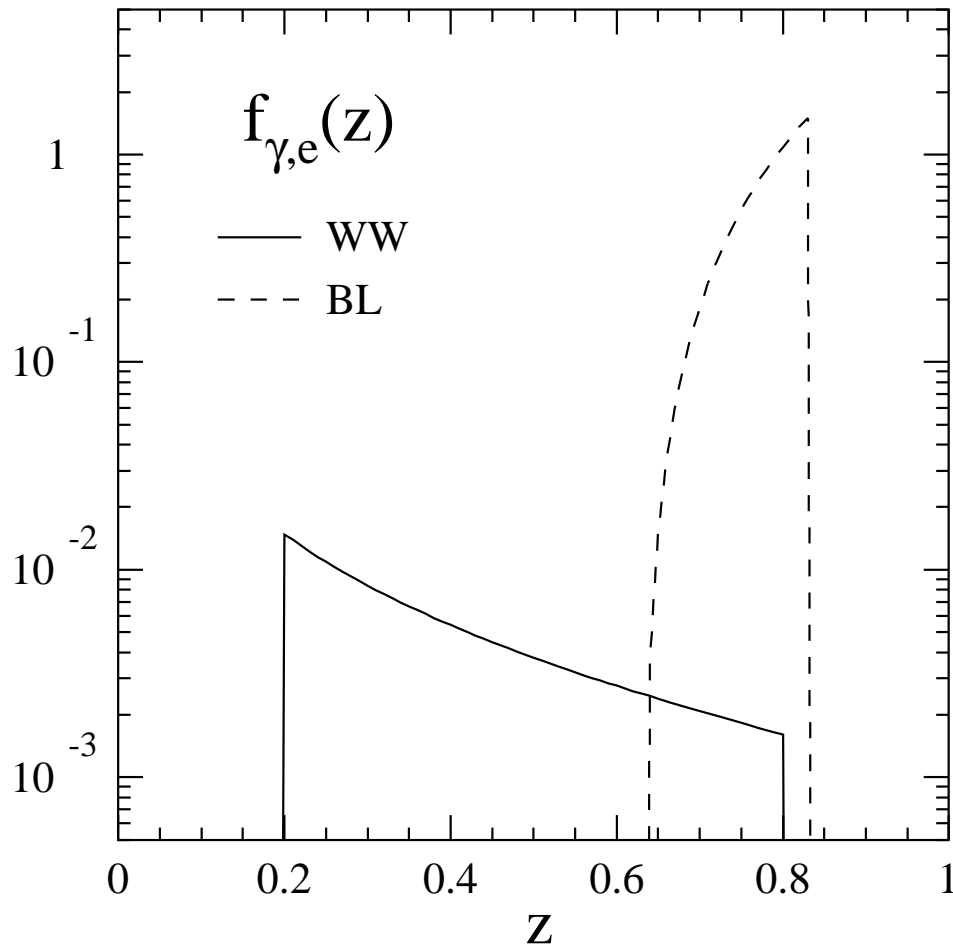
- 1) The errors have been reduced to about 5-10% at  $Q^2$  around 10-100 GeV $^2$ .
- 2) The measurements start to challenge theoretical predictions.
- 3) We need to worry more about the virtuality suppression of  $F_2^\gamma(x, Q^2, P^2)$  and radiative corrections.

# The future of the $F_2^\gamma$ measurement



The Linear Collider will play an important role in testing this fundamental prediction of perturbative QCD.

# Photon spectra for $F_2^\gamma$ measurements



## Used parameters:

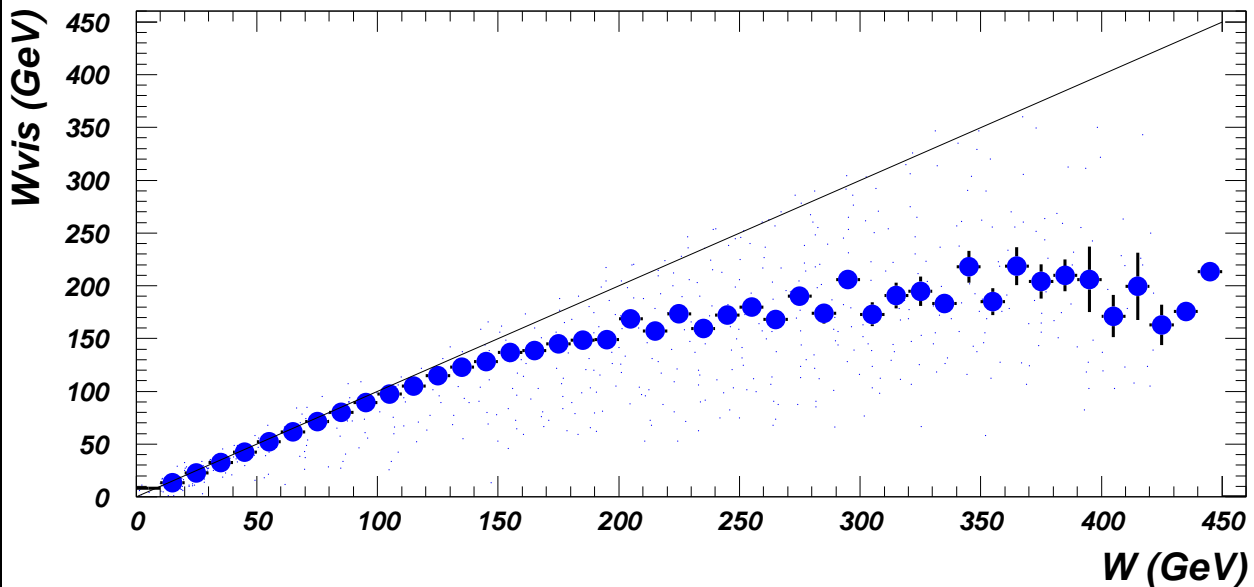
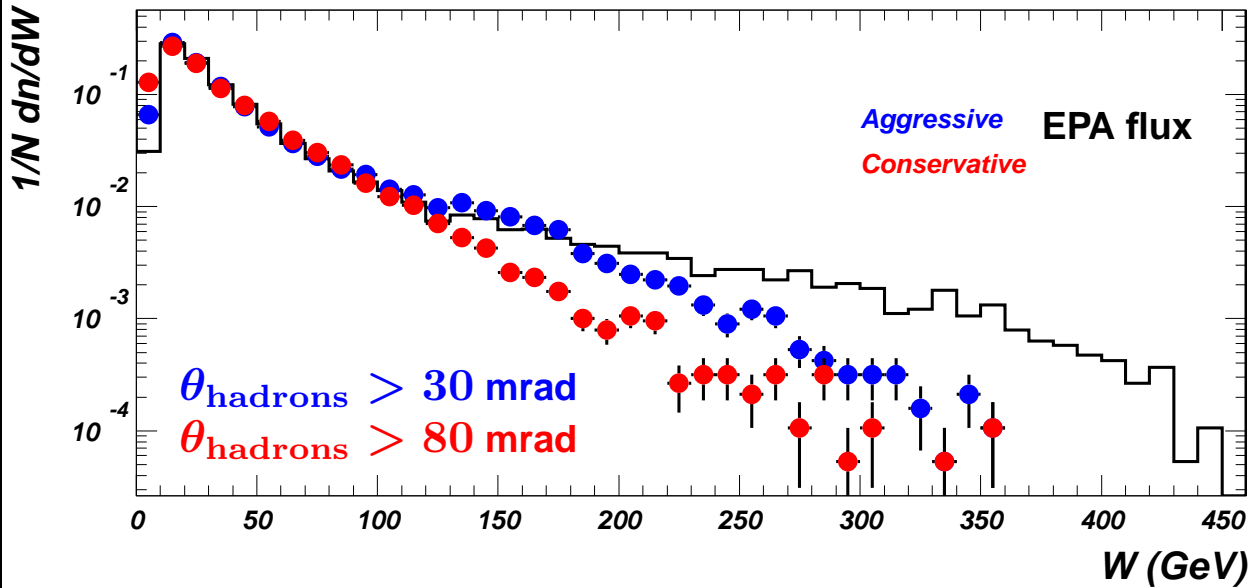
LC(WW):  $\epsilon = 10\%$  for tagging the electron that radiated the quasi-real photon

PC(BL):  $E_\gamma \approx 0.8E_b$  and  $\Delta E_\gamma \approx 0.1E_\gamma$

## Further assumptions:

$E_{\text{tag}} > 50 \text{ GeV}$  and  $\sigma_{\text{sys}} = \max(3\%, \sigma_{\text{stat}})$

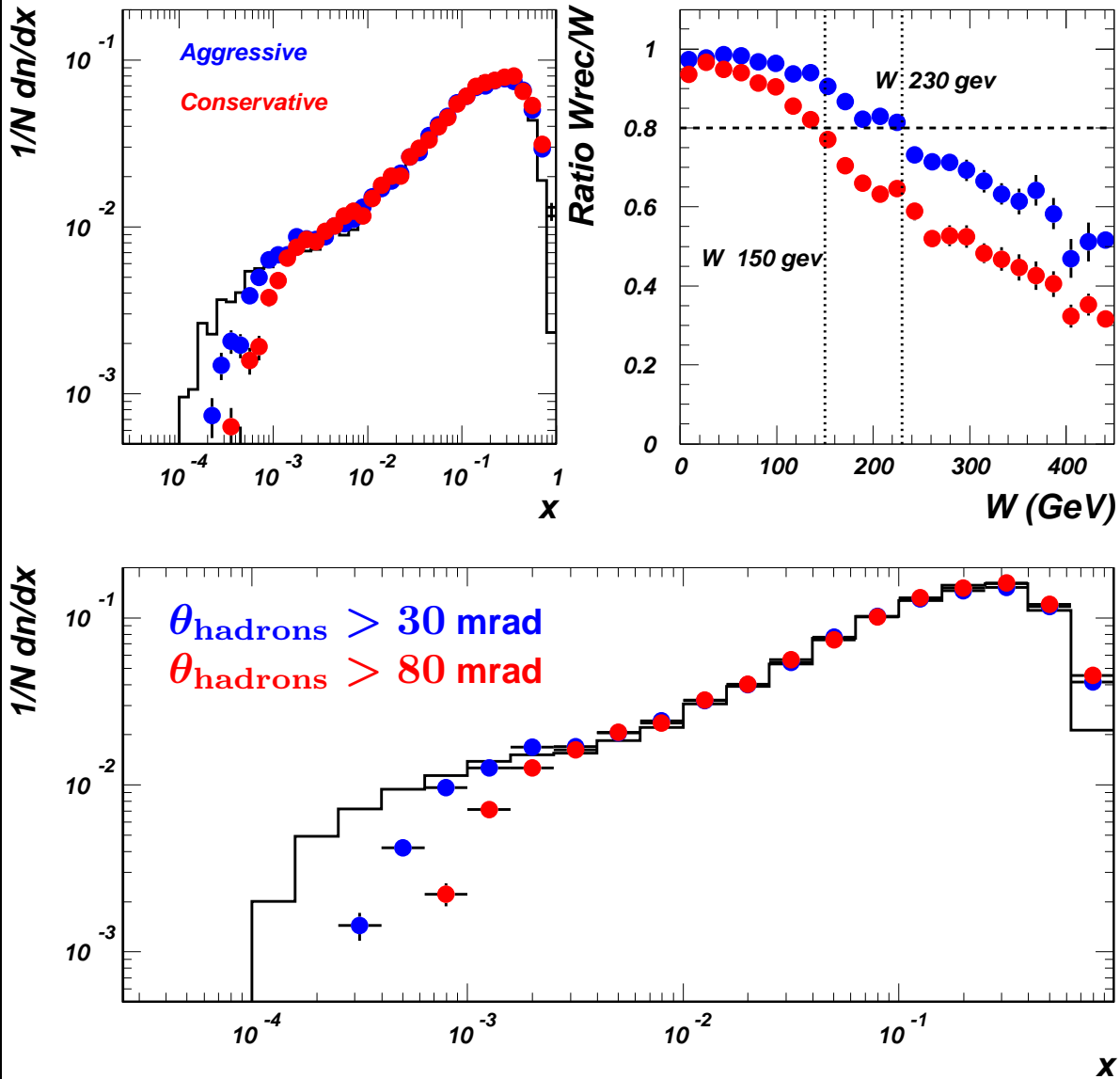
# The $W$ reconstruction



As usual, the forward region is vital for good  $W$  reconstruction.

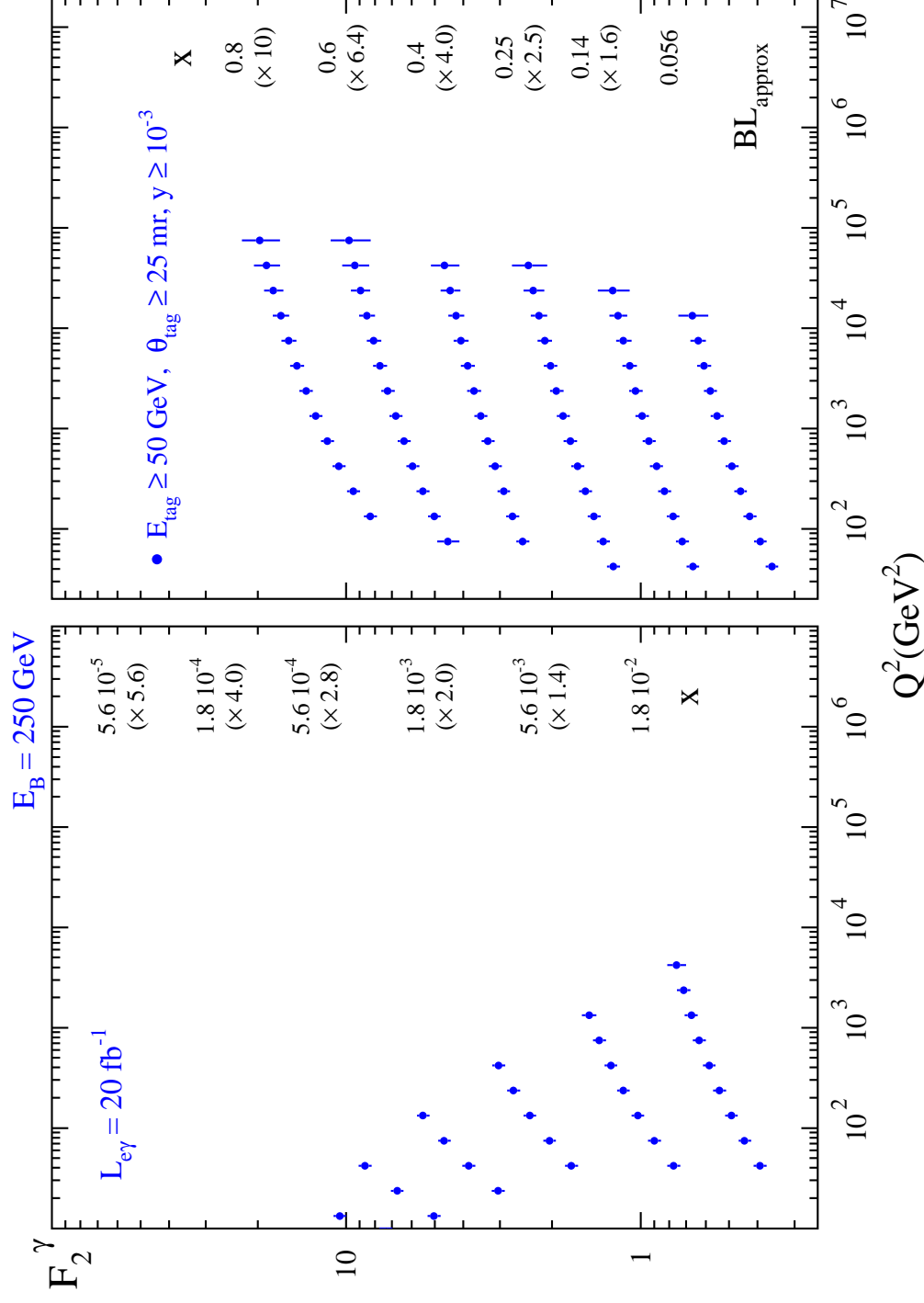


# The $x$ reconstruction



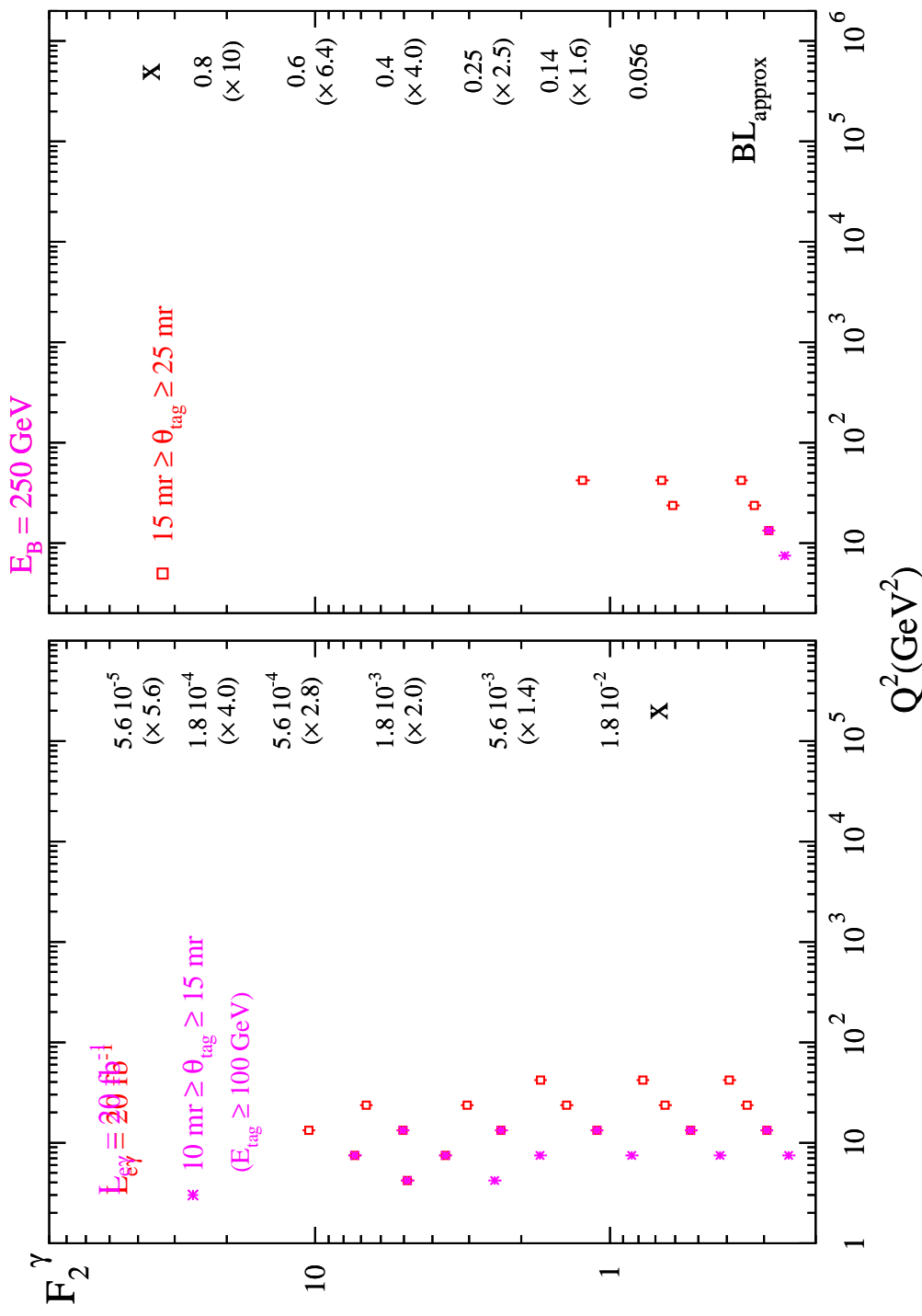
For  $\frac{W_{vis}}{W} > 0.8$  the reach in  $x$  is  
 $4 \cdot 10^{-4}$  or  $10^{-3}$  for  $\theta_{hadrons} > 30$  or 80 mrad.

# The $x$ and $Q^2$ reach for $F_2^\gamma$ at a Photon Collider (I)



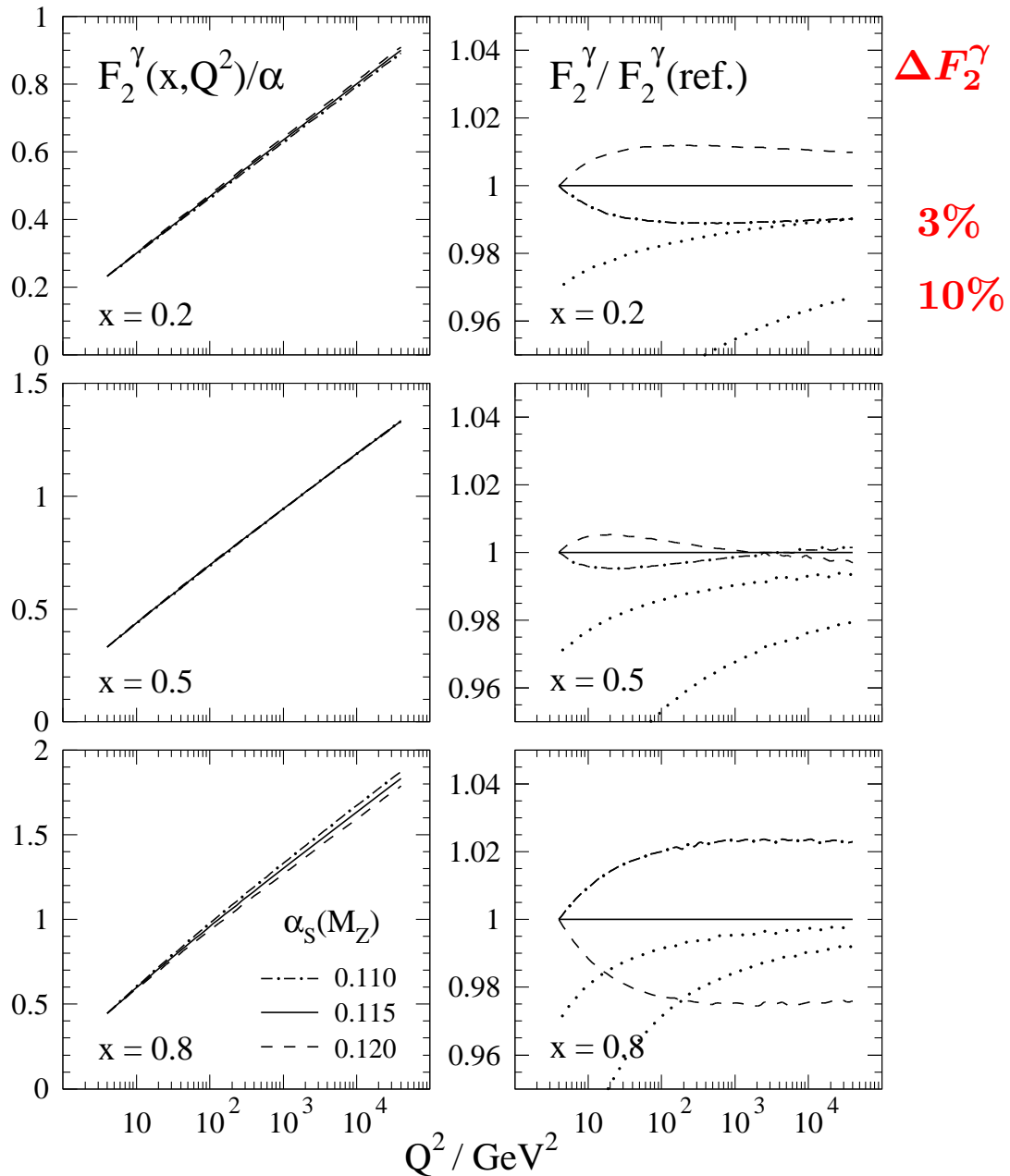
The phase space will be extended both to lower  $x$  and larger  $Q^2$ .

# The $x$ and $Q^2$ reach for $F_2^\gamma$ at a Photon Collider (II)



**Never stop dreaming!**

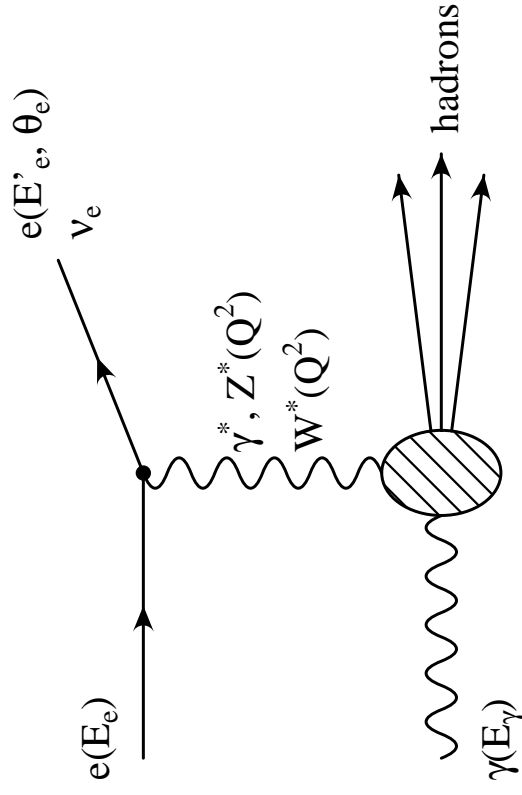
# The sensitivity to $\alpha_s$ at large $x$



The normalisation of  $F_2^\gamma$  depends on  $\alpha_s$ .

However, only very small effects are predicted:  
 e.g. at  $x = 0.8$  a variation of  $\Delta\alpha_s = 5\%$  means  
 $\Delta F_2^\gamma = 3\%$ . This will be hard to measure.

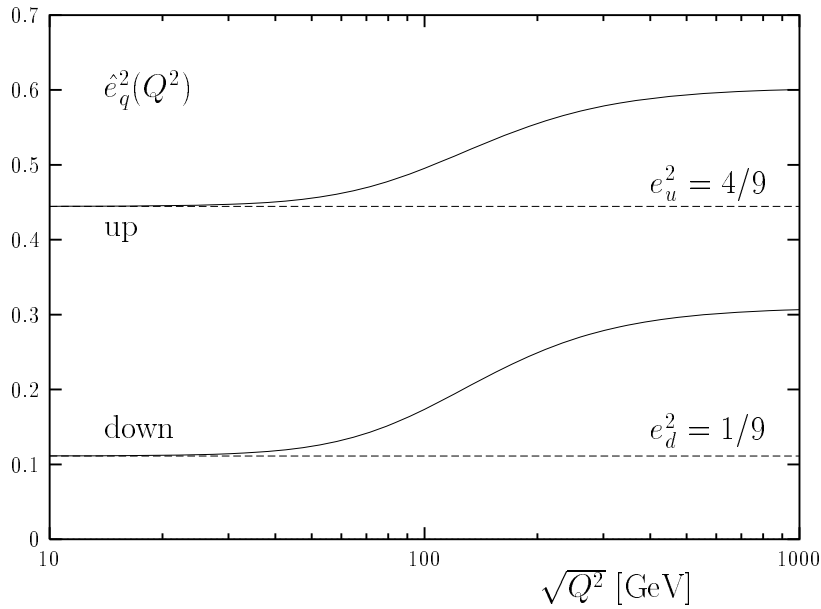
## Flavour decomposition of $F_2^\gamma$



$$\frac{d\sigma}{dx dy}(e\gamma \rightarrow eX) \propto \sum_{q=u..}^b \hat{e}_q^2 x q(x, Q^2)$$

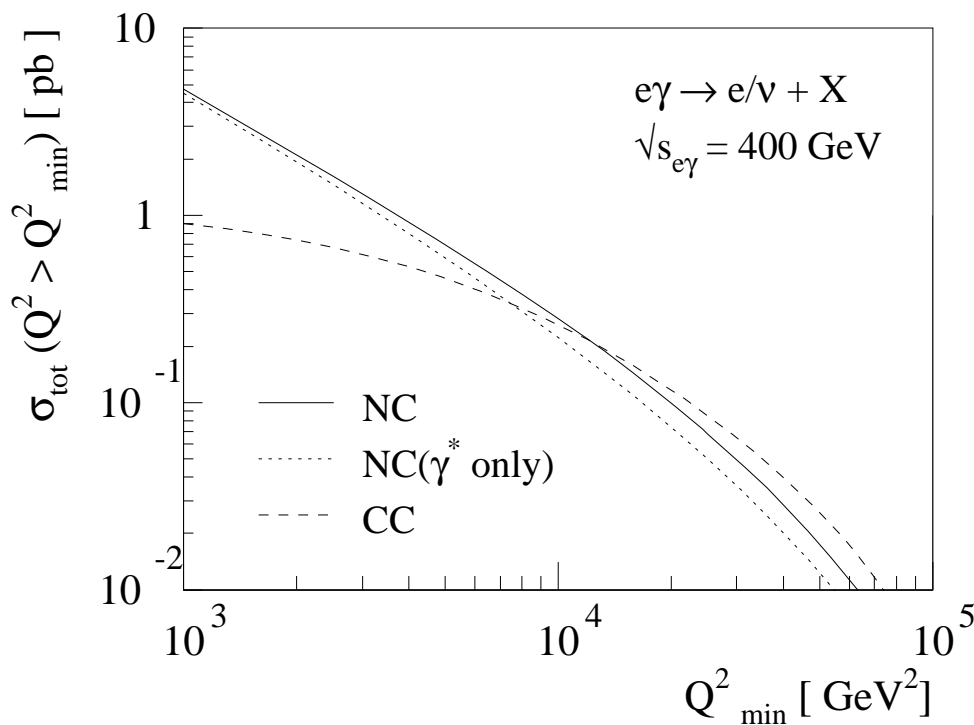
$$\frac{d\sigma}{dx dy}(e\gamma \rightarrow \nu_e X) \propto x [(u+c) + (1-y)^2 (d+s)]$$

# Effective charge and cross-section



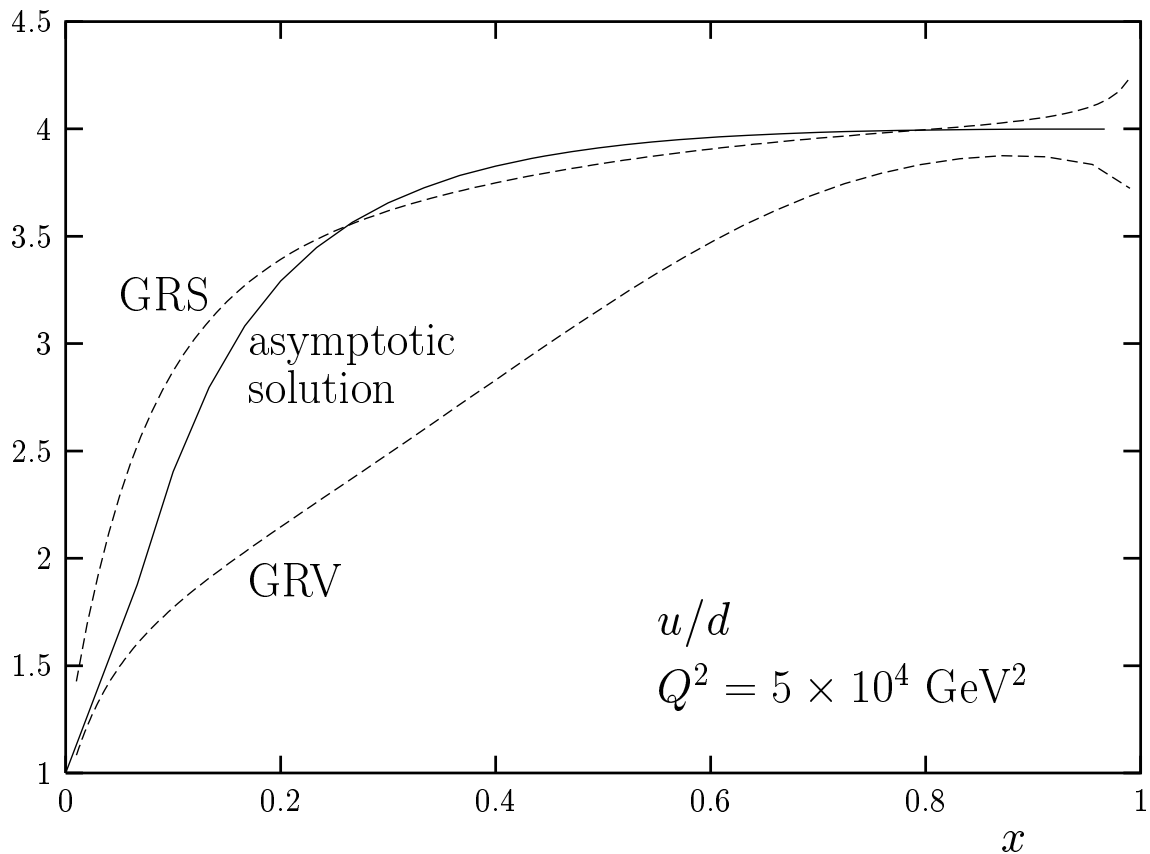
**0.44  $\rightarrow$  0.60**

**0.11  $\rightarrow$  0.31**



**This gives  $10^4$  CC and  $4 \cdot 10^4$  NC events per year.**

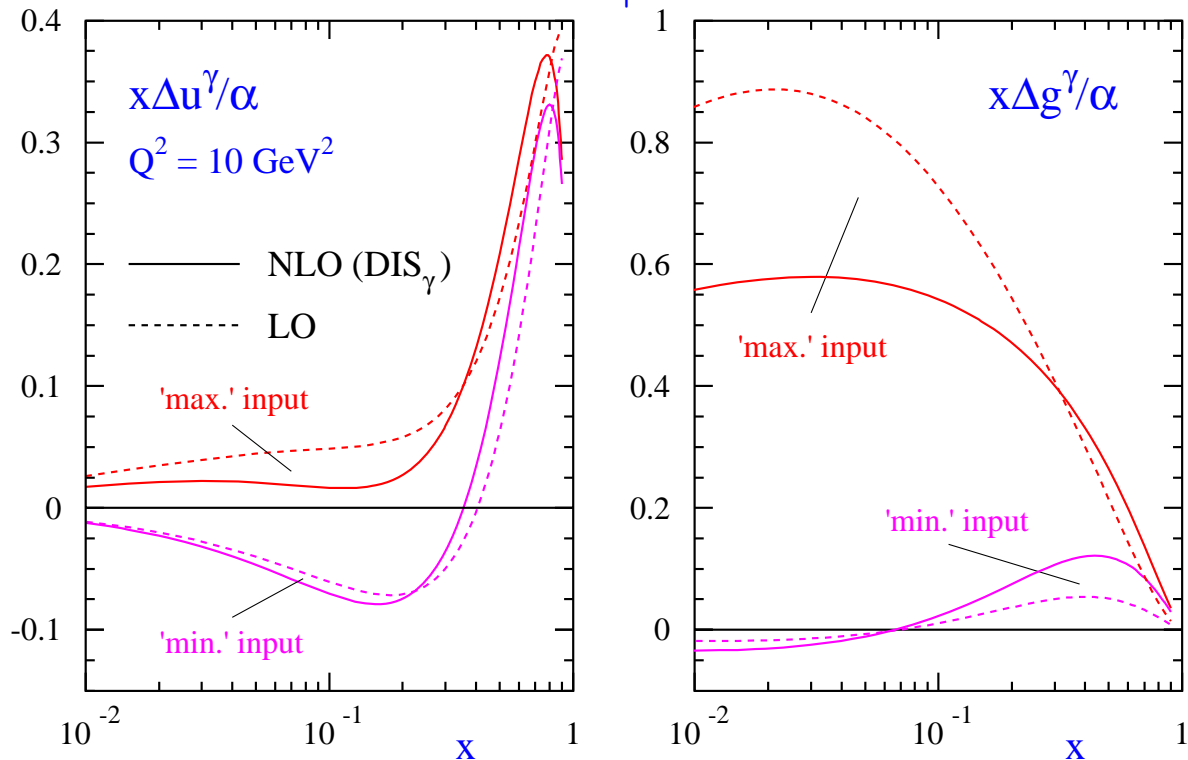
## Predictions of the u to d ratio



**At present the predictions for the u to d ratio vary within a factor of 2 to 3.**

# Polarized parton distributions

**Definition:**  $\Delta f^\gamma \equiv f_+^{\gamma+} - f_-^{\gamma+}$  for  $f = q, \bar{q}, g$



**Asymmetries:**  $\frac{\Delta\sigma}{\sigma} \equiv \frac{\sigma(++)-\sigma(+-)}{\sigma(++)+\sigma(+-)}$

At present we have **NO** experimental information on  $\Delta f^\gamma$ .

**Constraint:**  $\Delta\sigma \leq \sigma \Rightarrow |\Delta f^\gamma(x, Q^2)| \leq f^\gamma(x, Q^2)$

Fullfilled for  $\Delta f_{\text{point-like}}^\gamma$  but needs to be enforced for

$\Delta f_{\text{hadron-like}}^\gamma$

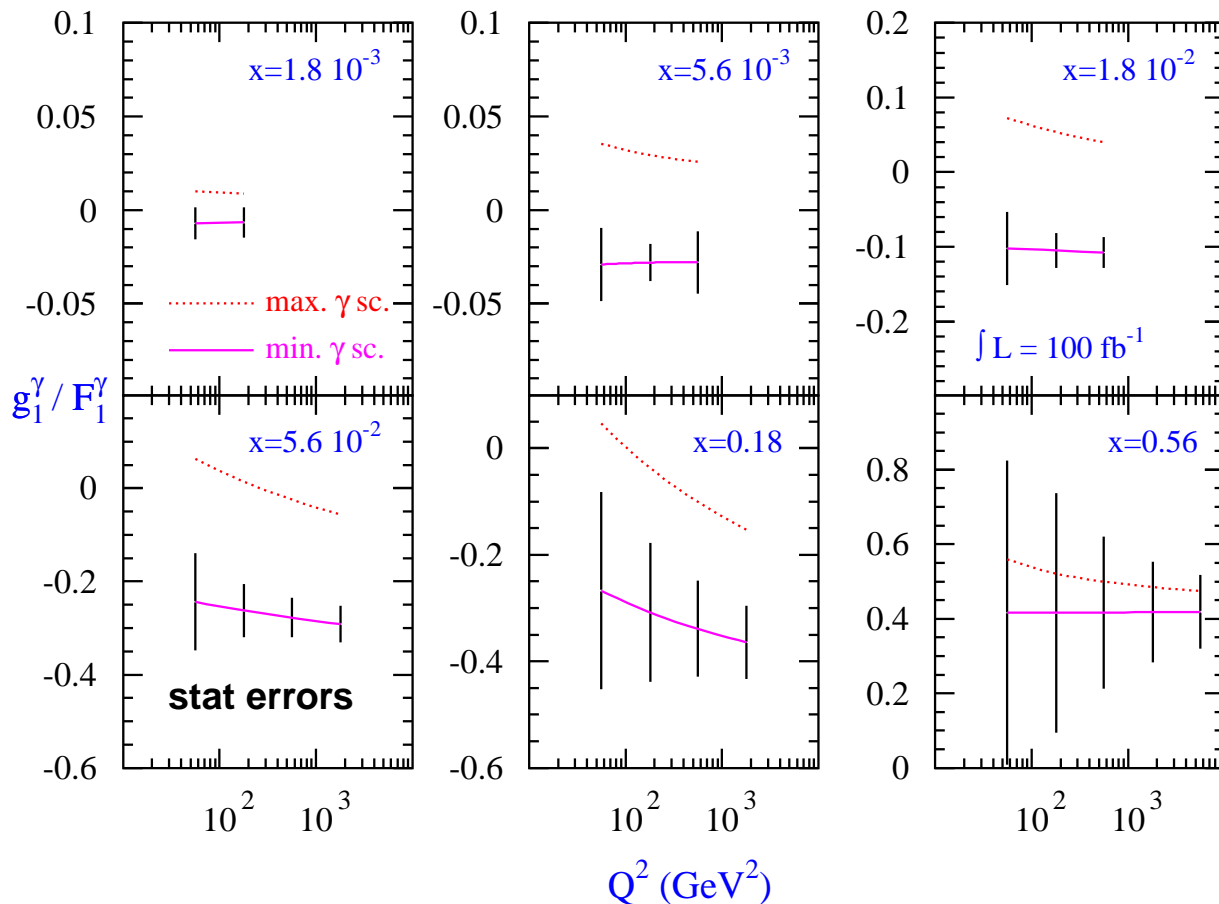
**Choices:**

$$\Delta f_{\text{hadron-like}}^\gamma(x, \mu^2) = \begin{cases} f^\gamma(x, \mu^2) & \text{'max input' } \\ 0 & \text{'min input' } \end{cases}$$

**Experimental information is highly desirable.**



# The ratio $g_1^\gamma / F_1^\gamma$ from DIS

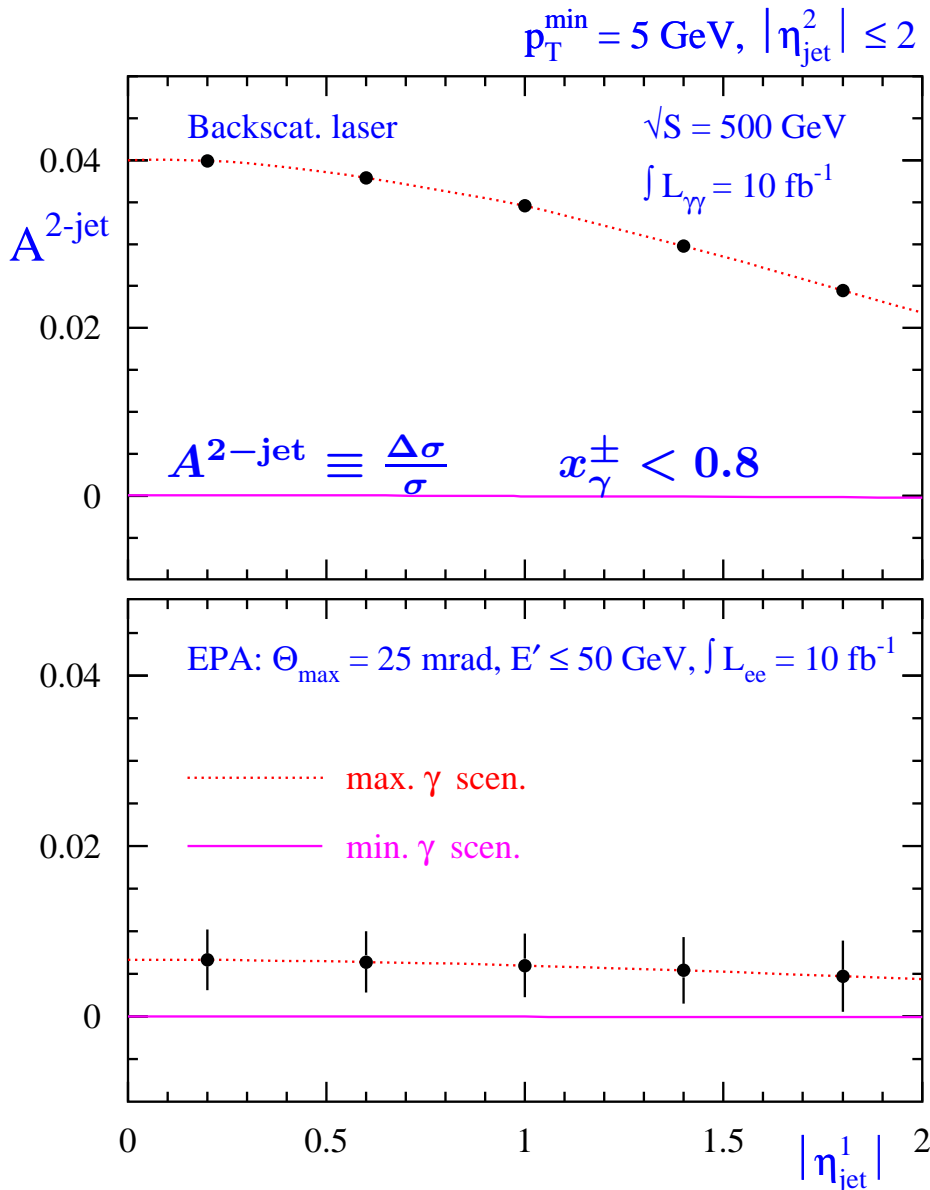


Asymmetry:  $\frac{\Delta\sigma}{\sigma} \propto \frac{g_1^\gamma}{F_1^\gamma}$

with:  $g_1^\gamma \propto \Delta q^\gamma + \alpha_s \Delta g^\gamma$

The structure function  $g_1^\gamma$  is mainly sensitive to quarks. Use  $F_1^\gamma$  from unpolarized DIS to determine the polarized distribution function  $\Delta q^\gamma$ .

# The di-jet sensitivity to $\Delta g^\gamma$

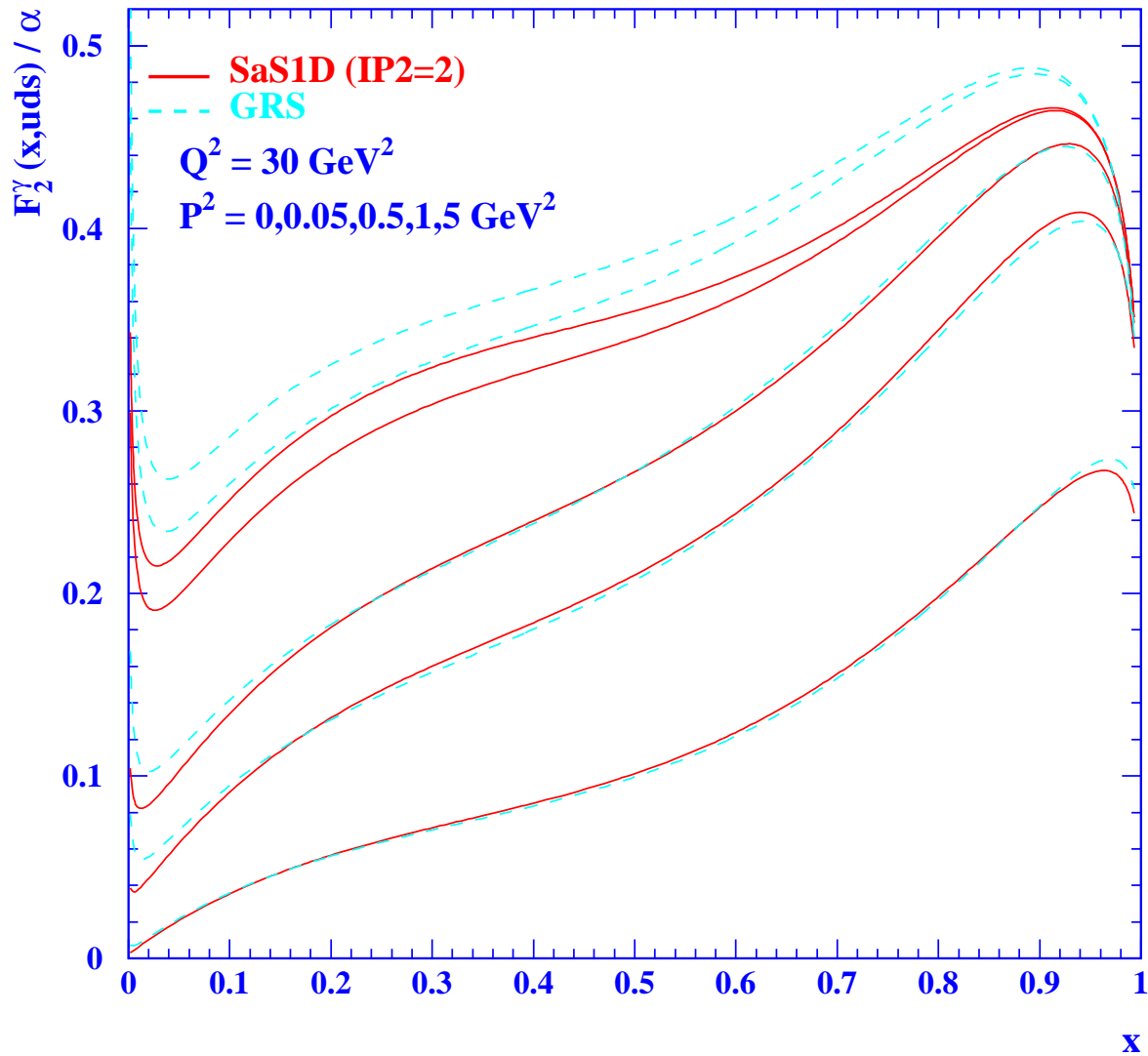


For double-resolved events  $A^{2\text{-jet}}$  is mainly sensitive to  $gg \rightarrow q\bar{q}$ , but also other processes contribute.

$\Rightarrow$  Use effective parton distribution function.

Extract  $\Delta g^\gamma$  from  $A^{2\text{-jet}}$  together with  $\Delta q^\gamma$  obtained from DIS. A Photon Collider is probably needed.

# $F_2^\gamma$ for virtual photons



The absolute predictions agree for  $P^2 > 0.5 \text{ GeV}^2$ ,  
when using SaS1D ( $IP2 = 2$ )

**The double tag limit:  $Q^2, P^2 \gg m_e^2, \frac{\rho_i^{00}}{2\rho_i^{++}} \rightarrow 1$**

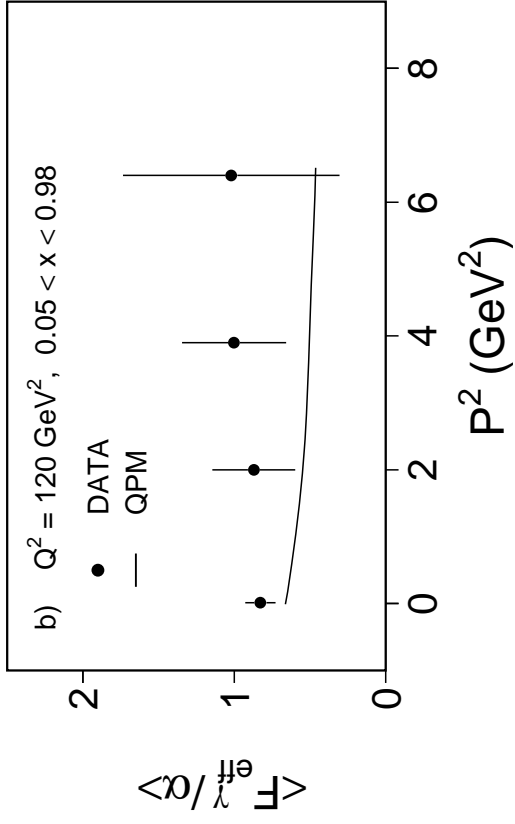
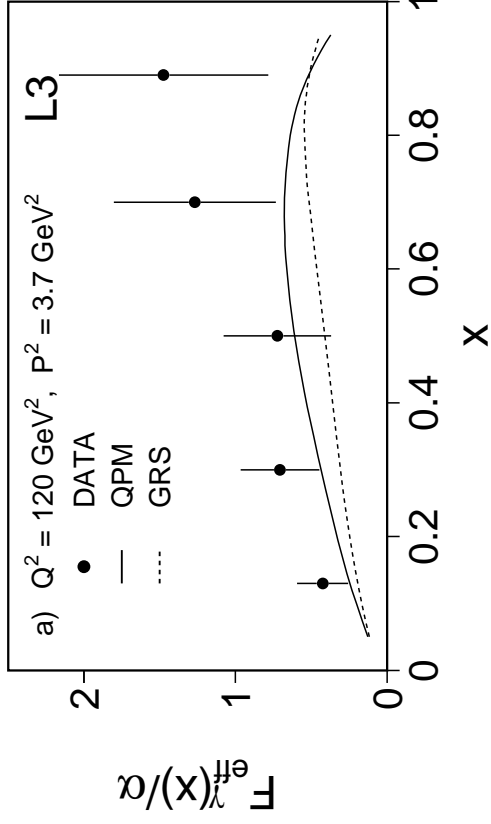
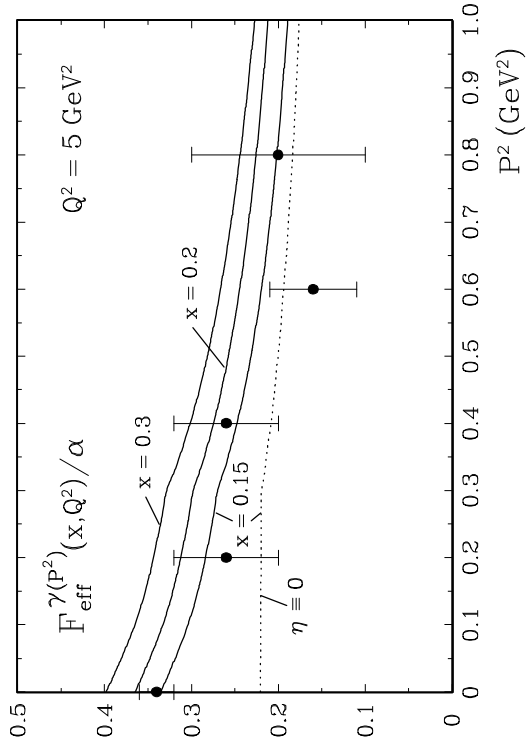
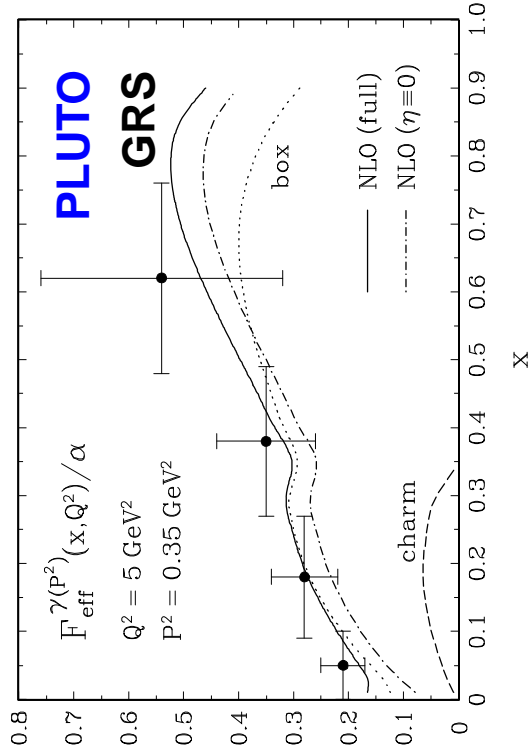
$$d^6\sigma = \frac{d^3p'_1 d^3p'_2}{E'_1 E'_2} \frac{\alpha^2}{16\pi^4 q^2 p^2} \left[ \frac{(q \cdot p)^2 - q^2 p^2}{(p_1 \cdot p_2)^2 - m_e^2 m_e^2} \right]^{1/2} 4\rho_1^{++} \rho_2^{++} \cdot$$

$$\left( \sigma_{TT} + \sigma_{TL} + \sigma_{LT} + \sigma_{LL} + \frac{1}{2}\tau_{TT} \cos 2\bar{\phi} - 4\tau_{TL} \cos \bar{\phi} \right)$$

$$d^6\sigma = \frac{d^3p'_1 d^3p'_2}{E'_1 E'_2} \mathcal{L}_{TT} \sigma_{\gamma^* \gamma^*},$$

$$d^6\sigma = L_{TT} \sigma_{\gamma^* \gamma^*} \quad \text{with:} \quad L_{TT} = \int \frac{d^3p'_1 d^3p'_2}{E'_1 E'_2} \mathcal{L}_{TT}$$

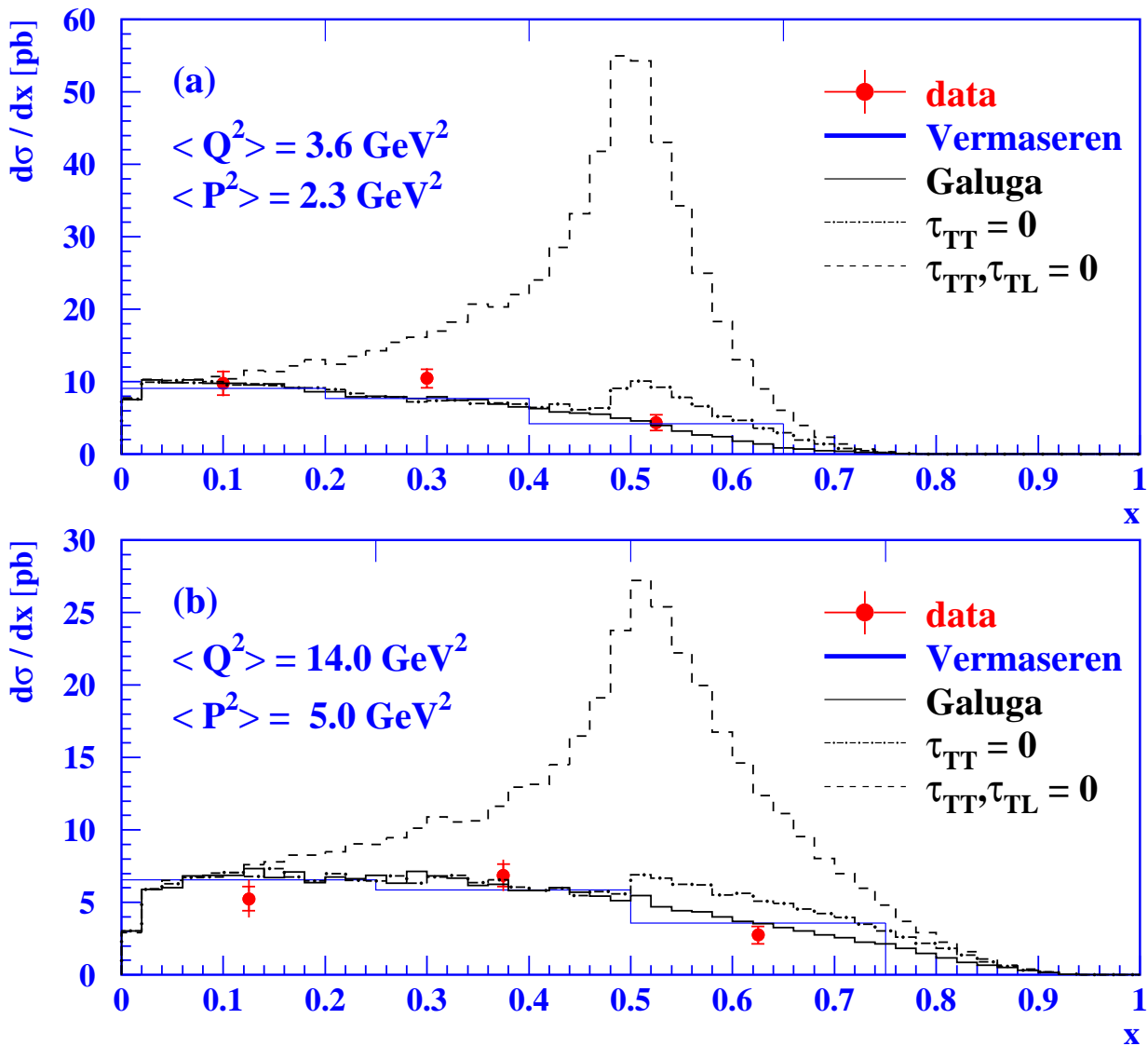
# The Measurements of $F_{\text{eff}}^{\gamma}$



# The cross-section for double tags

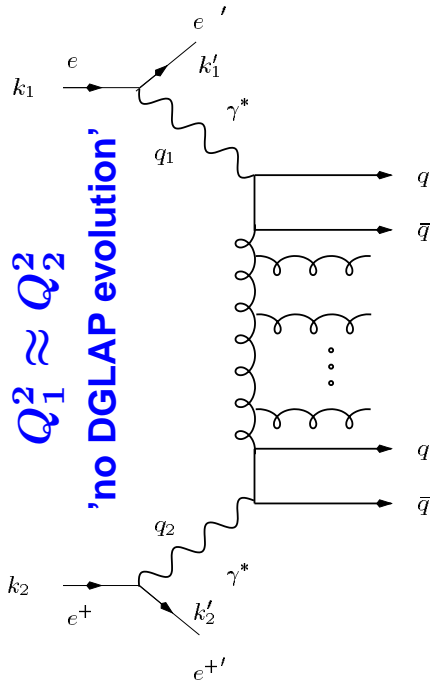
$$\text{for } e^+e^- \xrightarrow{\gamma^*\gamma^*} e^+e^- \mu^+\mu^-$$

OPAL



**QED agrees well with the data and the presence of the interference terms is clearly seen for the first time.**

# $\sigma_{\gamma^*\gamma^*}$ as a signal of BFKL



$$y_1 = \frac{q_1 k_2}{k_1 k_2}, \quad Q_1^2 = -q_1^2$$

$$s = (k_1 + k_2)^2, \quad s_0 = \frac{\sqrt{Q_1^2 Q_2^2}}{y_1 y_2}$$

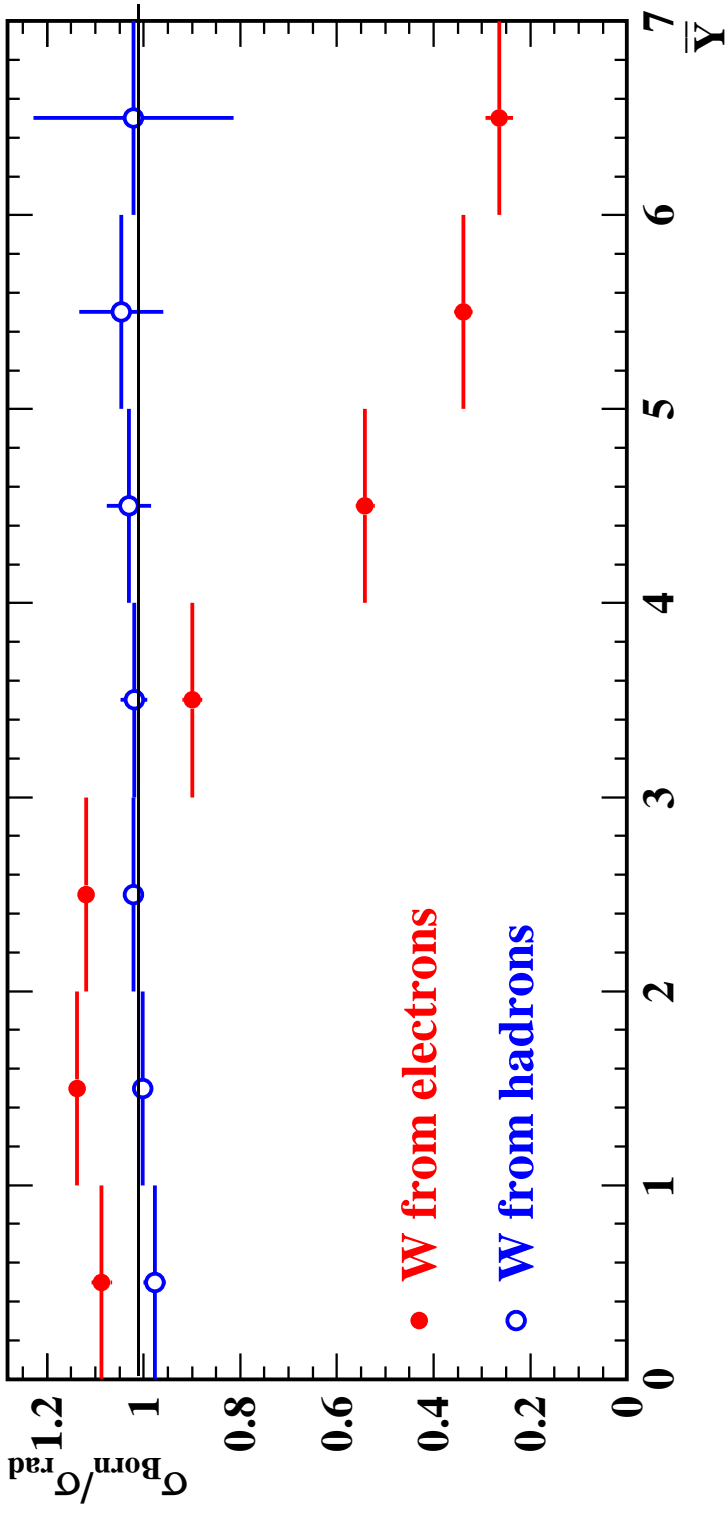
$$\hat{s} = W^2 \approx s y_1 y_2$$

- 1) Take  $Q_i^2 \gg \Lambda_{\text{QCD}}^2$  and  $Q_1^2 \approx Q_2^2$  to allow for a perturbative prediction without DGLAP evolution.
- 2) Look at a region where the phase space for gluon emission is large  $\Rightarrow W^2 \gg Q_1^2, Q_2^2$ .
- 3) Define:

$$Y = \ln \left( \frac{s y_1 y_2}{\sqrt{Q_1^2 Q_2^2}} \right) \simeq \ln \left( \frac{W^2}{\sqrt{Q_1^2 Q_2^2}} \right) = \bar{Y},$$

and measure the cross-section as a function of  $Y$  or  $\bar{Y}$ .

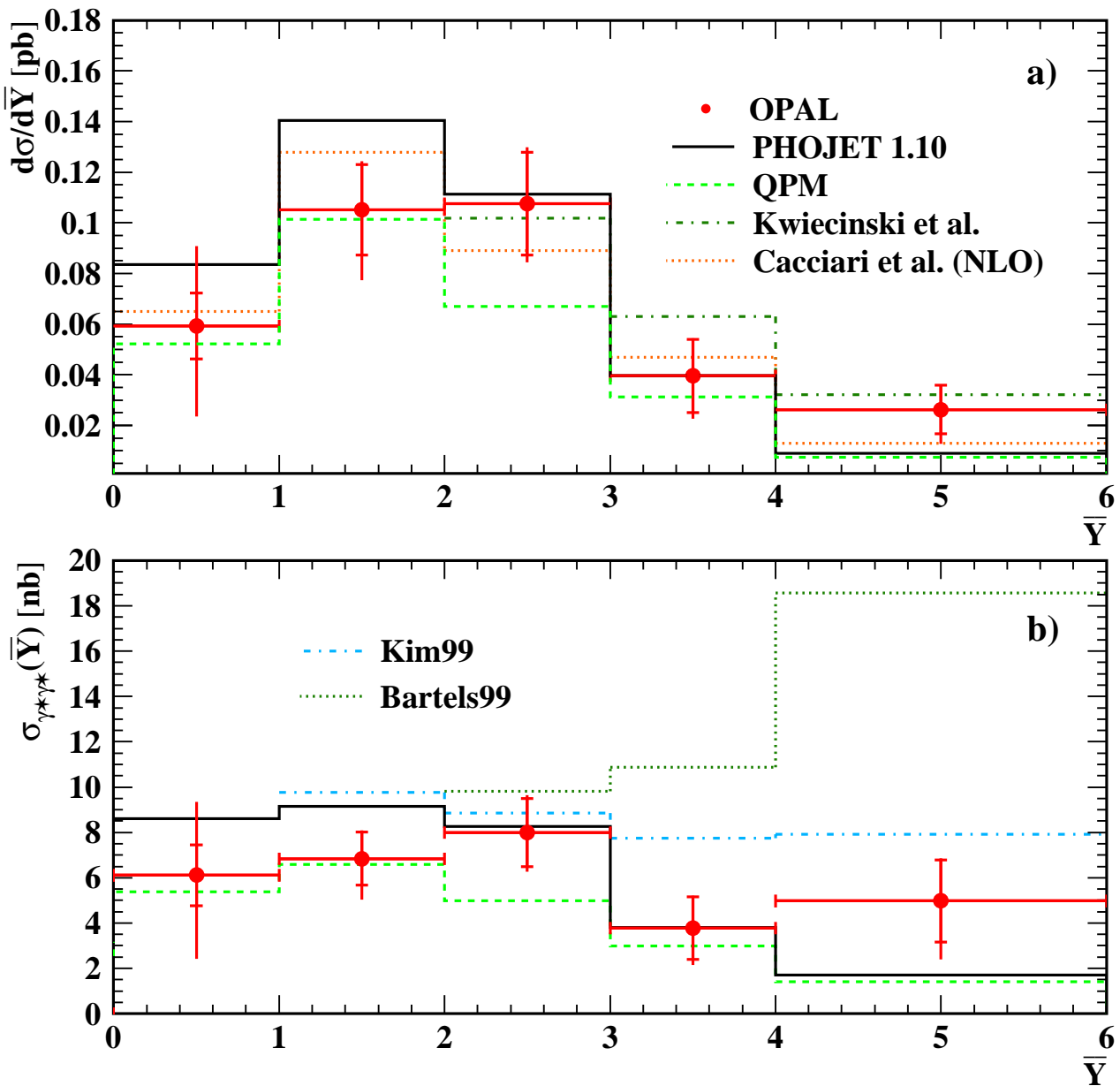
## The importance of QED radiative corrections



Radiative corrections are only important for the electron method, and they are large at large  $\bar{Y}$  which means at low electron energies.

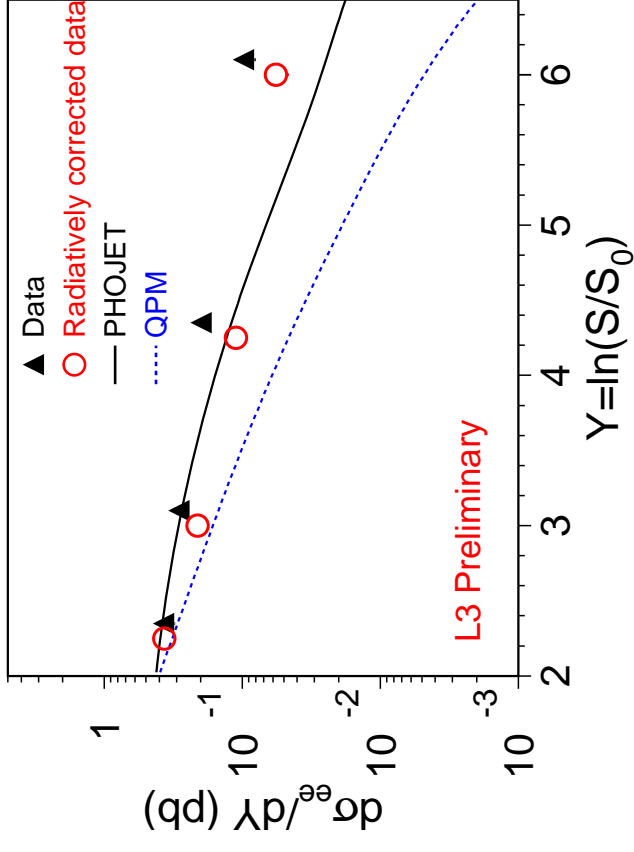
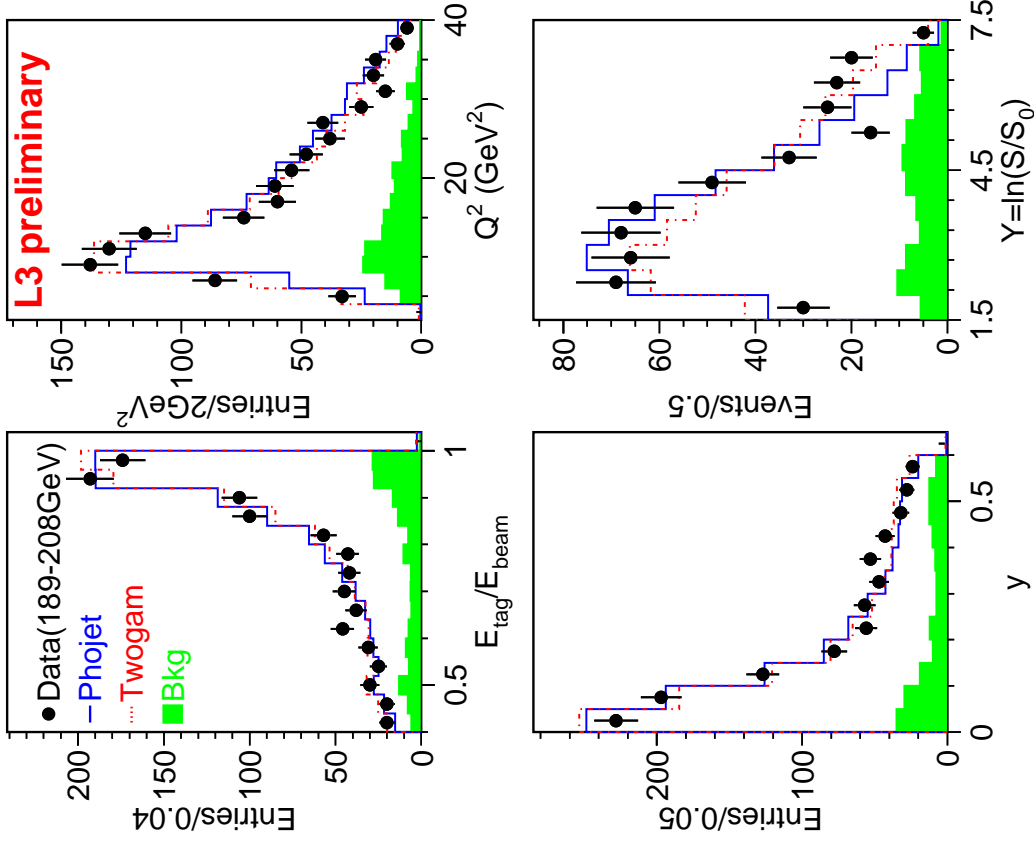


# $\sigma_{\gamma^*\gamma^*}$ from OPAL



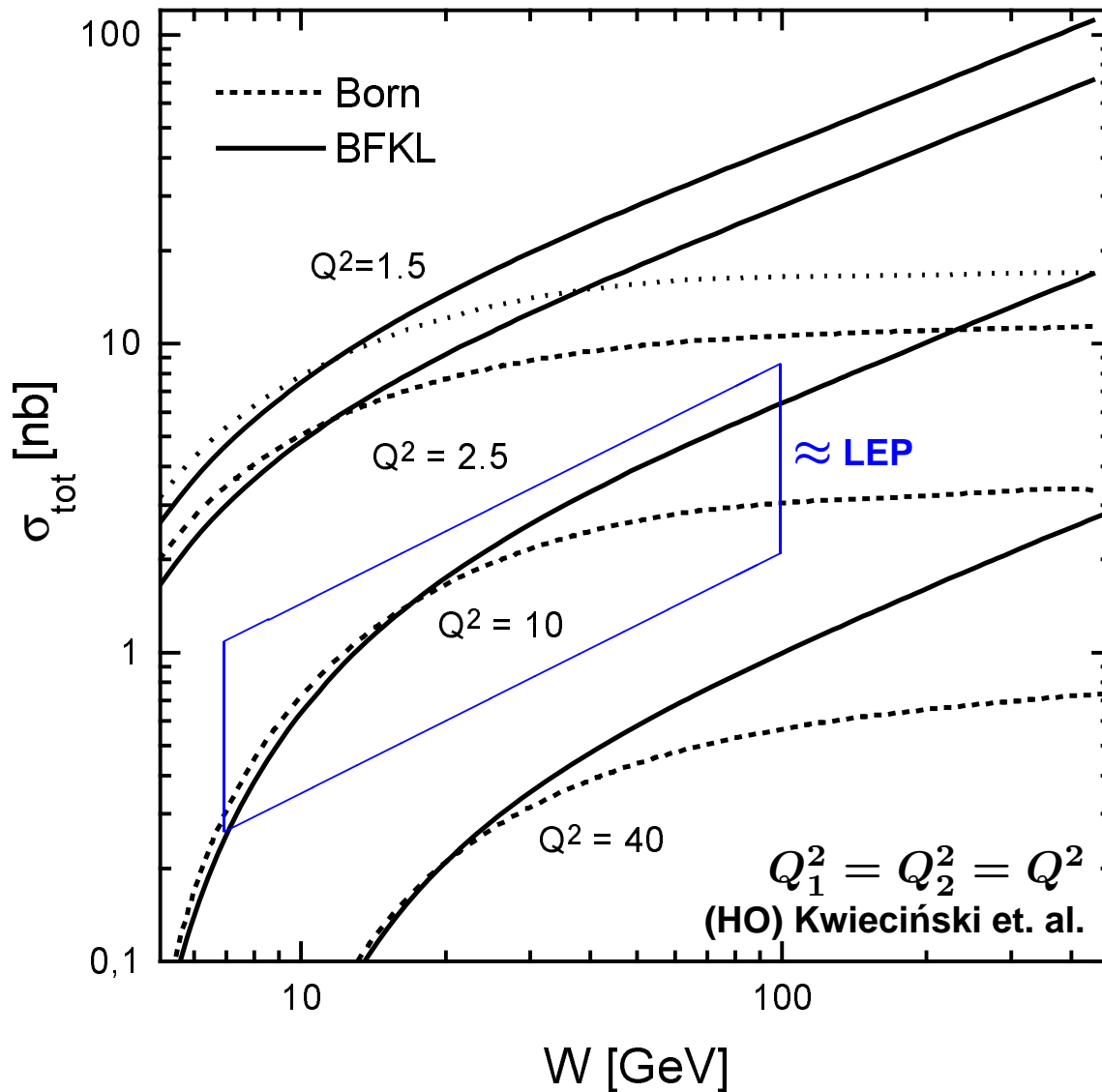
- 1) Bartels99  $\Rightarrow$  LO BFKL is too high.
- 2) Cacciari et. al  $\Rightarrow$  NLO DGLAP QCD is sufficient.
- 3) Kwiecinski et. al  $\Rightarrow$  HO BFKL also fits the data.

# Double tag hadronic cross-section from L3



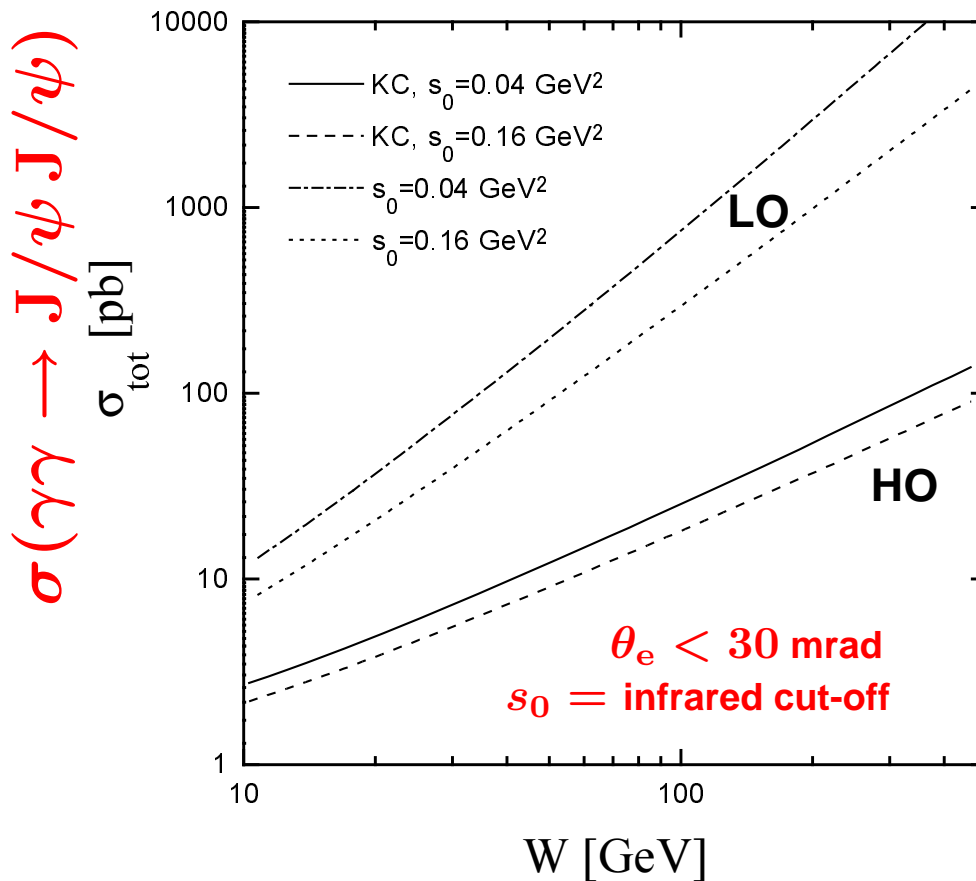
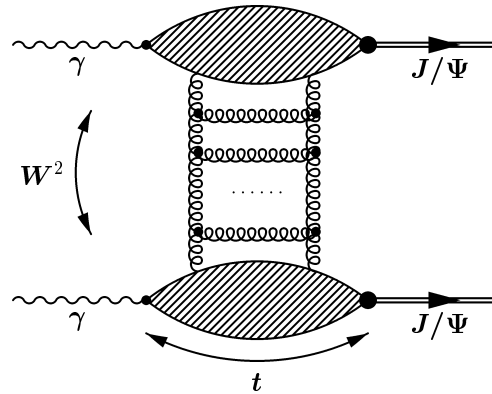
Some excess is seen at large  $Y$

## BFKL expectation for large $W$



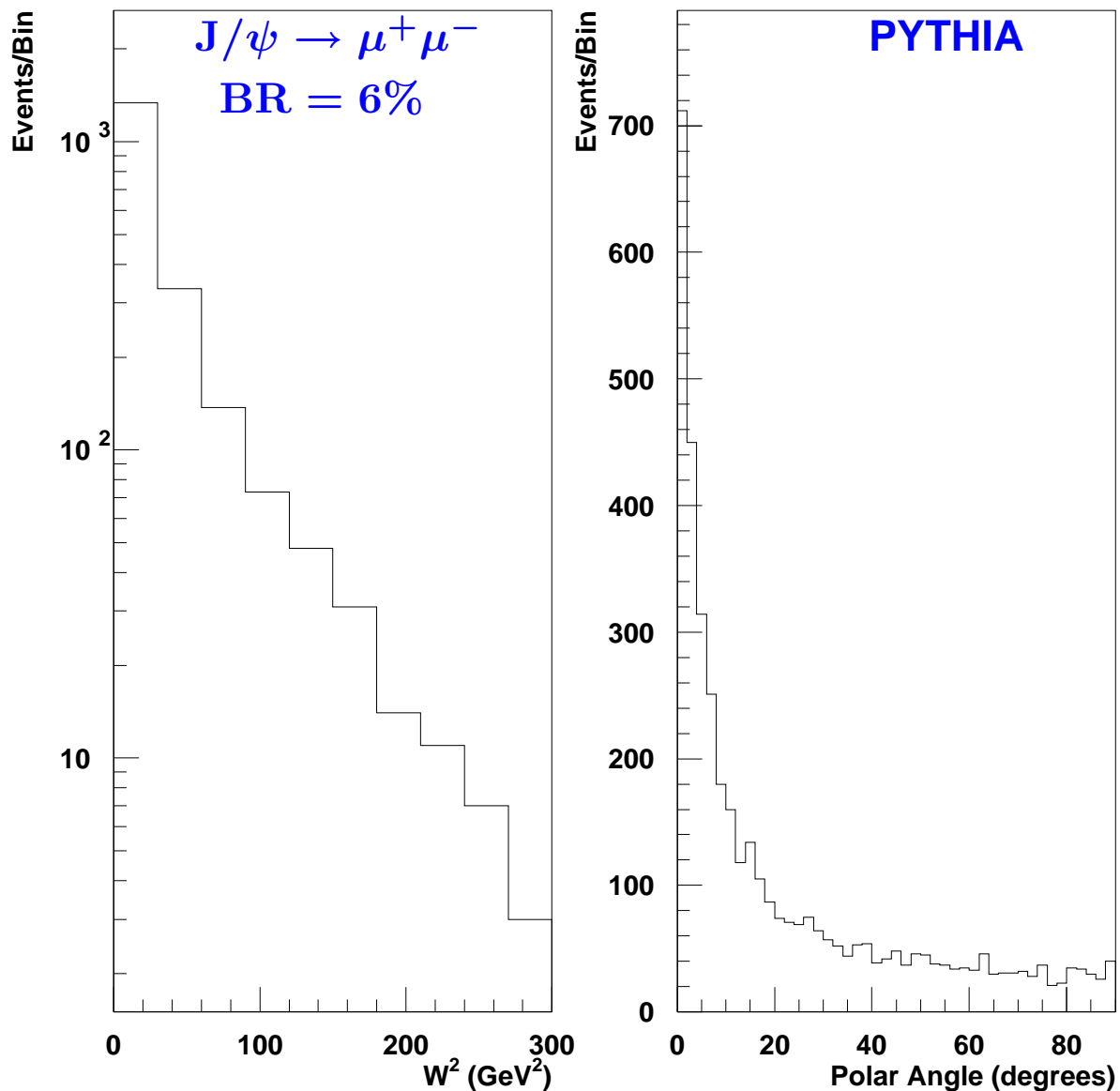
- 1) LEP probes the region for  $W$  up to about 100 GeV and  $\langle Q^2 \rangle \approx 15 \text{ GeV}^2$ .
- 2) The Linear Collider will extend the region to larger  $W^2$  for moderate  $Q^2$ , giving access to large  $Y$ .

# QCD Pomeron and $J/\psi$ production



$\sigma(e^+e^- \rightarrow e^+e^- J/\psi J/\psi) = 0.75 \text{ pb.}$   
 This yields 75k events for  $\mathcal{L}_{\text{int}} = 100 \text{ fb}^{-1}$ , but the  $J/\psi$  are mainly produced at low angles  $\Rightarrow$  acceptance?

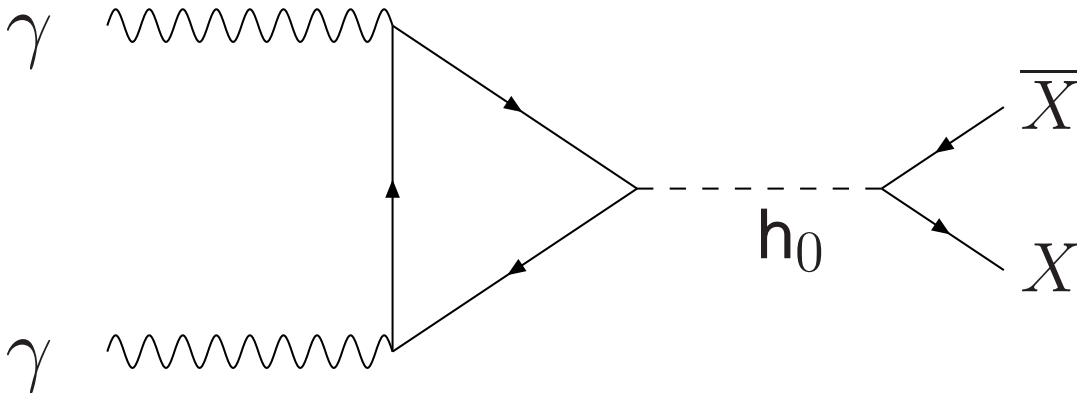
# Properties of $J/\psi \rightarrow 4\mu$



For  $p_\mu \geq 2$  GeV and  $\theta_\mu > 20/100/150$  mrad the acceptance is only 40/17/10%, which yields about 10-100 events for  $\mathcal{L}_{\text{int}} = 100 \text{ fb}^{-1}$ .

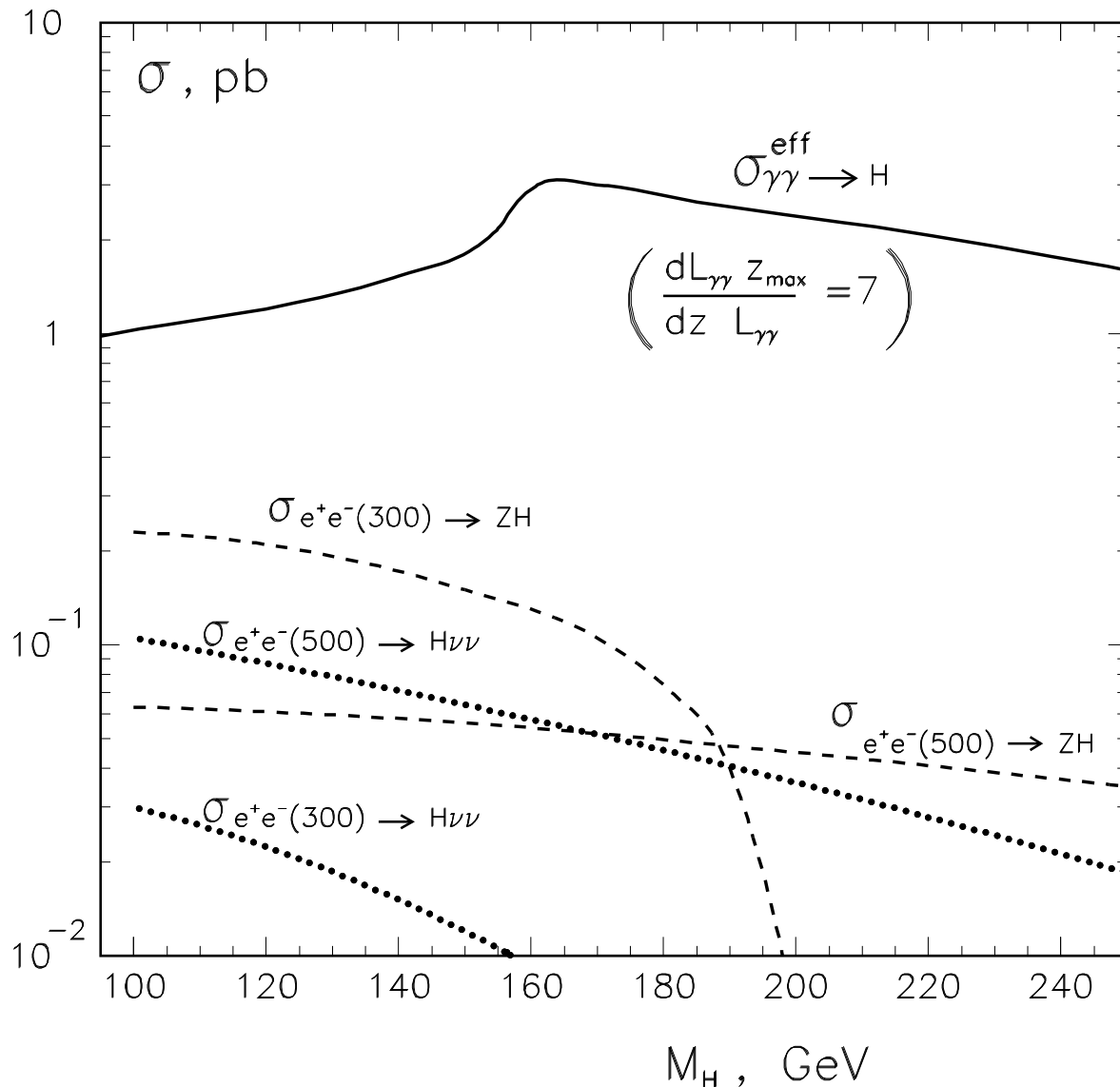
**With small acceptance and branching ratio a large luminosity is needed to observe the process.**

# Higgs search in $\gamma\gamma \rightarrow h_0 \rightarrow X\bar{X}$



1. The Higgs is produced as an s-channel resonance. A measurement of  $\Gamma(\gamma\gamma \rightarrow h_0)$  is very fundamental as it is sensitive to all charged particles in the loop which couple to the Higgs.
2. The required accuracy for  $\Gamma(\gamma\gamma \rightarrow h_0)$  is at the few percent level to be sensitive to new particles in the decoupling limit.
3. Combined measurements of  $\Gamma(\gamma\gamma \rightarrow h_0)$  and  $\text{BR}(h_0 \rightarrow \gamma\gamma)$  at the  $e^+e^-$  and  $\gamma\gamma$  collider provide a model independent measurement of the total width of the Higgs.

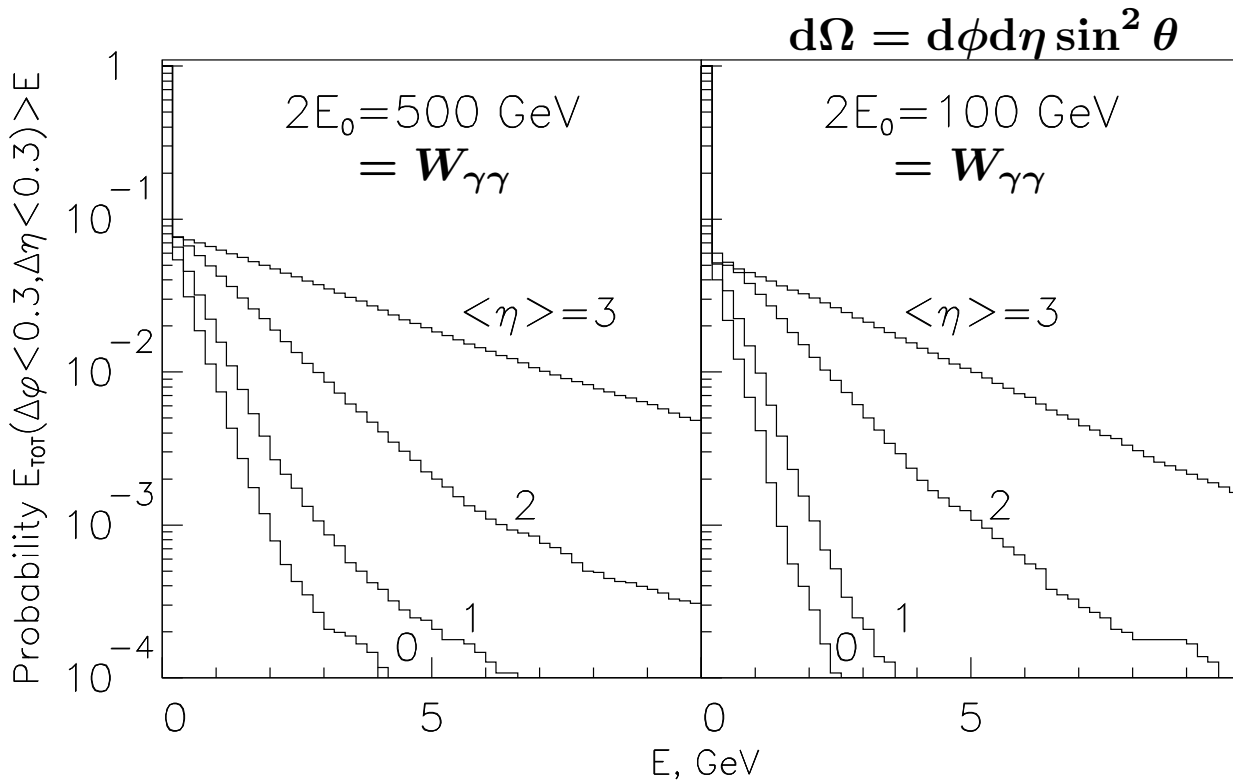
# Higgs production $\gamma\gamma \rightarrow h_0$



$$\sigma_{\gamma\gamma}^{\text{eff}} = \frac{dL_{\gamma\gamma}}{dW_{\gamma\gamma}} \frac{M_{h_0}}{L_{\gamma\gamma}} \frac{4\pi^2 \Gamma(\gamma\gamma \rightarrow h_0) (1 - \lambda_1 \lambda_2)}{M_{h_0}^3}$$

**Good prospects for  $\gamma\gamma$  production of Higgs bosons, because of the larger cross-section and the reach to higher masses than for  $e^+e^-$ .**

# $\gamma\gamma \rightarrow$ hadrons as underlying event



- 1) The energy resolution for a jet of 100 GeV energy is about 3 GeV.
- 2) Assuming two  $\gamma\gamma \rightarrow$  hadrons reactions per event, the probability to have an additional energy of 2 GeV in a jet at  $\eta = 0(2)$  is 1.5(60)%.
- 3) The background potentially degrades the mass resolution, especially at large rapidities, and most likely has to be measured directly from the data.

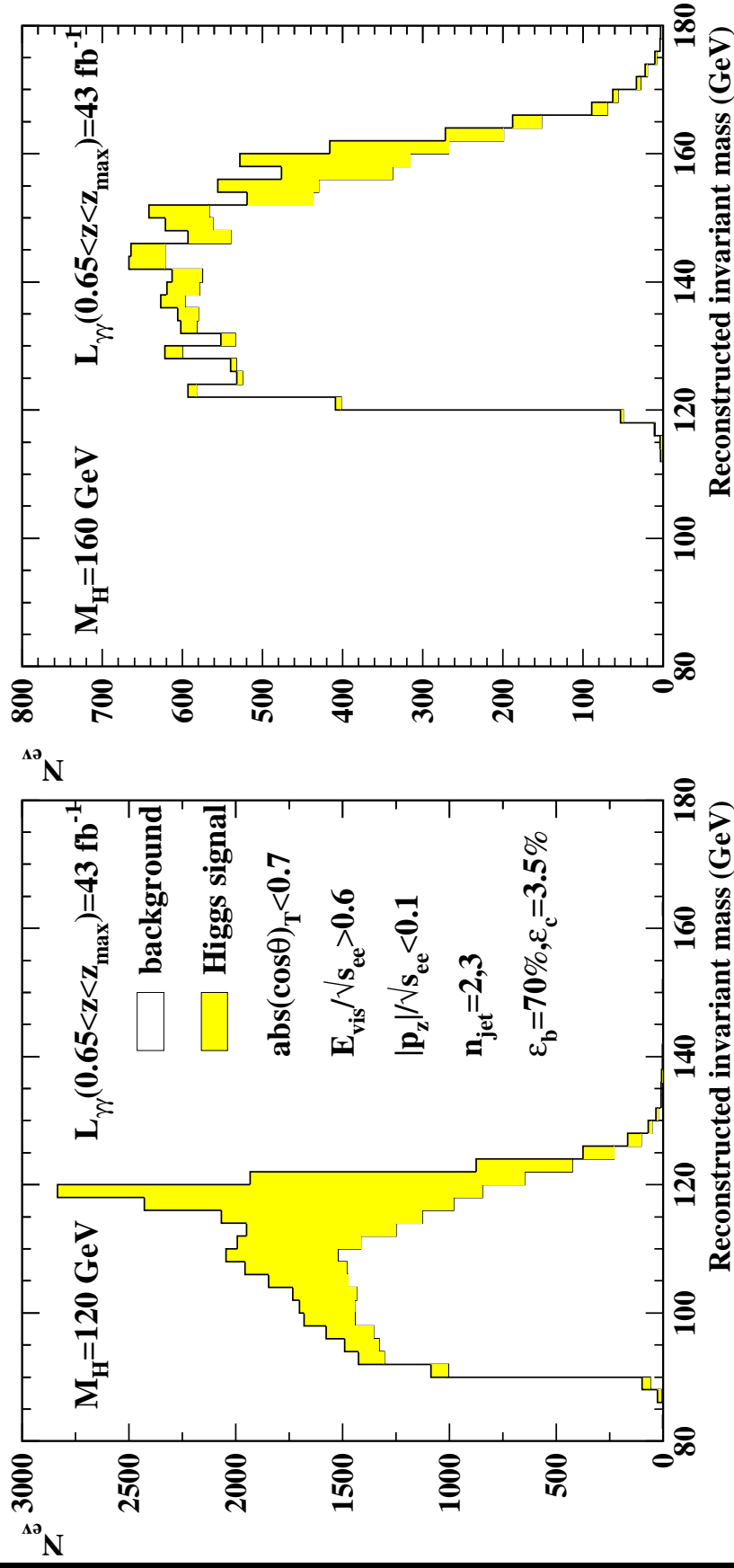


## The test case $\gamma\gamma \rightarrow h_0 \rightarrow b\bar{b}$

1. To reduce the continuum production of  $b\bar{b}$  and  $c\bar{c}$  one needs to select  $J_z = 0$ , because then  $\sigma(\gamma\gamma \rightarrow q\bar{q}) \propto m_q/W_{\gamma\gamma}$ .
2. In addition, good b tagging and c suppression is mandatory.
3. Assume 100% laser and 85% electron polarization and run the collider at  $\sqrt{s_{ee}} = M_{h_0}/0.8$  such that the Higgs mass corresponds to the peak of the  $\gamma\gamma$  luminosity spectrum.
4. Use additional cuts to further suppress the background.

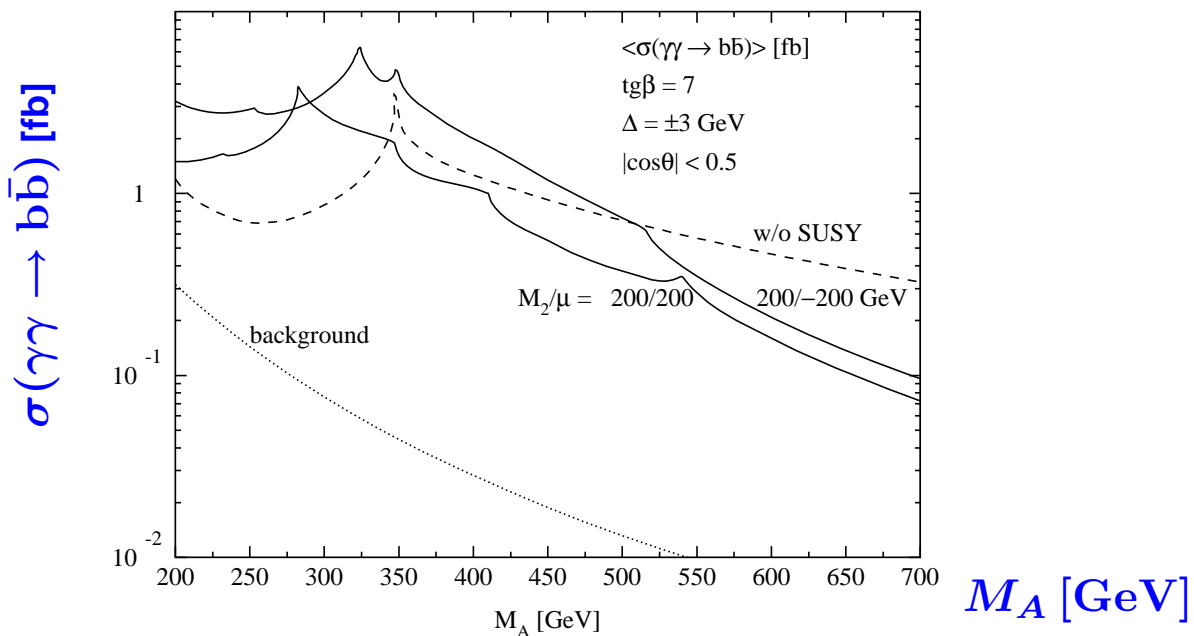
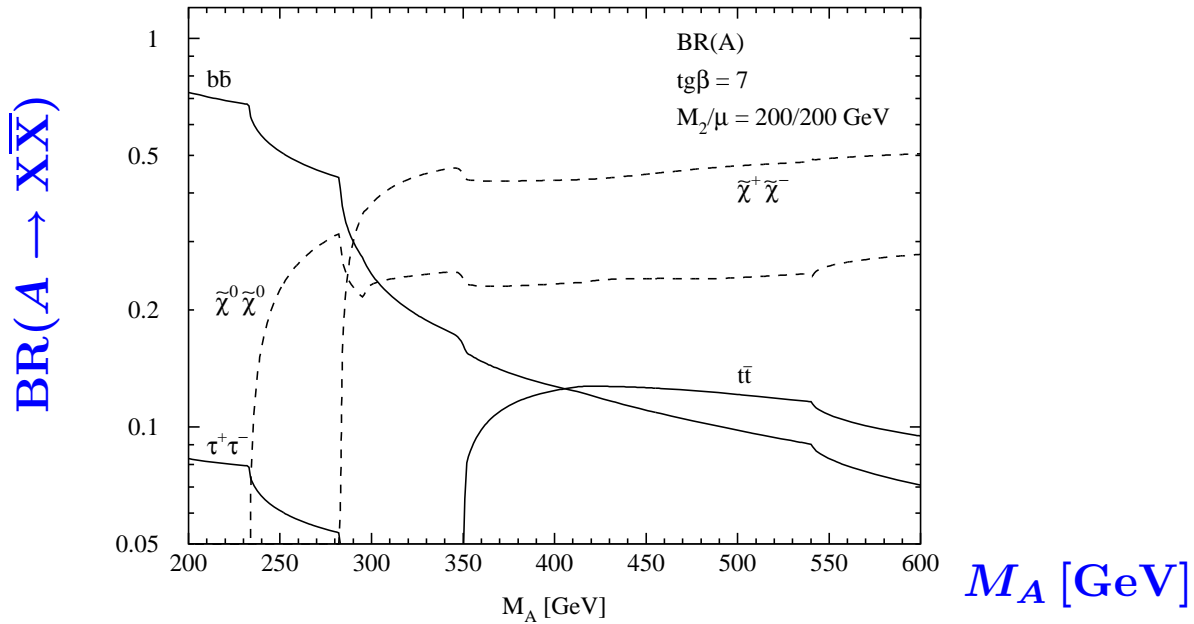
For  $L_{\gamma\gamma} = 43 \text{ fb}^{-1}$  in the peak, which means about  $400 \text{ fb}^{-1} e^+e^-$  luminosity,  $\Gamma(\gamma\gamma \rightarrow h_0)$  can be determined with a precision of about 2-10% in the mass range  $120 < M_{h_0} < 160 \text{ GeV}$ .

# Higgs reconstruction for $\gamma\gamma \rightarrow h_0 \rightarrow b\bar{b}$



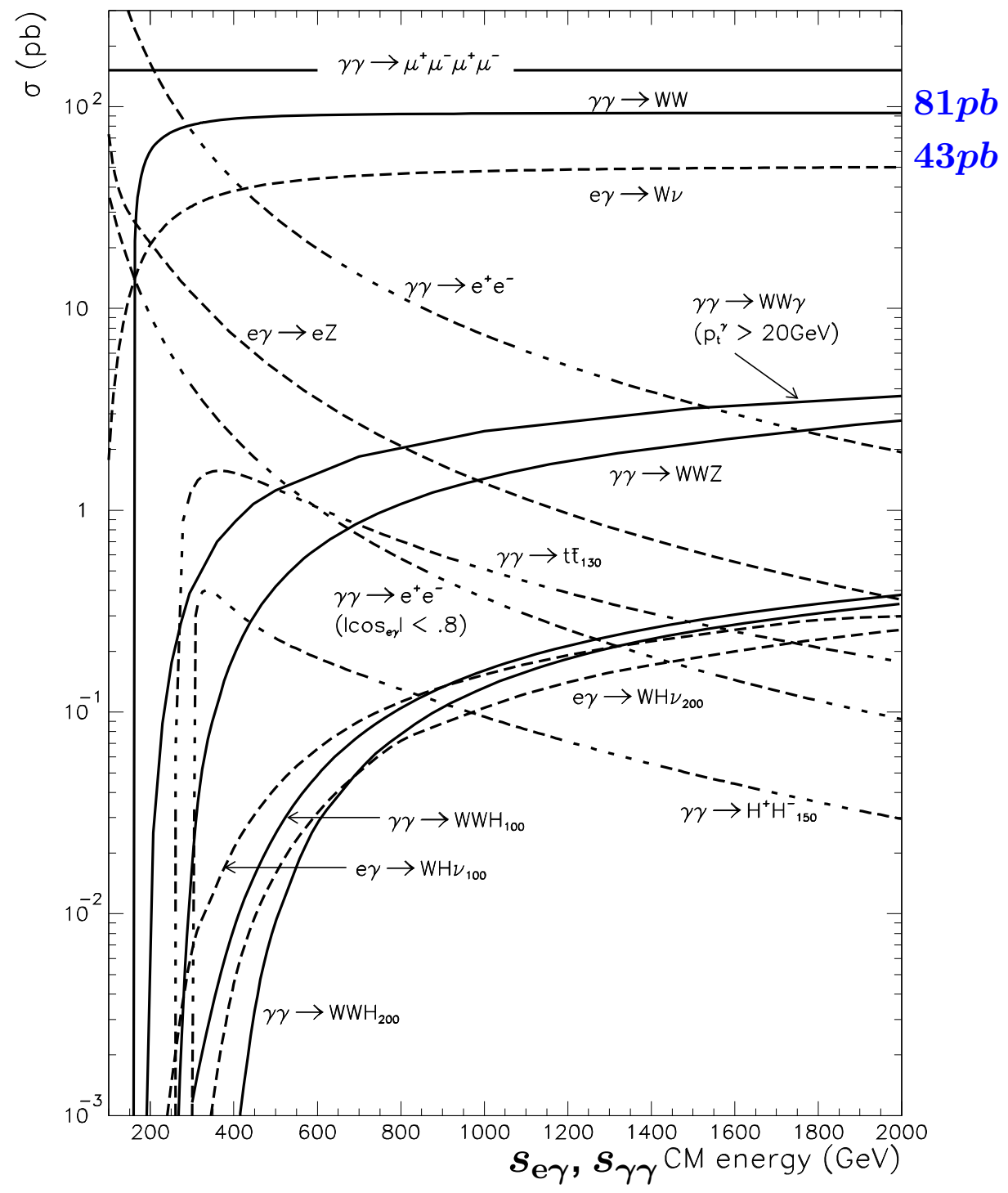
**Clear signals are observed, especially for low Higgs masses.**

# Search for MSSM Higgs bosons

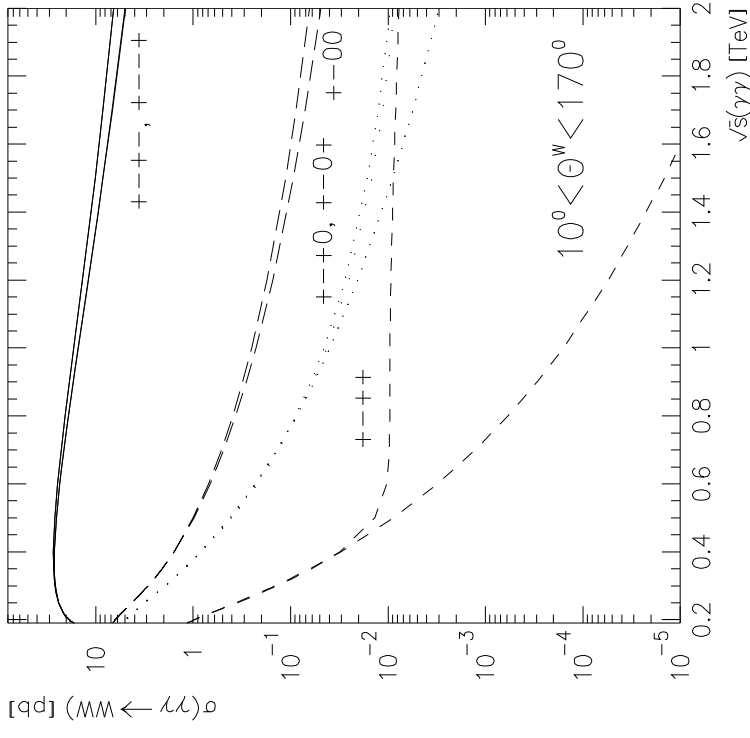
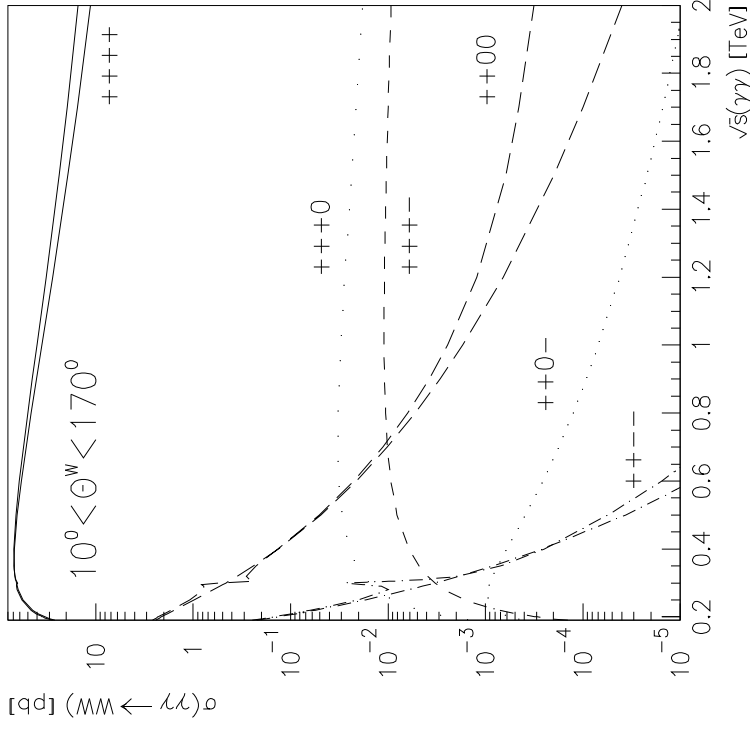


Good prospects for  $\gamma\gamma$  production of MSSM neutral Higgs bosons up to  $M_A = 400$  GeV in a region of parameter space where the LHC is blind [ $\tan(\beta) = 7, M_2/\mu = 200/200$  GeV].

# Some $\gamma\gamma$ and $e\gamma$ cross sections

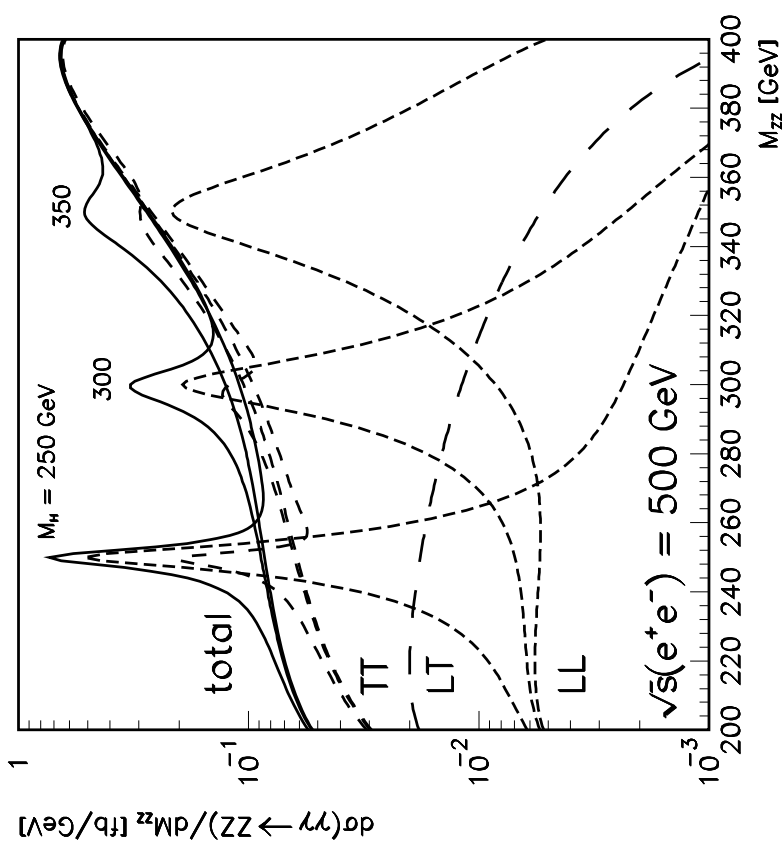
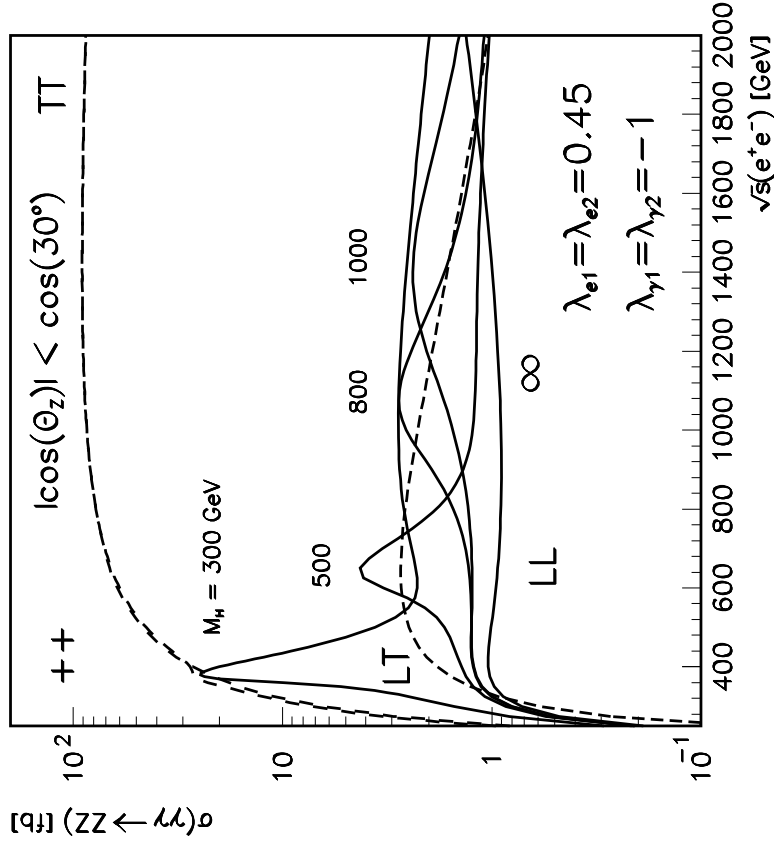


## The $WW(\gamma)$ final state



1. The  $\mathcal{O}(\alpha)$  cross-sections yield  $\sigma_{\gamma\gamma}(\sigma_{ee}) = 61$  (6.6) pb within cuts.
2. The radiative corrections are moderate but strongly depend on  $\theta^W$ .
3. About  $10^6$   $W^+W^-$  pairs per year are produced. A sample well suited for studies of anomalous couplings of the W.

# The production of $Z^0$ pairs at a Photon Collider



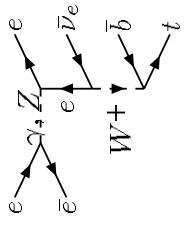
1. The cross-section strongly depend on the helicities of the  $Z$  bosons.
2. Higgs signals up to  $M_H = 350$  GeV can be observed, for higher masses the background from the continuum  $Z_T Z_T$  production is too high.

## The various options for single top production

reaction	no. of diagrams	polarization	$t\bar{t}$	$\sigma_{\text{top}}$ [fb]	
				0.5 TeV	1 TeV
$e^+e^- \rightarrow e^- \bar{\nu}_e t \bar{b}$	20	LR	yes	10.0	16.9
$\gamma\gamma \rightarrow e^- \bar{\nu}_e t \bar{b}$	21	++	yes	11.1	19.2
$e^-e^- \rightarrow e^- \nu_e \bar{t} b$	20	LL	no	2.6	19.1
$e^- \gamma \rightarrow \nu_e \bar{t} b$	4	L+	no	94.3	174.7

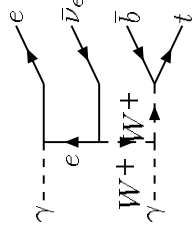
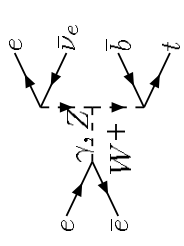
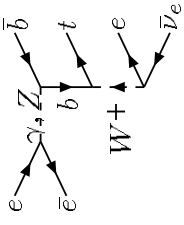
$e^- \gamma \rightarrow \nu_e \bar{t} b$  is the best option since it has the largest cross-section, no  $t\bar{t}$ -pair background and a high degree of polarization is possible. It has excellent sensitivity to  $V_{tb}$  and to anomalous couplings at the  $Wtb$  vertex.

# Diagrams for single top production



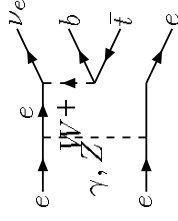
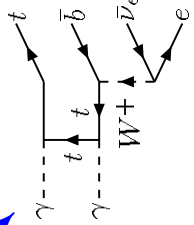
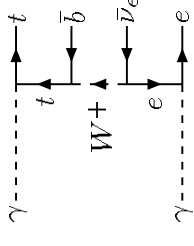
$e^+e^-:$

$N = 20$



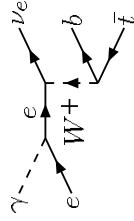
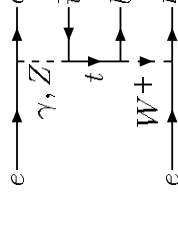
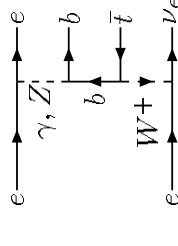
$\gamma\gamma:$

$N = 20$



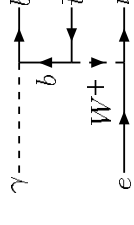
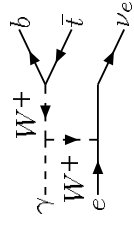
$e^-e^-:$

$N = 4$



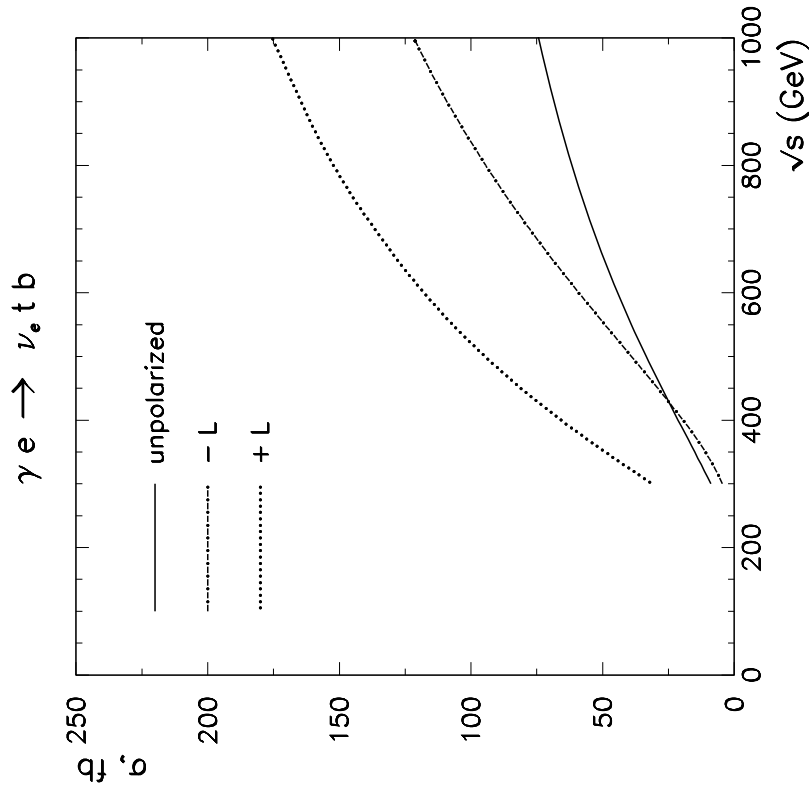
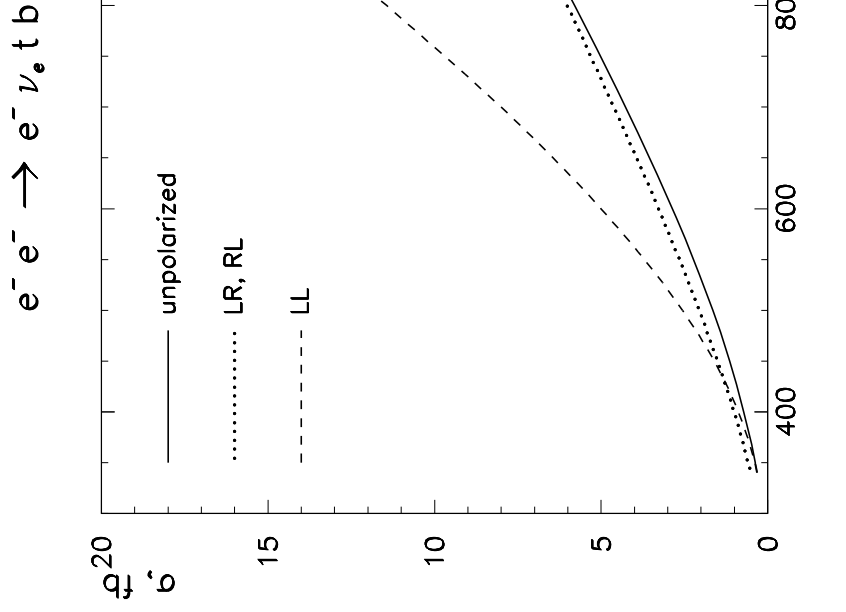
$e^-\gamma:$

$N = 21$





# Single top production



**For  $\mathcal{L}_{\text{int}} = 100 \text{ fb}^{-1}$  at  $\sqrt{s_{ee}} = 500 \text{ GeV}$ , the matrix element  $V_{tb}$  can be measured with 3.5% and 0.5% statistical precision for  $e^-e^- \rightarrow e^- \nu_e t b$  and  $e^- \gamma \rightarrow \nu_e t b$ .**

## Conclusion

1. The Linear Collider is an ideal tool to investigate photon–photon physics at the highest energies.
2. The tagging of electrons down to the lowest possible angles is a challenging task, but it is mandatory to achieve overlap with the results from LEP II in several areas, i.e. structure function measurements.
3. Due to the high centre-of-mass energy, especially in the Photon Collider mode, new channels (Higgs, W, Z<sup>0</sup>, LQ, ...) are open to be copiously produced.
4. For some of the reactions the Photon Collider extends the reach of a e<sup>+</sup>e<sup>-</sup> Collider significantly, and in some cases it is unique.

**Much work is ahead of us to bring a Linear Collider to life, but it should be fun and the physics potential is certainly worth the effort.**

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Slides: <http://home.cern.ch/nisius>