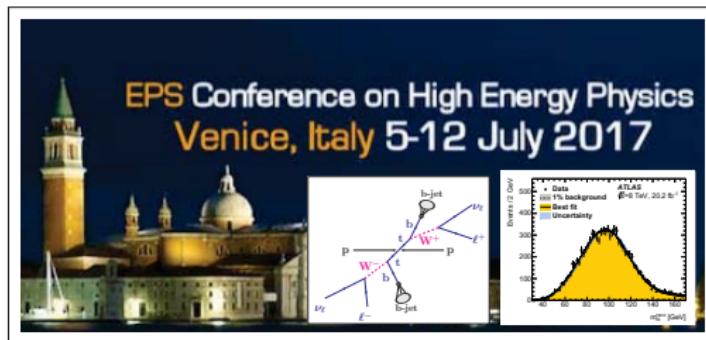


# Measurements of the top quark mass with the ATLAS detector



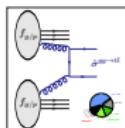
EPS 2017 Conference  
Venice, July 7, 2017



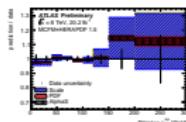
Richard Nisius (MPP München)  
for the ATLAS Collaboration



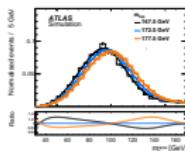
## The plan of this presentation



**Introduction**

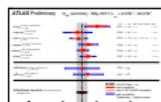


**Indirect determination of  $m_{\text{top}}^{\text{pole}}$**   
— Lepton differential distributions, [ATLAS-CONF-2017-044](#)



**Direct measurements of  $m_{\text{top}}$**

- All-jets channel, [arXiv:1702.07546](#)
- Lepton + jets channel, [Eur. Phys. J. C75 \(2015\) 330](#)
- Dilepton channel, [Phys. Lett. B761 \(2016\) 350](#)



**Combination of direct measurements**

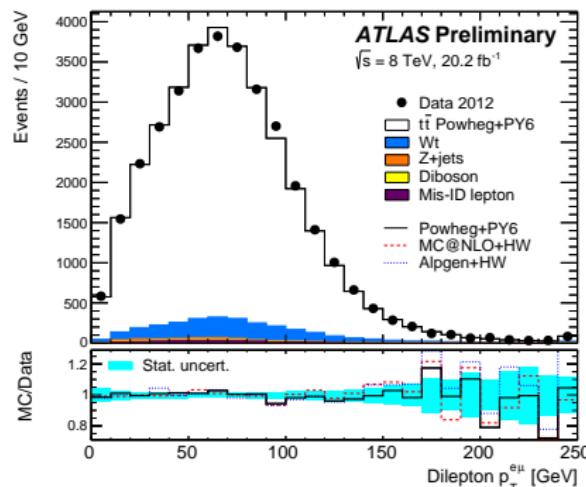
*The End*

**Conclusions**

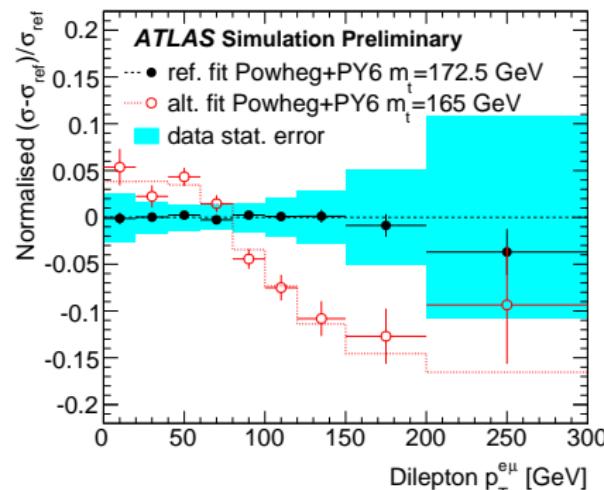
Note: - I cannot discuss in detail all displayed content, however, the main result figures have hyperlinks to the web page of the corresponding document.

# The lepton differential cross-sections from 8 TeV data

## An example compared to simulation



## The sensitivity of $p_T^{e\mu}$ to $m_{\text{top}}$

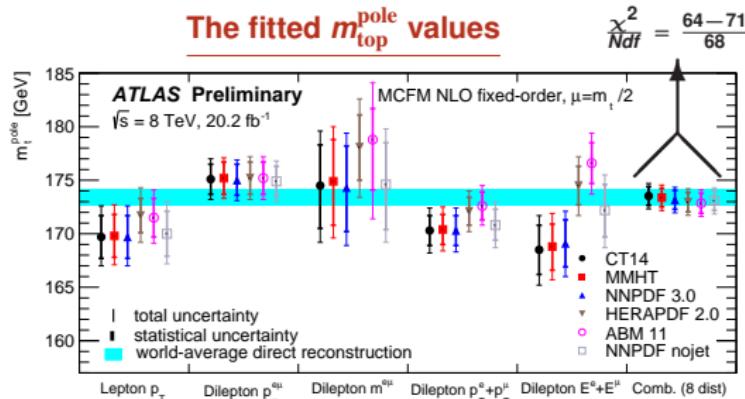
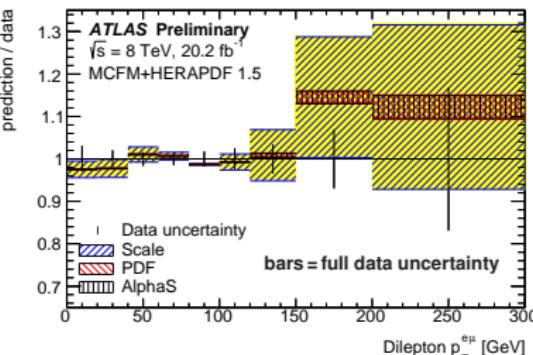


- Measure a number of lepton differential distributions in  $t\bar{t} \rightarrow e\mu + X$  events.
- Correct to stable particle level (using Powheg+Pythia6+CT10), subtract the background and convert into normalised lepton differential cross-sections  $\frac{1}{\sigma_x} \frac{d\sigma_x}{dx}$ .
- Clear sensitivity to  $m_{\text{top}}$  for  $x = p_T^e, p_T^{e\mu}, m^{e\mu}, p_T^e + p_T^\mu, E^e + E^\mu$ , but not for  $|\eta^e|, |y^{e\mu}|, \Delta\Phi^{e\mu}$ .

**The lepton differential cross-sections can be used to determine  $m_{\text{top}}$  or  $m_{\text{top}}^{\text{pole}}$ .**

# The $m_{\text{top}}^{\text{pole}}$ mass from lepton differential cross-sections

## Comparison to a fixed order prediction



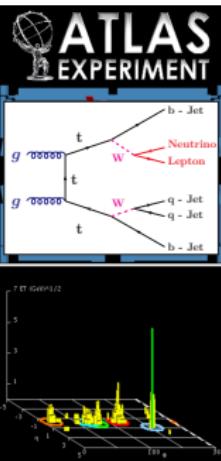
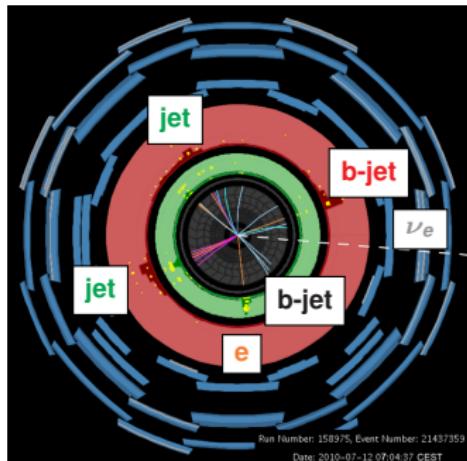
- Within the sizeable uncertainties, the fixed order prediction describes the data.
- The results in  $m_{\text{top}}^{\text{pole}}$  are from fits to individual distributions, or to all distributions (including  $|\eta^\ell|$ ,  $|y^{e\mu}|$ ,  $\Delta\Phi^{e\mu}$ ) while constraining the syst. uncertainties with nuisance parameters.
- The spread in the individual results is about 6 GeV. The combined result is:

$m_{\text{top}}^{\text{pole}} = 173.2 \pm 0.9 \text{ (stat.)} \pm 0.8 \text{ (syst.)} \pm 1.2 \text{ (theo.) GeV} = 173.2 \pm 1.6 \text{ GeV}$ . The theo. uncertainty is from PDF (0.3 GeV) and fixed vs. dynamic (e.g.  $\frac{E_T}{2}$ ) scale variations (1.1. GeV).

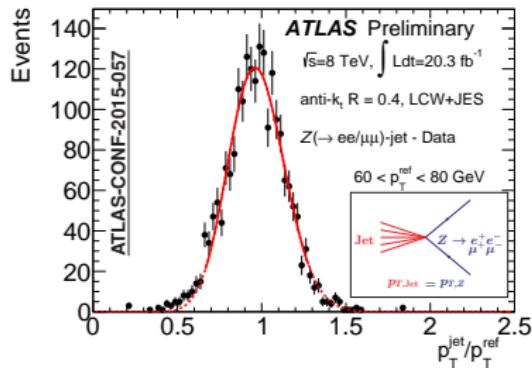
**The first measurement of  $m_{\text{top}}^{\text{pole}}$  using this method results in an uncertainty of 1.6 GeV.**

## The uncertainty in the jet energy scale (JES)

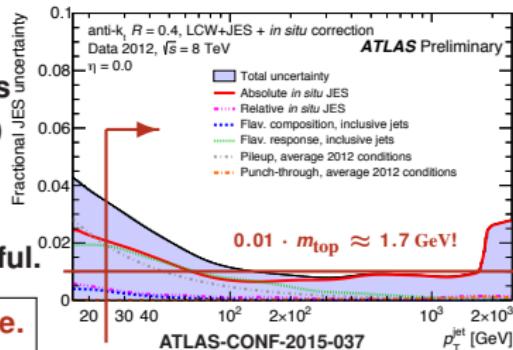
$t\bar{t} \rightarrow (b e \nu) (b q \bar{q})$ ,  $M(q\bar{q}) = m_W$ ,  $M(b\bar{q}q) = m_{top}$



### Calibration via $p_T$ -balance



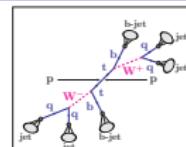
### JES uncertainty versus Jet- $p_T$



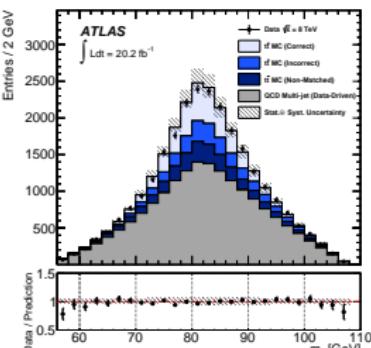
- Precise calibrations of the energy scale of inclusive jets (JES) and the relative  $b$ -to-light-jet energy scale (bJES) are vital for precise measurements of  $m_{top}$ .
- For high precision in  $m_{top}$  the possibility of in-situ calibrations of the mean JES and bJES are extremely helpful.

A small JES-induced uncertainty in  $m_{top}$  is indispensable.

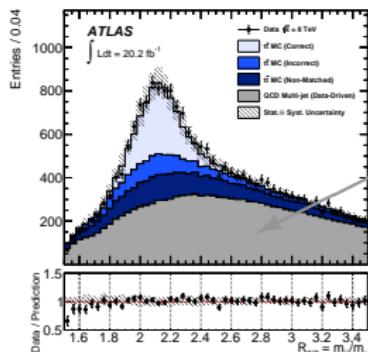
## Measurement in the all-jets channel from 8 TeV data



### The $m_{jj}$ distribution

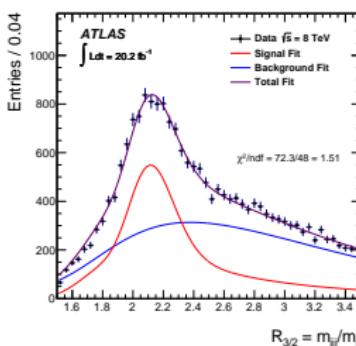


### The $R_{32}$ distribution



### Some analysis details

- The number of  $b$ -tagged jets amongst the six leading jets and  $\langle \Delta\Phi(b, W) \rangle$  in the signal and three control regions are used to determine the shape of the background distributions from data.
- Choosing the  $R_{32} = \frac{m_{jj}}{m_{jj}} = \frac{m_{bqq}}{m_{qq}}$  distribution (with an ATLAS Exp. expected 'peak' at  $\frac{172.84}{80.37} = 2.15$ ) stabilises  $m_{top}$  against a global JES uncertainty.



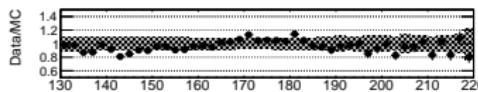
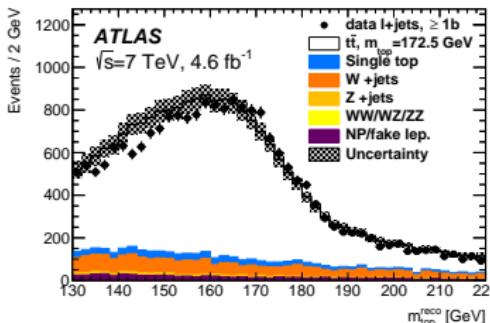
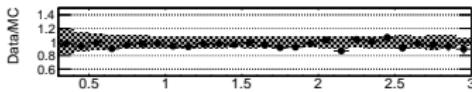
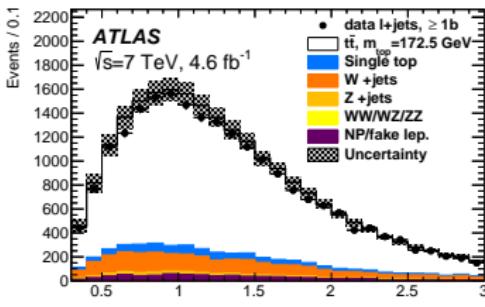
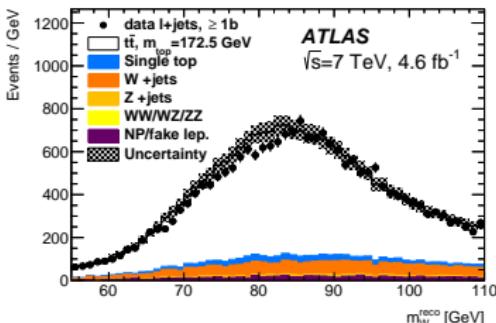
### The result from the fit to data

- $m_{top} = 173.72 \pm 0.55 \text{ (stat)} \pm 1.01 \text{ (syst)} \text{ GeV}$
- Most important systematic uncertainties: JES (0.60 GeV), bJES (0.34 GeV) and hadronisation (0.64 GeV).
- The summary so far:

Channel ( $\sqrt{s}$ )	Stat	Model	Background	Experimental
All-jets (8)	$0.55$	$0.70 \pm 0.16$	$0.19$	$0.71 \pm 0.04$

An about 40% improvement compared to the 7 TeV analysis.

## Three-dimensional lepton + jets analysis from 7 TeV data

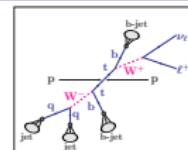


$$1. \quad m_{top}^{\text{reco}} = f(m_{top}, \text{JSF}, \text{bJSF}).$$

$$2. \quad m_W^{\text{reco}} = f(\text{JSF}).$$

$$3. \quad R_{bq}^{\text{reco}} = f(\text{bJSF}) \text{ with a weak } m_{top} \text{ dependence.}$$

- The 2D ( $m_{top}^{\text{reco}}, m_W^{\text{reco}}$ ) or 3D ( $+R_{bq}^{\text{reco}}$ ) template fit reduces the JES and bJES induced uncertainties in  $m_{top}$ .
- Since the JSF and bJSF are global, but JES and bJES are  $f(p_t, \eta)$ , residual uncertainties remain.



### The analysis idea

– (b)JSF = (b)Jet Scale Factor to obtain scaled jets

$$p'_t(q) = \text{JSF} \cdot p_t(q)$$

$$p'_t(b) = \text{JSF} \cdot \text{bJSF} \cdot p_t(b)$$

– Additional dimensions

$$2. \quad m_W^{\text{reco}} = 2E_1 E_2 (1 - \cos\theta_{12}) \\ \propto \text{JSF}^2$$

$$3. \quad R_{bq}^{\text{reco}} = \frac{\sum p_t(b)}{\sum p_t(q)} \\ \propto \frac{\text{bJSF} \cdot \text{JSF}}{\text{JSF}} = \text{bJSF}$$

This is the first 3D  $m_{top}$  analysis worldwide.

## The list of systematic uncertainties

		$t\bar{t} \rightarrow \text{lepton+jets}$		
		$m_{\text{top}}^{\ell+\text{jets}}$ [GeV]	JSF	bJSF
Results		172.33	1.019	1.003
Statistics		0.75	0.003	0.008
– Stat. comp. ( $m_{\text{top}}$ )		0.23	n/a	n/a
– Stat. comp. (JSF)		0.25	0.003	n/a
– Stat. comp. (bJSF)		0.67	0.000	0.008
Method		$0.11 \pm 0.10$	0.001	0.001
Signal MC		$0.22 \pm 0.21$	0.004	0.002
Hadronisation		$0.18 \pm 0.12$	0.007	0.013
ISR/FSR		$0.32 \pm 0.06$	0.017	0.007
Underlying event		$0.15 \pm 0.07$	0.001	0.003
Colour reconnection		$0.11 \pm 0.07$	0.001	0.002
PDF		$0.25 \pm 0.00$	0.001	0.002
W/Z+jets norm		0.02 ± 0.00	0.000	0.000
W/Z+jets shape		0.29 ± 0.00	0.000	0.004
NP/fake-lepton norm.		0.10 ± 0.00	0.000	0.001
NP/fake-lepton shape		0.05 ± 0.00	0.000	0.001
Jet energy scale		0.58 ± 0.11	0.018	0.009
<i>b</i> -Jet energy scale		<u>0.06 ± 0.03</u>	0.000	0.010
Jet resolution		0.22 ± 0.11	0.007	0.001
Jet efficiency		0.12 ± 0.00	0.000	0.002
Jet vertex fraction		0.01 ± 0.00	0.000	0.000
<i>b</i> -Tagging		0.50 ± 0.00	0.001	0.007
$E_T^{\text{miss}}$		0.15 ± 0.04	0.000	0.001
Leptons		0.04 ± 0.00	0.001	0.001
Pile-up		0.02 ± 0.01	0.000	0.000
Total		1.27 ± 0.33	0.027	0.024

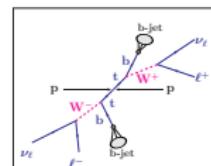
- The third dimensions reduces the bJES induced uncertainty in  $m_{\text{top}}$  from 0.88 to  $\sqrt{0.67^2 + 0.06^2} = 0.67$ , but now it is mostly statistical.
- As a side effect a number of MC modelling uncertainties are reduced as well. This is because a different bJSF better accounts for the MC differences than a different  $m_{\text{top}}$ .
- The uncertainty in  $m_{\text{top}}$  is back to being dominated by the JES induced uncertainty.

– The summary so far:

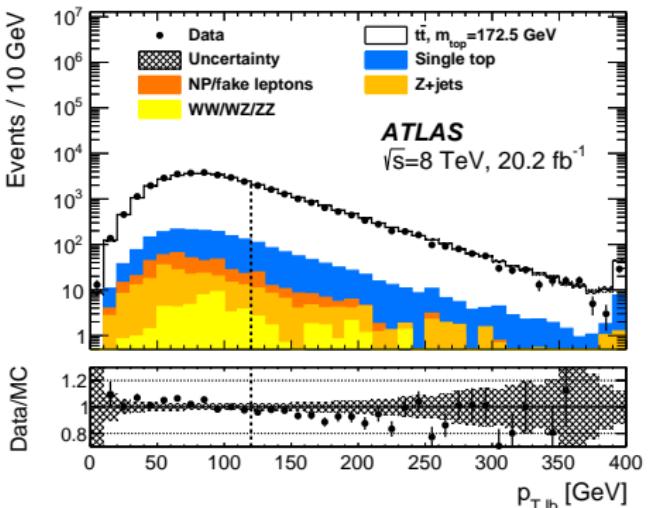
Channel ( $\sqrt{s}$ )	Stat	Model	Background	Experimental
All jets (8)	0.55	$0.70 \pm 0.16$	0.19	$0.71 \pm 0.04$
Lepton + jets (7)	0.75	$0.53 \pm 0.11$	$0.31 \pm 0.00$	$0.82 \pm 0.08$

In this channel, the bJES induced uncertainty has finally lost its fright.

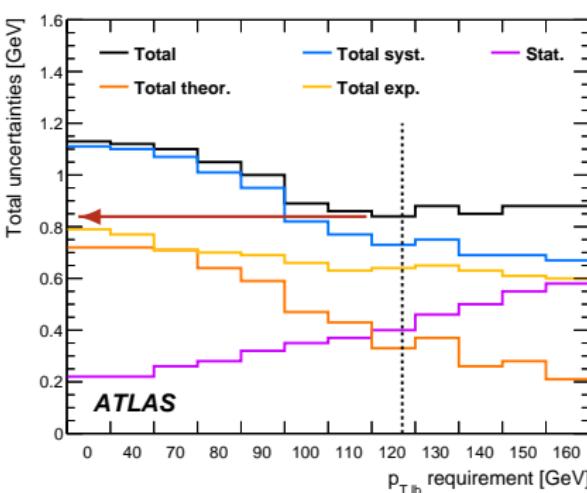
## Optimisation in the dilepton channel from 8 TeV data



### The $p_{T,\ell b}$ distribution



### Uncertainty vs. $p_{T,\ell b}$



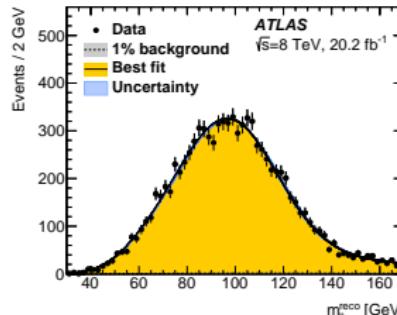
- The variable  $p_{T,\ell b}$  denotes the mean  $p_T$  of the two lepton– $b$ -jet pairs.
- The data-to-MC difference in  $p_{T,\ell b}$  is covered by the hadronisation uncertainty (backup).
- Using  $p_{T,\ell b} > 120 \text{ GeV}$  results in the smallest total uncertainty  $\Rightarrow$  final selection.

**The optimisation significantly reduces the total uncertainty.**

## The result from 8 TeV data

	$\sqrt{s} = 7 \text{ TeV}$	$\sqrt{s} = 8 \text{ TeV}$	
	$m_{\text{top}}^{\ell+\text{jets}}$ [GeV]	$m_{\text{top}}^{\text{dil}}$ [GeV]	$m_{\text{top}}^{\text{dil}}$ [GeV]
Results	172.33	173.79	172.99
Statistics	0.75	0.54	0.41
Method	$0.11 \pm 0.10$	$0.09 \pm 0.07$	$0.05 \pm 0.07$
Signal Monte Carlo generator	$0.22 \pm 0.21$	$0.26 \pm 0.16$	$0.09 \pm 0.15$
Hadronisation	$0.18 \pm 0.12$	$0.53 \pm 0.09$	$0.22 \pm 0.09$
Initial- and final-state QCD radiation	$0.32 \pm 0.06$	$0.47 \pm 0.05$	$0.23 \pm 0.07$
Underlying event	$0.15 \pm 0.07$	$0.05 \pm 0.05$	$0.10 \pm 0.14$
Colour reconnection	$0.11 \pm 0.07$	$0.14 \pm 0.05$	$0.03 \pm 0.14$
Parton distribution function	$0.25 \pm 0.00$	$0.11 \pm 0.00$	$0.05 \pm 0.00$
Background normalisation	$0.10 \pm 0.00$	$0.04 \pm 0.00$	$0.03 \pm 0.00$
$W/Z+\text{jets}$ shape	$0.29 \pm 0.00$	$0.00 \pm 0.00$	0
Fake leptons shape	$0.05 \pm 0.00$	$0.01 \pm 0.00$	$0.08 \pm 0.00$
Jet energy scale	$0.58 \pm 0.11$	$0.75 \pm 0.08$	$0.54 \pm 0.04$
Relative $b$ -to-light-jet energy scale	$0.06 \pm 0.03$	$0.68 \pm 0.02$	$0.30 \pm 0.01$
Jet energy resolution	$0.22 \pm 0.11$	$0.19 \pm 0.04$	$0.09 \pm 0.05$
Jet reconstruction efficiency	$0.12 \pm 0.00$	$0.07 \pm 0.00$	$0.01 \pm 0.00$
Jet vertex fraction	$0.01 \pm 0.00$	$0.00 \pm 0.00$	$0.02 \pm 0.00$
$b$ -tagging	$0.50 \pm 0.00$	$0.07 \pm 0.00$	$0.03 \pm 0.02$
Leptons	$0.04 \pm 0.00$	$0.13 \pm 0.00$	$0.14 \pm 0.01$
$E_T^{\text{miss}}$	$0.15 \pm 0.04$	$0.04 \pm 0.03$	$0.01 \pm 0.01$
Pile-up	$0.02 \pm 0.01$	$0.01 \pm 0.00$	$0.05 \pm 0.01$
Total systematic uncertainty	$1.03 \pm 0.31$	$1.31 \pm 0.23$	$0.74 \pm 0.29$
Total	$1.27 \pm 0.33$	$1.41 \pm 0.24$	$0.84 \pm 0.29$

**Look at these lines on next slide**



- Largest experimental uncertainties stem from the jet energy scales.
- Largest modelling uncertainties are due to Hadronisation and ISR/FSR.
- The correlations of the estimators for all sources of systematic uncertainty are evaluated rather than assigned (as is commonly done).

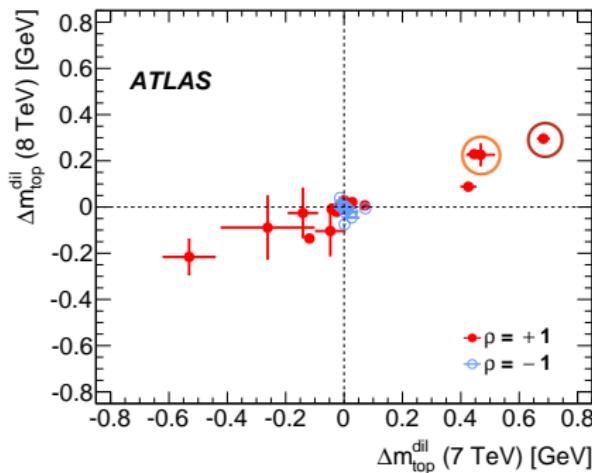
### — The summary:

Channel ( $\sqrt{s}$ )	Value	Stat	Model	Background	Experimental	Total
All-jets (8)	173.72	0.55	$0.70 \pm 0.16$	0.19	$0.71 \pm 0.04$	1.15 (0.66 %)
Lepton + jets (7)	172.33	0.75	$0.53 \pm 0.11$	$0.31 \pm 0.00$	$0.82 \pm 0.08$	1.27 (0.74 %)
Dilepton (8)	172.99	0.41	$0.35 \pm 0.09$	$0.08 \pm 0.01$	$0.64 \pm 0.04$	0.85 (0.49 %)

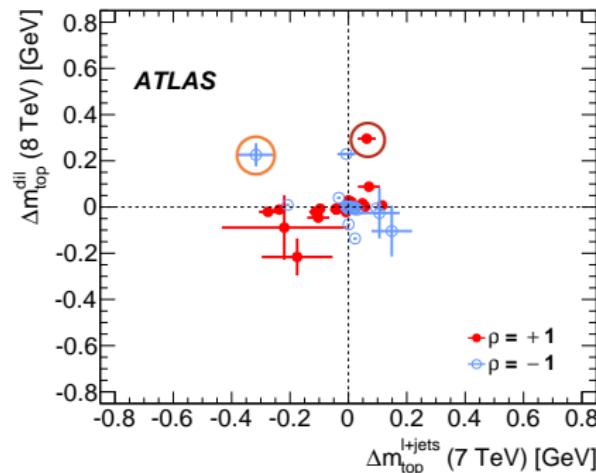
This is the most precise ATLAS measurement and the most precise result in this channel.

## The correlations of the estimators for individual sources

Dilepton 7 vs. dilepton 8 TeV



Lepton + jets, 7 vs. dilepton 8 TeV



- $\Delta m$  = shift in mass from pairs of samples using 500 pseudo-experiments of the data size.
- Each point corresponds to a single (sub-) component, with  $p = +1$  or  $p = -1$ .

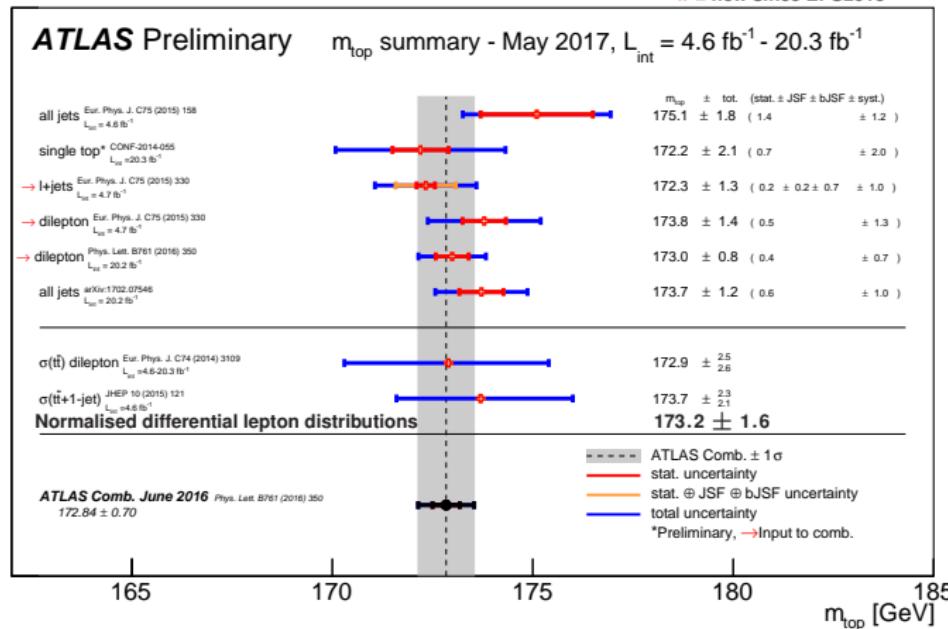
bJES:  $0.30 \pm 0.01$  (dil, 8),  $0.68 \pm 0.02$  (dil, 7,  $p = +1$ ),  $0.06 \pm 0.03$  ( $\ell + \text{jets}$ , 7,  $p = +1$ ).

ISR/FSR:  $0.23 \pm 0.07$  (dil, 8),  $0.47 \pm 0.05$  (dil, 7,  $p = +1$ ),  $0.32 \pm 0.06$  ( $\ell + \text{jets}$ , 7,  $p = -1$ ).

**By construction, the correlations to the three-dimensional lepton + jets analysis are small.**

# The ATLAS measurements of $m_{\text{top}}$ and $m_{\text{top}}^{\text{pole}}$

★ = new since EPS2015



– The combination of three ATLAS measurements results in:

$$m_{\text{top}} = 172.84 \pm 0.34 \text{ (stat)} \pm 0.61 \text{ (syst)} \text{ GeV} = 172.84 \pm 0.70 \text{ GeV (0.40%).}$$

**The direct measurements are superior in determining  $m_{\text{top}}$ .**

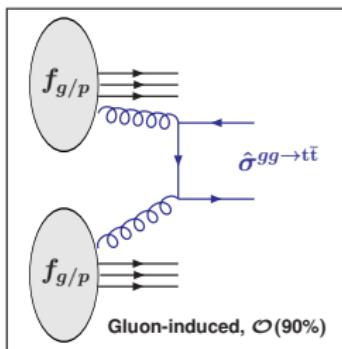
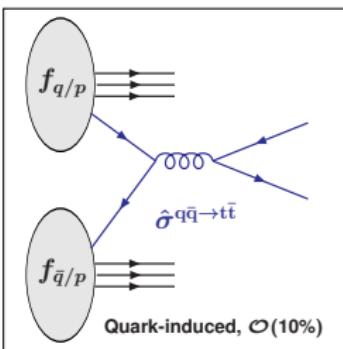
## Conclusions

- ATLAS has performed various  $m_{\text{top}}^{\text{pole}}$  measurements based on novel methods, e.g. by using  $t\bar{t} + 1\text{-jet events}$  and differential distributions of leptonic variables .
- Compared to direct measurements of  $m_{\text{top}}$ , these  $m_{\text{top}}^{\text{pole}}$  determinations are performed in a well-defined renormalisation scheme, but suffer from larger uncertainties.
- The top quark  $m_{\text{top}}$  mass was directly measured in all  $t\bar{t}$  decay channels.
- The dilepton result:  $m_{\text{top}} = 172.99 \pm 0.41 \text{ (stat)} \pm 0.74 \text{ (syst)} \text{ GeV} = 172.99 \pm 0.84 \text{ GeV}$ , is the most precise ATLAS measurement and the most precise in this channel to date.
- The largest experimental uncertainties stem from the calibration of the jet energy scales.
- The largest modelling uncertainties are due to Hadronisation and ISR/FSR radiation.
- For the combination of this result with other measurements the correlations of the estimators for all sources of systematic uncertainty are evaluated rather than assigned.
- The result is:  $m_{\text{top}} = 172.84 \pm 0.34 \text{ (stat)} \pm 0.61 \text{ (syst)} \text{ GeV} = 172.84 \pm 0.70 \text{ GeV}$ .

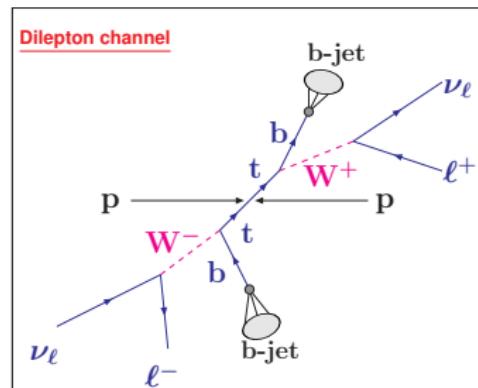
# Backup - Transparencies

## Production and decay of top-quark pairs

### Production processes



### Decay channels ( $V_{tb} \approx 1$ )

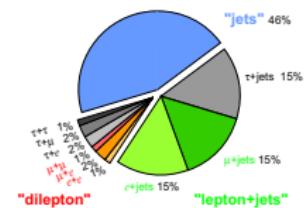


– For  $m_{top} = 172.5$  GeV and  $\sqrt{s} = 8$  TeV, the cross-section is  $\sigma(t\bar{t}) = 253^{+13}_{-15}$  pb, resulting in 250k events per 1/fb.

All-jets: highest rate  $\mathcal{O}(46\%)$ , but largest background.

Lepton + jets: medium rate  $\mathcal{O}(30\%)$ , lepton 'tag', good compromise.

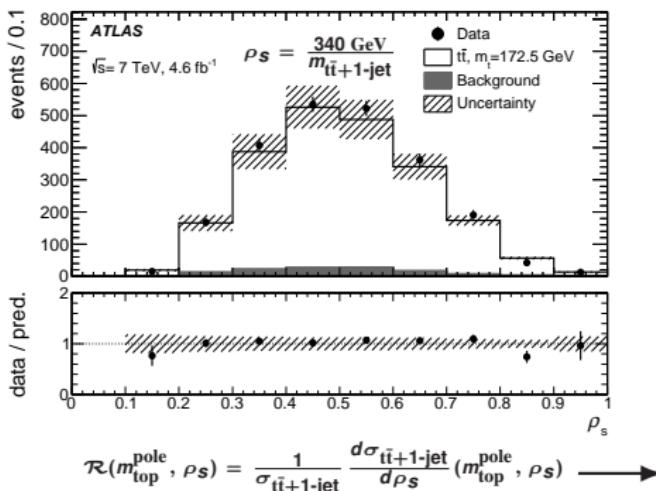
Dilepton: lowest rate  $\mathcal{O}(4\%)$ , high purity, incomplete kinematics.



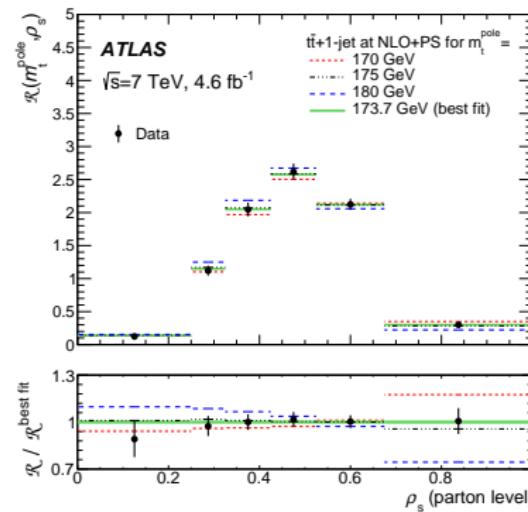
The LHC is a top quark factory. In all channels, the systematic uncertainties matter most.

# $m_{\text{top}}^{\text{pole}}$ from the normalised differential $t\bar{t} + 1\text{-jet}$ cross-section

## The data distribution



## The unfolded distribution



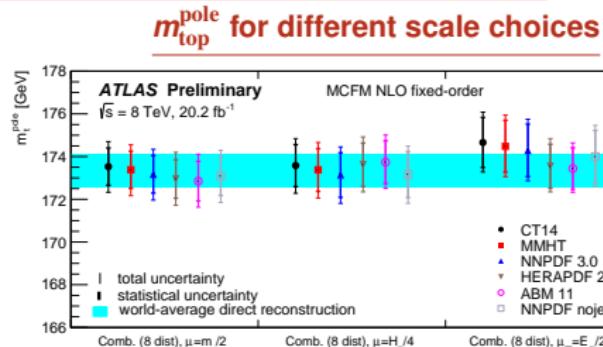
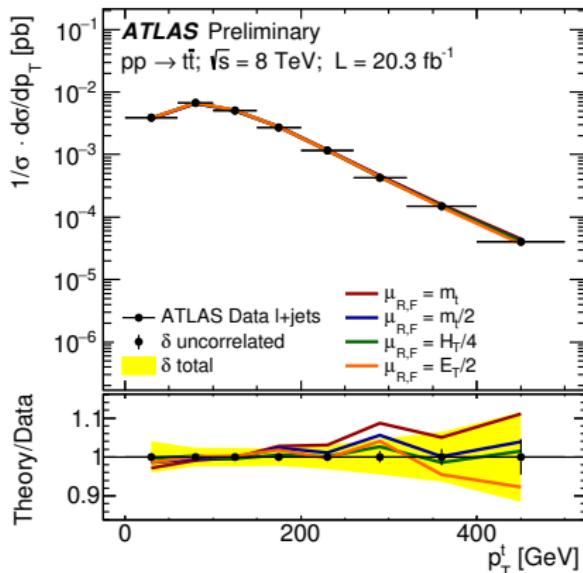
Largest sensitivity is close to threshold

- Measure distribution of  $t\bar{t} + 1\text{-jet}$  events in the lepton + jets channel in 7 TeV data.
- Unfold to parton level and compare  $\mathcal{R}$  to the NLO+PS prediction as a function of  $m_{\text{top}}^{\text{pole}}$ .
- Perform  $\chi^2$  minimisation to get  $m_{\text{top}}^{\text{pole}}$  that best describes the data.
- Result:  $m_{\text{top}}^{\text{pole}} = 173.7 \pm 1.5 \text{ (stat.)} \pm 1.4 \text{ (syst.)}^{+1.0}_{-0.5} \text{ (theo.)} \text{ GeV} = 173.7^{+2.3}_{-2.1} \text{ GeV}$

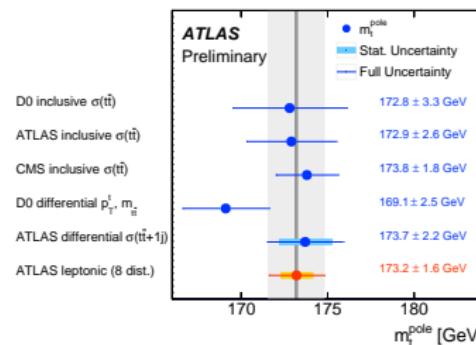
The first measurement of  $m_{\text{top}}^{\text{pole}}$  using this method, still with about 2.2 GeV uncertainty.

# $m_{\text{top}}^{\text{pole}}$ mass from lepton differential cross-sections - additional info

## The top quark $p_T$ spectrum

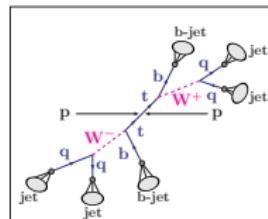


## Comparison of measurements of $m_{\text{top}}^{\text{pole}}$



The largest theoretical uncertainty stems from the choice of the QCD scale.

## Measurement in the all-jets channel from 8 TeV data



### The list of uncertainties

Source of uncertainty	$\Delta m_{\text{top}}$ [GeV]
Monte Carlo generator	$0.18 \pm 0.21$
Hadronisation modelling	$0.64 \pm 0.15$
Parton distribution functions	$0.04 \pm 0.00$
Initial/final-state radiation	$0.10 \pm 0.28$
Underlying event	$0.13 \pm 0.16$
Colour reconnection	$0.12 \pm 0.16$
Bias in template method	0.06
Signal and bkgd parameterisation	0.09
Non all-hadronic $t\bar{t}$ contribution	0.06
ABCD method vs. ABCDEF method	0.16
Trigger efficiency	$0.08 \pm 0.01$
Lepton/ $E_T^{\text{miss}}$ calibration	$0.02 \pm 0.01$
Overall flavour-tagging	$0.10 \pm 0.00$
Jet energy scale (JES)	$0.60 \pm 0.05$
b-jet energy scale (bJES)	$0.34 \pm 0.02$
Jet energy resolution	$0.10 \pm 0.04$
Jet vertex fraction	$0.03 \pm 0.01$
<b>Total systematic uncertainty</b>	1.01
<b>Total statistical uncertainty</b>	0.55
<b>Total uncertainty</b>	1.15

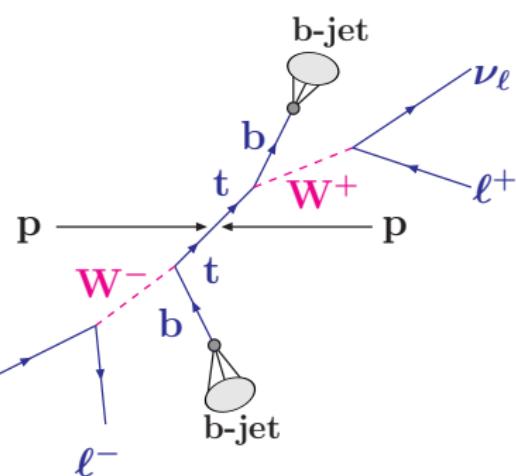
### Numbers of events retained in the selection

Cut	Event yields (thousands)	
	Data	$t\bar{t}$ all-hadronic (MC)
Initial	850450	2338 $\pm$ 1
$N_{\text{PV} > 4 \text{ tracks}}$ & no isolated $e/\mu$	33476	308.7 $\pm$ 0.6
Trigger: 5 jets with $p_T > 55 \text{ GeV}$ & $\geq 6$ good jets	16110	241.4 $\pm$ 0.5
No 2 good jets ( $j_i, j_k$ ) within $\Delta R(j_i, j_k) < 0.6$	7646	142.9 $\pm$ 0.4
$\geq 5$ good jets with $p_T > 60 \text{ GeV}$	3303	51.4 $\pm$ 0.2
$E_T^{\text{miss}} < 60 \text{ GeV}$	3021	46.3 $\pm$ 0.2
$\Delta\phi(b_i, b_j) > 1.5$	1737	30.9 $\pm$ 0.2
$\chi^2 < 11$	645.8	22.3 $\pm$ 0.1
$N_{b_{\text{tag}}} \geq 2$	21.9	6.61 $\pm$ 0.08
$\langle \Delta\phi(b, W) \rangle < 2$	12.9	4.40 $\pm$ 0.07

- Results: 7 TeV:  $m_{\text{top}} = 175.1 \pm 1.4 \text{ (stat)} \pm 1.2 \text{ (syst)} \text{ GeV} = 175.1 \pm 1.8 \text{ GeV.}$
- 8 TeV:  $m_{\text{top}} = 173.72 \pm 0.55 \text{ (stat)} \pm 1.01 \text{ (syst)} \text{ GeV} = 173.72 \pm 1.16 \text{ GeV.}$

An about 40% improvement compared to the 7 TeV analysis.

## The dilepton channel from 8 TeV data



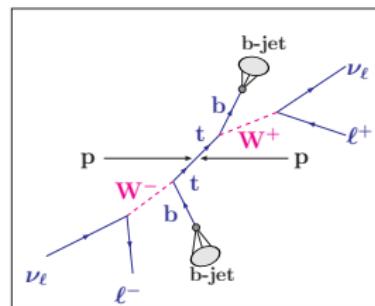
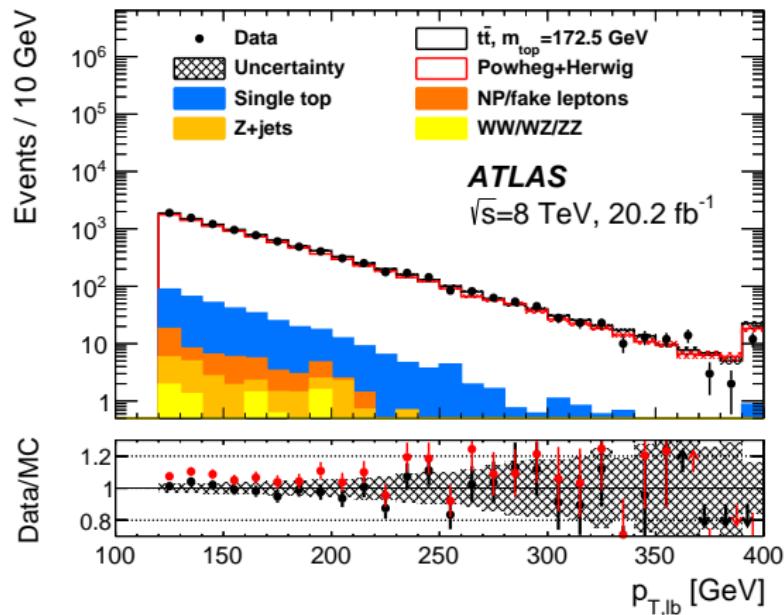
### Pre-selection of events in 8 TeV data

- Use  $W^+W^- \rightarrow \ell^+\ell^-\nu\bar{\nu}$  with  $\ell = e, \mu$ .
- Quality requirements  $\Rightarrow 20.2 \pm 0.4 \text{ fb}^{-1}$ .
- Trigger, good primary vertex  $\geq 5$  tracks.
- Electrons:  $E_T > 25 \text{ GeV}$ ,  $|\eta| < 2.47$ .
- Muons:  $p_t > 25 \text{ GeV}$ ,  $|\eta| < 2.5$ .
- $e\bar{e}, \mu\bar{\mu}$  channel:  $E_T^{\text{miss}} > 60 \text{ GeV}$   
 $m_{ee} > 15 \text{ GeV}$ ,  $|m_{ee} - M_{Z^0}| > 10 \text{ GeV}$ .
- $e\mu$  channel:  $H_T > 130 \text{ GeV}$ .
- At least two jets with  $p_t > 25 \text{ GeV}$  and  $|\eta^{\text{jet}}| < 2.5$ .
- At least one  $b$ -tagged jet ( $\epsilon_b = 70\%$ ).

- Single top quark production is treated as signal rendering an  $m_{\text{top}}$  independent background.

**The pre-selection yields about 36k events with 1% background.**

## The hadronisation uncertainty in 8 TeV data

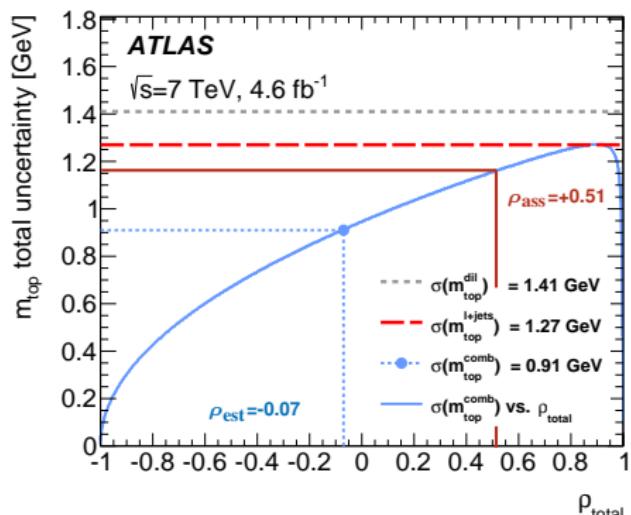


- The difference between POWHEG+PYTHIA and POWHEG+HERWIG results in an hadronisation induced uncertainty in  $m_{\text{top}}$  of  $0.22 \pm 0.09$  GeV.

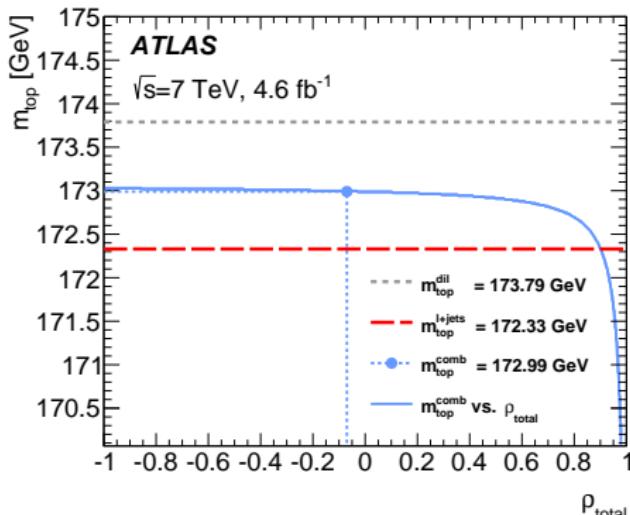
**For this distribution, the data description is better for the POWHEG+HERWIG event sample.**

## Combination - dilepton and lepton + jets at 7 TeV

The uncertainty in  $m_{\text{top}}$



The combined value of  $m_{\text{top}}$

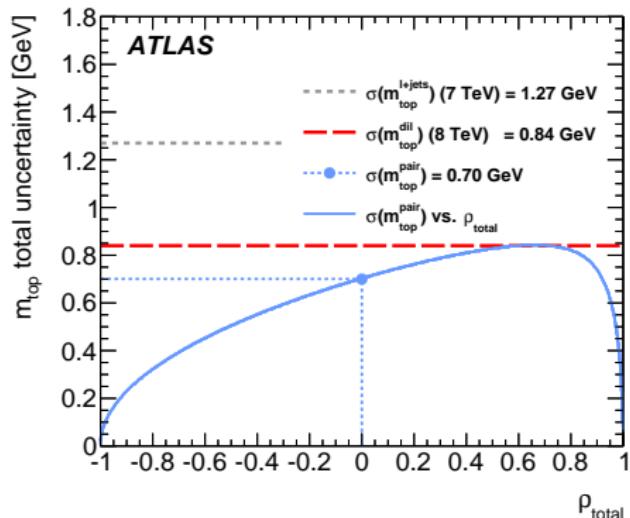


- (1)  $m_{\text{top}} = 172.91 \pm 0.50 \text{ (stat)} \pm 1.05 \text{ (syst)} \text{ GeV}$  (assigned  $\rho_{\text{ass},i}$  from world combination).
  - (2)  $m_{\text{top}} = 172.99 \pm 0.48 \text{ (stat)} \pm 0.78 \text{ (syst)} \text{ GeV}$ , (estimated  $\rho_{\text{est},i}$ ).
- $\Rightarrow \frac{\sigma_2}{\sigma_1} = \frac{0.91}{1.16} = 0.78$ , i.e. a very significant improvement due to the estimated correlations.

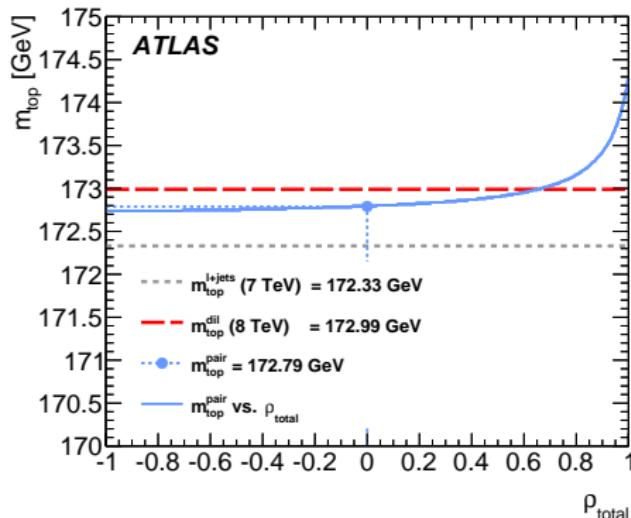
The use of the three-dimensional versus the one-dimensional fit is paying off.

## Combination - dilepton at 8 TeV with lepton + jets at 7 TeV

The uncertainty in  $m_{\text{top}}$



The combined value of  $m_{\text{top}}$



- Large improvement with respect to the more precise result, because the correlation is low,  $\rho = 0.00 \ll \frac{0.84}{1.27} = 0.66 \Leftrightarrow$  the point of no improvement.

**The use of the three-dimensional versus the one-dimensional fit is paying off.**

## The various combinations

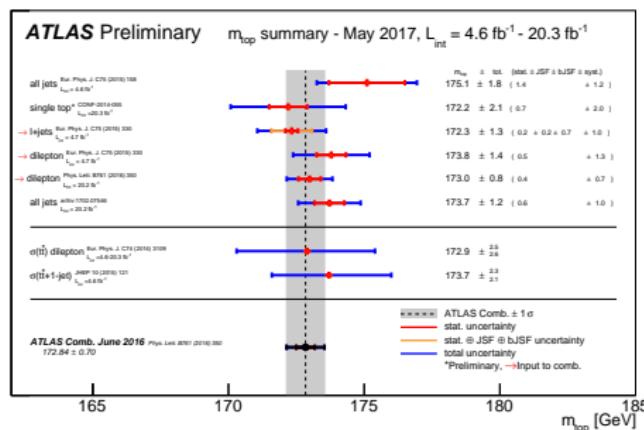
	$\sqrt{s} = 7 \text{ TeV}$			$\sqrt{s} = 8 \text{ TeV}$			Correlations			Combinations		
	$m_{\text{top}}^{\ell+\text{jets}}$ [GeV]	$m_{\text{top}}^{\text{dil}}$ [GeV]	$m_{\text{top}}^{\text{dil}}$ [GeV]	$m_{\text{top}}^{\text{dil}}$ [GeV]	$\rho_{01}$	$\rho_{02}$	$\rho_{12}$	$m_{\text{top}}^7 \text{ TeV}$ [GeV]	$m_{\text{top}}^{\text{dil}}$ [GeV]	$m_{\text{top}}^{\text{all}}$ [GeV]		
		Results	172.33		0	0	0	172.99	173.04	172.84		
Statistics		0.75	0.54	0.41	0	0	0	0.48	0.38	0.34		
Method		0.11 ± 0.10	0.09 ± 0.07	0.05 ± 0.07	0	0	0	0.07	0.05	0.05		
Signal Monte Carlo generator	0.22 ± 0.21	0.26 ± 0.16	0.09 ± 0.15	+1.00	+1.00	+1.00	0.24	0.10	0.14			
Hadronisation	0.18 ± 0.12	0.53 ± 0.09	0.22 ± 0.09	+1.00	+1.00	+1.00	0.34	0.24	0.23			
Initial- and final-state QCD radiation	0.32 ± 0.06	0.47 ± 0.05	0.23 ± 0.07	-1.00	-1.00	+1.00	0.04	0.24	0.08			
Underlying event	0.15 ± 0.07	0.05 ± 0.05	0.10 ± 0.14	-1.00	-1.00	+1.00	0.06	0.10	0.02			
Colour reconnection	0.11 ± 0.07	0.14 ± 0.05	0.03 ± 0.14	-1.00	-1.00	+1.00	0.01	0.03	0.01			
Parton distribution function	0.25 ± 0.00	0.11 ± 0.00	0.05 ± 0.00	+0.57	-0.29	+0.03	0.17	0.04	0.08			
Background normalisation	0.10 ± 0.00	0.04 ± 0.00	0.03 ± 0.00	+1.00	+0.23	+0.23	0.07	0.03	0.04			
$W/Z+\text{jets}$ shape	0.29 ± 0.00	0.00 ± 0.00	0	0	0	0	0.16	0.00	0.09			
Fake leptons shape	0.05 ± 0.00	0.01 ± 0.00	0.08 ± 0.00	+0.23	+0.20	-0.08	0.03	0.07	0.05			
Jet energy scale	0.58 ± 0.11	0.75 ± 0.08	0.54 ± 0.04	-0.23	+0.06	+0.35	0.41	0.52	0.41			
Relative $b$ -to-light-jet energy scale	0.06 ± 0.03	0.68 ± 0.02	0.30 ± 0.01	+1.00	+1.00	+1.00	0.34	0.32	0.25			
Jet energy resolution	0.22 ± 0.11	0.19 ± 0.04	0.09 ± 0.05	-1.00	0	0	0.03	0.08	0.08			
Jet reconstruction efficiency	0.12 ± 0.00	0.07 ± 0.00	0.01 ± 0.00	+1.00	+1.00	+1.00	0.10	0.01	0.04			
Jet vertex fraction	0.01 ± 0.00	0.00 ± 0.00	0.02 ± 0.00	-1.00	+1.00	-1.00	0.00	0.02	0.02			
$b$ -tagging	0.50 ± 0.00	0.07 ± 0.00	0.03 ± 0.02	-0.77	0	0	0.25	0.03	0.15			
Leptons	0.04 ± 0.00	0.13 ± 0.00	0.14 ± 0.01	-0.34	-0.52	+0.96	0.05	0.14	0.09			
$E_T^{\text{miss}}$	0.15 ± 0.04	0.04 ± 0.03	0.01 ± 0.01	-0.15	+0.25	-0.24	0.08	0.01	0.05			
Pile-up	0.02 ± 0.01	0.01 ± 0.00	0.05 ± 0.01	0	0	0	0.01	0.05	0.03			
Total systematic uncertainty	1.03 ± 0.31	1.31 ± 0.23	0.74 ± 0.29				0.77	0.74	0.61			
Total	1.27 ± 0.33	1.41 ± 0.24	0.84 ± 0.29	-0.07	0.00	0.51	0.91	0.84	0.70			

– The combined result:  $m_{\text{top}} = 172.84 \pm 0.34 \text{ (stat)} \pm 0.61 \text{ (syst) GeV} = 172.84 \pm 0.70 \text{ GeV}$ .

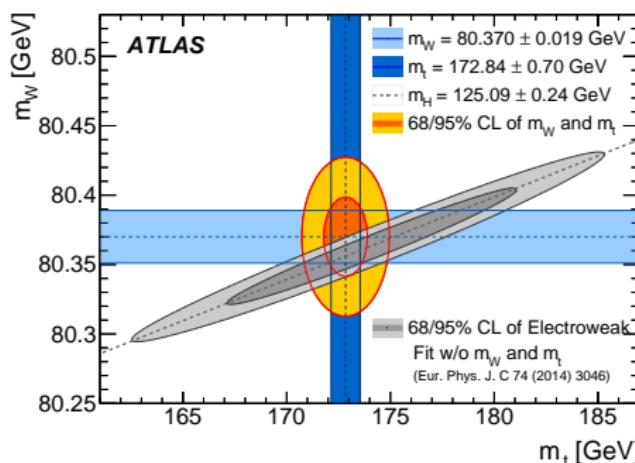
This combination of only three results has a precision of 0.4%.

# Precision measurements and the Standard Model

## The $m_{\text{top}}$ combination



## Consistency of the Standard Model



- The combination of three ATLAS measurements results in:  
 $m_{\text{top}} = 172.84 \pm 0.34 \text{ (stat)} \pm 0.61 \text{ (syst)} \text{ GeV} = 172.84 \pm 0.70 \text{ GeV (0.4%).}$
- The good description of the precise measurements of  $m_W$  with  $\sigma(m_W) = 0.02\%$ ,  $m_{\text{top}}$  with  $\sigma(m_{\text{top}}) = 0.4\%$  and  $M_H$  with  $\sigma(M_H) = 0.2\%$  (from LHC) is another success of the SM.

The Standard Model has successfully passed another precision test.