# Distortion Corrections for the ALEPH TPC

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# **Overview**

- Brief overview of the detector
- Historical development
- Distortion corrections for the TPC
- Tour through some problems and their correction
- Detector performances
- Summary

### **The ALEPH Detector**



TPC



- rφ from pad position
  z from drift time (pads + wires)
- dE/dx from wires and pads

- Length = 4.7 m
- Outer radius = 1.8 m
- Total weight = 3.6 t
- Drift length  $2 \times 2.2m$
- Up to 21 space points / track
- 18 wire chambers / endplate
- 47340 channels in total
- B = 15 kG
- HV (Membrane) = -27.5 kV
- Gas
  - Volume  $43m^3$
  - Argon/Methan (91:9) at atmospheric pressure
- Angular coverage
  - $2\pi$  in  $\varphi$
  - 21 pad rows hit for  $|\cos \Theta| \le 0.8$
  - At least 3 pad rows for  $|\cos \Theta| \le 0.97$



# **Historical Development**

#### LEP startup 1989 –1990

- Failure of magnet compensating power supplies in 1989 requires development of field correction methods
  - Derived from 2 special Laser runs (B on/off)
  - Correction methods described in NIM A306(1991)446
- High statics Muon pairs from Z-decay is main calibration sample

# 1991-1994 (LEP 1)

- Silicon Vertex Detector 1 becomes operational in 1991
- Development of common alignment procedures for all three tracking detectors
- Incidents affect large portions of collected statistics and require correction methods based directly on data
  - 1991–1993 7 shorts on field cage affect 24% of collected data.
     1994 disconnected gating grids make 20% of data unusable
  - All data finally recuperated with data-based correction models

## 1994–1996 (LEP 1/2)

- Aleph Tracking Upgrade Program (Reprocessing of LEP 1 data)
  - Improved coordinate determination requires better understanding of systematic effects.
  - Combined calculations for field and alignment distortions in TPC. Reevaluation of B-field map.
  - All methods for distortion corrections are based now directly on data
  - Development of "few" parameter correction models to cope with drastically reduced calibration samples at LEP 2.
  - Use high statistics LEP 1 muon pairs to make improved maps also for LEP 2

# 1995-2000 (LEP 2)

- New VDET 2 with larger acceptance (end 1995)
- Z pairs are only available in special calibration runs at begin of running period and on request from experiments after incidents. Very limited statistics compared to LEP 1.
- More frequent beam losses cause time dependent "charge up" effects in the TPC and new shorts. Both distortions are superimposed.
  - For short corrections LEP delivers small amount of Z pairs (~700 muon pairs) on experiment's request.
  - Time dependent effects are usually present throughout the year and have to be tracked with hadrons.

# Distortion Corrections for the TPC

- Use real data : Muon pairs from Z–decays
- Prerequisite: preliminary calibration of inner tracking detectors exists already
  - Global alignment e.g. from survey measurements or from previous data alignments
  - Internal calibration for VDET and ITC (Can be done without TPC)
- Fit the 2 tracks of each muon pair with a common single helix
  - Momentum is constrained to beam energy
  - Helix parameters are determined with 4 hits from VDET and up to 16 hits from ITC. TPC is not in the track fit.



• Measure coordinate residuals in TPC respective to extrapolated single helix on 3 dimensional grid  $(\Delta r \varphi, \Delta z)_{obs.}(r_n, \varphi_n, z_n)$ 



 $d_0$  = Signed distance of closest approach to origin

- Compute for fields and alignment  $(\Delta r \varphi, \Delta r, \Delta z)_{Fields, Alignment}$  from
  - Potential for fields
  - Coordinate transformation equations for alignment

$$\Rightarrow \Delta r \varphi_{Fields,Alignment}(r,\varphi,z) = \sum_{i} \Delta \widehat{r \varphi}_{i}(r,\varphi,z) \cdot A_{i}$$

Computed from first principles

- Solve (overdetermined) system of linear equations for unknown parameters  $\boldsymbol{A}_{i}$ 

$$\begin{pmatrix} \Delta r \varphi_{obs}(r_{1},\varphi_{1},z_{1}) \\ \Delta z_{obs}(r_{1},\varphi_{1},z_{1}) \\ \vdots \\ \Delta r \varphi_{obs}(r_{N},\varphi_{N},z_{N}) \\ \Delta z_{obs}(r_{N},\varphi_{N},z_{N}) \end{pmatrix} - \begin{pmatrix} \Delta \widehat{r}\widehat{\varphi}_{1}(r_{1},\varphi_{1},z_{1}) & \cdots & \Delta \widehat{r}\widehat{\varphi}_{M}(r_{1},\varphi_{1},z_{1}) \\ \Delta \widehat{z}_{1}(r_{1},\varphi_{1},z_{1}) & \cdots & \Delta \widehat{z}_{M}(r_{1},\varphi_{1},z_{1}) \\ \vdots & \vdots \\ \Delta \widehat{r}\widehat{\varphi}_{1}(r_{N},\varphi_{N},z_{N}) & \cdots & \Delta \widehat{r}\widehat{\varphi}_{M}(r_{N},\varphi_{N},z_{N}) \\ \Delta \widehat{z}_{1}(r_{N},\varphi_{N},z_{N}) & \cdots & \Delta \widehat{z}_{M}(r_{N},\varphi_{N},z_{N}) \end{pmatrix} \cdot \begin{pmatrix} A_{1} \\ \vdots \\ A_{M} \end{pmatrix} = Min$$

- Solve system of linear equations with <u>Singular Value</u>
   <u>Decomposition</u> (SVD) (e.g. Numerical Recipes, Cambridge University Press)
  - *SVD* can cope with linear dependencies in function matrix. Solution has from all possibilities the smallest length.  $\|\vec{A}\| = Min$
  - SVD provides for each parameter a weight which allows to identify insignificant parameters to the problem (i.e. remove all parameters with weight < threshold)</li>

# Ansatz for $(\Delta \hat{r} \varphi, \Delta \hat{r}, \Delta \hat{z})_{Fields}$

Start with Potential

$$\begin{split} \Phi_{E} &= U_{0} \left( 1 - \frac{|z|}{z_{M}} \right) - U_{0} \tilde{\Phi}_{E}(r, \varphi, z) ; \quad U_{0} \simeq -27 \, kV ; \quad \left| \tilde{\Phi}_{E}(r, \varphi, z) \right| \ll 1 ; \quad E - Field \\ \Phi_{B} &= -B_{z}^{0} z - B_{z}^{0} z_{M} \tilde{\Phi}_{B}(r, \varphi, z) ; \quad B_{z}^{0} \simeq 15 \, kG ; \quad \left| \tilde{\Phi}_{B}(r, \varphi, z) \right| \ll 1 ; \quad B - Field \end{split}$$

• Calculate solutions for Laplace equation for double cylinder

$$\Delta \Phi = 0$$
;  $\rightarrow \Phi = \sum_{ij} a_{ij} \Phi_{ij}(r, \varphi, z)$ ;

Compute

$$\vec{E} = -\nabla \Phi_E$$
;  $\vec{B} = -\nabla \Phi_B$ 

• Compute distortions from Langevin equation

$$\vec{v} = \frac{\mu}{1 + (\omega \tau)^2} \left( \vec{E} + (\omega \tau) \frac{\vec{E} \times \vec{B}}{|\vec{B}|} + (\omega \tau)^2 \frac{\vec{B} (\vec{E} \cdot \vec{B})}{\vec{B}^2} \right)$$

$$\begin{split} \Delta \widehat{r\varphi}_{E} &= \frac{1}{1 + (\omega\tau)^{2}} \int_{z}^{z_{M}} \left( \frac{E_{\varphi}}{E_{z}} - (\omega\tau) \operatorname{sign}(B_{z}) \frac{E_{r}}{E_{z}} \right) dz ; \quad \Delta \widehat{r}_{E} = \frac{1}{1 + (\omega\tau)^{2}} \int_{z}^{z_{M}} \left( \frac{E_{r}}{E_{z}} - (\omega\tau) \operatorname{sign}(B_{z}) \frac{E_{\varphi}}{E_{z}} \right) dz ; \\ \Delta \widehat{r\varphi}_{B} &= \frac{(\omega\tau)}{1 + (\omega\tau)^{2}} \int_{z}^{z_{M}} \left( (\omega\tau) \frac{B_{\varphi}}{B_{z}} - \frac{B_{r}}{|B_{z}|} \right) dz ; \quad \Delta \widehat{r}_{B} = \frac{(\omega\tau)}{1 + (\omega\tau)^{2}} \int_{z}^{z_{M}} \left( (\omega\tau) \frac{B_{r}}{B_{z}} - \frac{B_{\varphi}}{|B_{z}|} \right) ; \end{split}$$

$$r(z) \simeq r + \frac{\partial r}{\partial z} \delta z ; \quad \varphi(z) \simeq \varphi + \frac{\partial \varphi}{\partial z} \delta z ; \quad \left| \frac{\partial r}{\partial z} \right|, \left| \frac{\partial \varphi}{\partial z} \right| \ll 1$$

Approximations:

$$E_{z}(r,\varphi,z) \simeq E_{z}^{0} = \pm \frac{U_{0}}{z_{M}}; B_{z}(r,\varphi,z) \simeq B_{z}^{0};$$

#### **Characteristics of Solutions**

• Solution by separation of variables. 3 classes of solutions corresponding to choice of separation variable  $k^2$ 



• 
$$k^2 > 0$$
  

$$\tilde{\Phi}_{vm} = \Psi_{vm}(\lambda_{vm}r) \left( A_{vm} \sin(v\varphi) + B_{vm} \cos(v\varphi) \right) \begin{pmatrix} \frac{\sinh(\lambda_{vm}|z|)}{\sinh(\lambda_{vm}z_M)} \\ \frac{\sinh(\lambda_{vm}|z|)}{\sinh(\lambda_{vm}z_M)} \\ \frac{\sinh(\lambda_{vm}|z|)}{\sinh(\lambda_{vm}z_M)} \end{pmatrix};$$

$$\Psi_{vm}(\lambda_{vm}r) = \begin{vmatrix} J_v(\lambda_{vm}r_i) & N_v(\lambda_{vm}r_i) \\ J_v(\lambda_{vm}r) & N_v(\lambda_{vm}r) \end{vmatrix}; \quad \Psi_{vm}(\lambda_{vm}r_i) = \Psi_{vm}(\lambda_{vm}r_o) = 0;$$

$$v = 0...\infty; m = 1...\infty;$$

• 
$$k^2 < 0$$
  

$$\tilde{\Phi}_{vm} = \begin{pmatrix}
P_{vm, FCout}(\lambda_m r) \\
P_{vm, FCin}(\lambda_m r)
\end{pmatrix} \begin{pmatrix}
A_{vm} \sin(v \phi) + B_{vm} \cos(v \phi) \\
B_{vm} \sin(\lambda_m r) + B_{vm} \cos(v \phi) \\
P_{vm, FCout}(\lambda_m r) + B_{vm} \cos$$

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#### Greensfunction

$$\Delta_{\vec{x}} G(\vec{x}, \hat{\vec{x}}) = -4\pi \,\delta(\vec{x} - \hat{\vec{x}}) ; \quad G(\vec{x}, \hat{\vec{x}}) = 0 ; \quad \vec{x}, \hat{\vec{x}} \in Boundary$$

Solution with Ansatz:  $G(\vec{x}, \hat{\vec{x}}) = \sum_{\Lambda} a_{\Lambda}(\hat{\vec{x}}) U_{\Lambda}(\vec{x});$ 

$$\Rightarrow \qquad G(\vec{x}, \hat{\vec{x}}) = 4\pi \sum_{\Lambda} \frac{1}{\Lambda^2} U_{\Lambda}(\hat{\vec{x}}) U_{\Lambda}(\vec{x}) ;$$

*U* fulfills Helmholtz equation :

$$\Delta U_{\Lambda} + \Lambda^2 U_{\Lambda} = 0 ; \quad U_{\Lambda}(\vec{x}) = 0 ; \quad \vec{x} \in Boundary$$

$$U_{\Lambda_{vmn}}(r,\varphi,z) = \frac{1}{N_{vmn}} \Psi_{vm}(\lambda_{vm}r) \left( \frac{\sin(v\varphi)}{\cos(v\varphi)} \right) \sin\left( \frac{n\pi}{z_M} z \right); \quad \Lambda_{vmn}^2 = \lambda_{vm}^2 + \left( \frac{n\pi}{z_M} \right)^2;$$

# Ansatz for $(\Delta \hat{r} \varphi, \Delta \hat{r}, \Delta \hat{z})_{Alignment}$

Transformation from measured TPC coordinate to global ALEPH coordinate

$$\vec{x}_{\aleph} = A_3 \left( A_2 \left( A_1 \vec{x}_{TPC} + \vec{t}_1 \right) + \vec{t}_2 \right) + \vec{t}_3 ; \quad \stackrel{1. TPC sector frame \to TPC endplate frame}{2. TPC endplate frame \to TPC frame} \\ \stackrel{3. TPC frame \to Aleph global coordinate system}{3. TPC frame \to Aleph global coordinate system}$$

- Compute  $\Delta \vec{x}_{\aleph}$  as function of small variations of  $(A_i, \vec{t}_i)$  *e.g.*  $A_2 = R_x R_y R_z$ ;  $\Rightarrow \Delta A_2 = 9 T_x R_x R_y R_z + \delta R_x T_y R_y R_z + \phi R_x R_y T_z R_z$ ;  $R_{x,y,z} = Rotations of SO(3), T_{x,y,z} = Generators of Lie Algebra of SO(3)$
- Apply boundary conditions to alignment parameters, e.g endplate alignment should not move complete TPC

$$\rightarrow$$
  $\equiv$   $\rightarrow$ 

- Alignment and field corrections are not independent
  - e.g tilt of "perfect TPC" relative to B–field axis causes transverse drift velocities



• e.g bowing of the TPC endplate requires alignment and E-field corrections  $\mathbf{k} \cdot \mathbf{r} = \hat{\mathbf{r}}$ 

 $\begin{array}{c} & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & & & \\ & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ &$ 

#### Remarks

- There are other corrections (e.g. timing shifts in hardware) which may interfere with the above corrections.
- With the single helix fit residuals can only be measured in a limited acceptance region, i.e.
  - Field and alignment corrections can not always be distinguished. The solution may be not unique.
  - Fit matrix can be therefore almost degenerate ( $\rightarrow$  SVD).
  - "External" information helps in guiding the fit.



- Direct fitting of Fourierseries for field distortions is avoided
  - Slow convergence = many coefficients needed
  - Practical problems for numerical solutions
  - Does not allow to identify the contributing distortions
  - Normally a simple parameterised potential on the boundary is constructed and transformed via the Greensfunction in a parameterised distortion map (see examples later)
- The calibration is done iteratively (typically 2 iterations)





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#### Fourieranalysis

- Powerspectrum from measured residuals
- No corrections applied to data
- v=0 : fields (Eand B-map needed)
- v=1 : mainly global alignment
- v > 1 : mainly internal alignment (e.g. sector alignment)

#### Data without corrections



# Tour through some problems and their correction

- Static problems (always there)
  - TPC tilt
  - Endplate bowing
  - Nonlinear potential on fieldcage
- Single incidents
  - Disconnected gating grids (space charge)
  - Shorts on field cage
- Time dependent effects
  - "Charge up" effects

#### **Tilt of TPC**

 $\Delta r \varphi(r, \varphi, z) = r \phi_G - (\delta x)_G \sin \varphi + (\delta y)_G \cos \varphi - sign(z) z_M(\delta_G \sin \varphi + \vartheta_G \cos \varphi)$ 

- Example for coupling of field and alignment corrections
- Tilt already seen in survey measurements
- Confirmed with cosmic run (low statistics)
- Data were used to improve the previous measurements and to monitor time dependence



## **Bowing of TPC endpaltes**

- Discovered after installation of VDET 1
- Endplate bows outward (TPC has slight overpressure)
- Main effect
  - ~ 1mm bowing
- Small variation with time
- Coupling of alignment and field corrections (phi dependence from sectors)



Alignment

$$\Delta z(r,\varphi) = \sum_{S} \left( \vartheta_{S} r \sin(\varphi - \overline{\Phi}_{S}) + \delta_{S} (R_{S} - r \cos(\varphi - \overline{\Phi}_{S})) + (\delta z)_{S} \right);$$

Endplate is equipotential surface

$$\Phi(r,\varphi,z_{M}+\Delta z(r,\varphi))=0; \quad \Rightarrow \quad \tilde{\Phi}(r,\varphi,z_{M})\simeq -\frac{\Delta z(r,\varphi)}{z_{M}};$$

Distortionpotential

$$\tilde{\Phi}(r,\varphi,z) = -\sum_{\nu m} \frac{1}{2N_{\nu m}^{2}} (A_{\nu m} \sin \nu \varphi + B_{\nu m} \cos \nu \varphi) \Psi_{\nu m}(\lambda_{\nu m} r) \frac{\sinh(\lambda_{\nu m} z)}{\sinh(\lambda_{\nu m} z_{M})};$$

$$\begin{pmatrix} A_{\nu m} \\ B_{\nu m} \end{pmatrix} = \int_{r_{i}}^{r_{o}} \int_{0}^{2\pi} \Delta z(r,\varphi) \Psi_{\nu m}(\lambda_{\nu m} r) \begin{pmatrix} \sin \nu \varphi \\ \cos \nu \varphi \end{pmatrix} r \, dr \, d\varphi ;$$

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## **Nonlinear Potential on Field Cage**

Possible sources

- Manufacturing errors on electrodes
- Nonlinear resistor chain
- Finite resistivity of FC insulator





• Results from fit can be interpreted as potential deviation or axial shift of electrodes

• Fit prefers  $\rho \simeq 10^{16} [\Omega \ cm]$ 





#### **Correction for nonlinear potential + endplate bowing**

## **Disconnected Gating Grids**

- In 1994 the gating grids of 2 sectors got disconnected
  - ~10% of collected statistics affected
  - Endplate potential changes
  - Ions escape into TPC volume (spacecharge)
- Distortions depend on <u>azimuthal angle</u> and on <u>current</u>





#### Data 1994



#### **Short on Field Cage**

- History
  - First one end of 1991 (~13% of collected data affected)
    - Sharp edge on electrode damaged FC insulator
    - During repair carbon fibres were introduced in the TPC volume
  - 1992: series of 5 shorts (~41% of collected data affected)
  - 1993: 1 short (~10% of collected data affected)
  - July 1999: short after beam loss (~58% of collected data affected)
    - Appears just before LEP ramps CM energy to 200 GeV
  - August–September 2000: short appears after beam loss and disappears after a second one (~15% of collected data affected)
    - Higgshunt

## Characteristics

- Appear typically after beam loss
- $R\varphi$  residuals in TPC ~ 1 [mm]  $\Rightarrow$  severe impact on tracking
- Except for the 1991 short all shorts are due to introduced carbon fibres
  - Short may disappear again (1992, 2000)
  - Position of fibre may change after a new beam loss (e.g. 1992)
  - Fibre may be not found or at a different place during a TPC opening = short position not necessarily known from intervention
     ⇒ corrections from data are essential
- At LEP2 shorts were always accompanied by time dependent "charge up effects" on inner FC
   ⇒ need for parameterised model to disentangle both effects in data







$$\tilde{\Phi}(r,\varphi,z) \simeq sign(z_s) \left(\frac{\Delta U_0}{U_0}\right) \sum_{n} \frac{\cos(\frac{n\pi}{z_M} z_s)}{n\pi} \sin(\frac{n\pi}{z_M} z) P_{On, FCont}(\frac{n\pi}{z_M} r);$$





Short 1999 : Fit with all tracking detectors

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## "Charge up" effects on Field Cage

- History
  - First observed 1992 after a beamloss which caused also a short
  - At LEP2 observed every year (beam losses were more frequent)
- Characteristics
  - Effect on inner FC, near interaction point ,  $\Delta r \phi \sim 200 \ [\mu m]$  at inner padrows
  - Residuals depend on time, decaytime ~ month
  - No convincing azimuthal dependence observed
  - Impact on physics: mainly bias on impact parameter
  - Source: unknown
- Corrections can not be done with  $\mu$ -pairs at LEP2  $\rightarrow$  not enough statistics to follow time evolution









- Model parameters
  - Position  $z_0(\varphi_0)$

• Width 
$$z_{w}(\dot{\boldsymbol{\varphi}}_{w})$$

- $\Delta V$
- Data are binned in time intervals and fitted with model

Distortion potential (independent of  $\varphi$ )





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- Corrections fitted with Hadrons in time slices
- Result tested with muon pairs



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# **Tracking Spectrometer Resolutions**

- All data are from 1997 to 2000
- Calibration data
  - Muon pairs taken at Z with no known detector problem
  - High statistics
  - Represent optimal resolutions
  - Calibration data for corrections of TPC problems are shown separately
- High energy muon pairs
  - Include also all periods with detector problems (e.g. shorts)
  - Low statistics
  - Test corrections obtained at Z or with Hadrons

#### **Impact Parameter Resolution**



#### **Impact Parameter Resolution**



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#### Momentum Resolution

Calibration Data

## High Energy Data



### Momentum Resolution



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## **Calibration Data for TPC Problems**



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# Summary

- Mathematical distortion correction models with only a <u>small</u> <u>number of free parameters</u> and mainly <u>data driven correction</u> <u>methods</u> allowed
  - to understand the different distortion contributions
  - to cope with limited calibration samples (e.g. at LEP 2)
  - to recuperate large portions of data which were affected by incidents
  - to follow time dependent effects
  - to maintain the spectrometer resolutions throughout the running periods

- Muon pairs from Z decays with its kinematic constraints provided a unique reaction to measure residual distributions in the TPC directly with data
  - no a priori assumptions about TPC distortions (>< "Hadron fit")
  - limits the application of some of the correction methods in other environments besides unbiased residual distributions can be obtained with other methods